



# Top Mass Measurements at the Tevatron

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for the CDF and D0 collaborations*



# Today's Menu



- Why are top mass measurements so interesting?
- The Tevatron
- Experimental challenges
- Measurements of the top mass:
  - The methods en bref
  - Flagship measurements in the semileptonic channel
  - All-hadronic channel
  - Dilepton channel
- Finita la comedia!





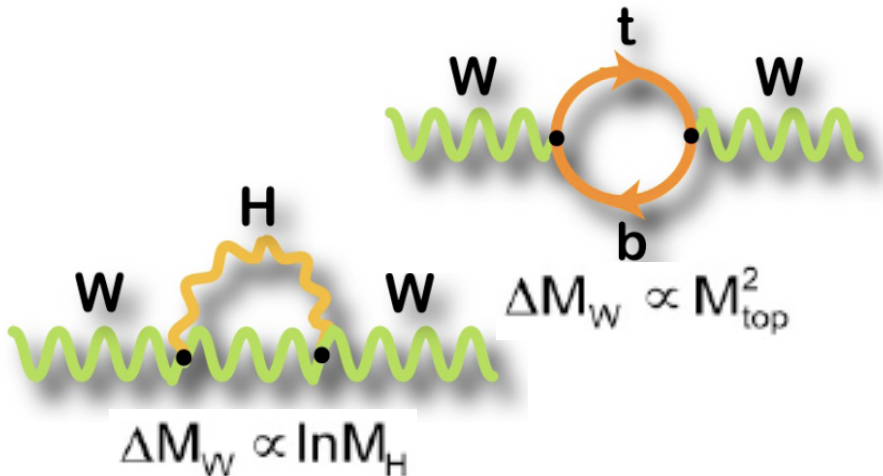
# Top Mass Measurement Motivation



- The top is special:
  - Heaviest particle of the SM
  - Yukawa coupling is  $\sim 1$ 
    - Special role in EW symmetry breaking?



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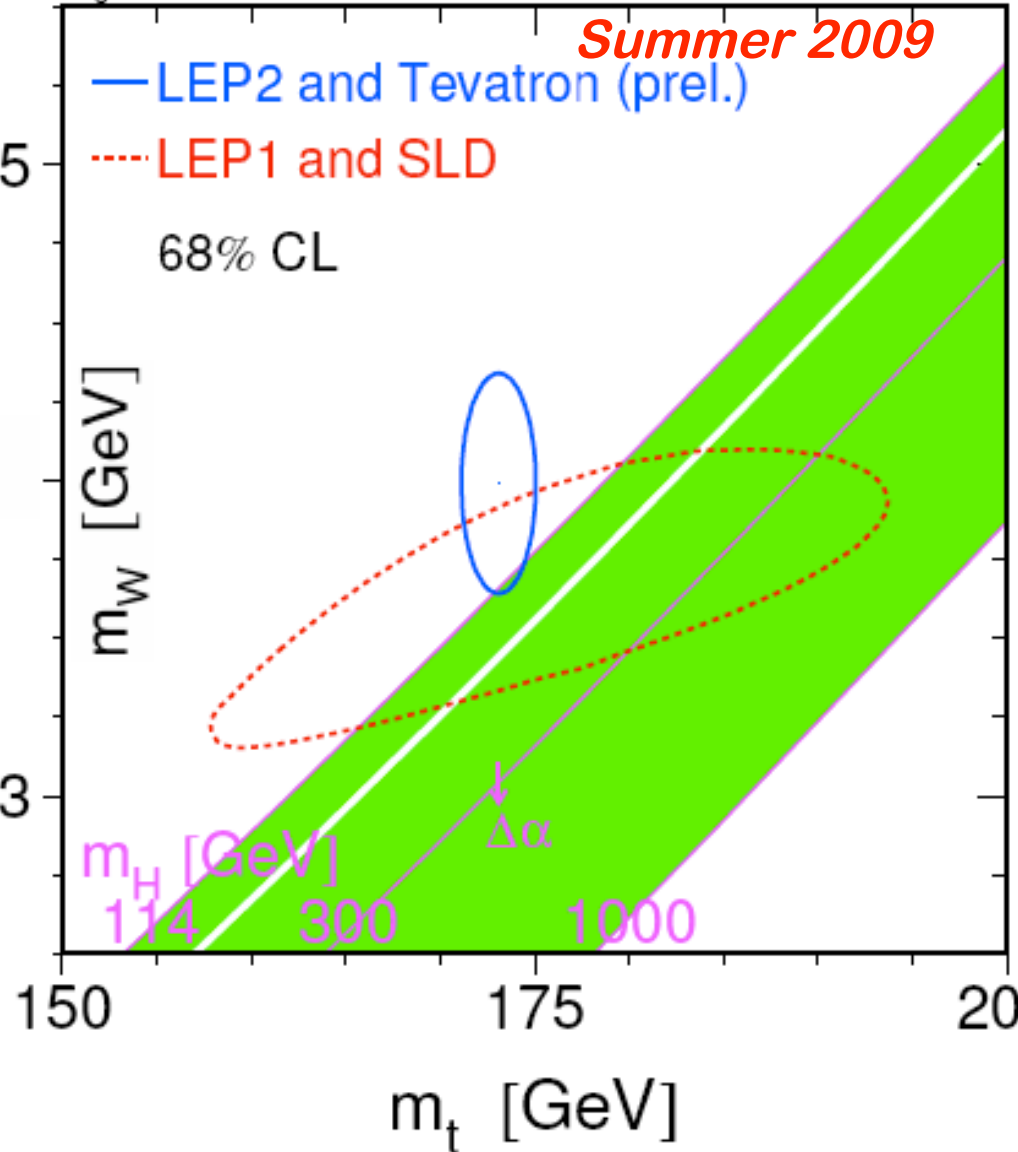
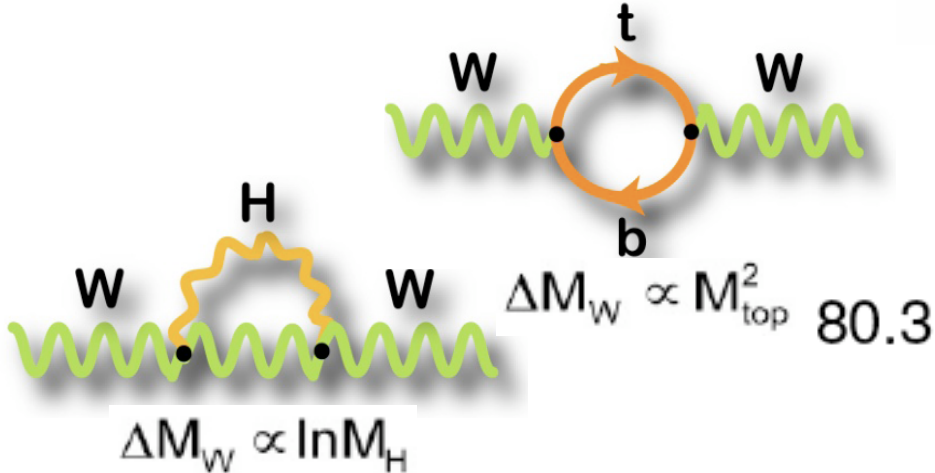
# Top Mass Measurement Motivation



August 2009

Summer 2009

- The top is special:
  - Heaviest particle of the SM
  - Yukawa coupling is  $\sim 1$ 
    - Special role in EW symmetry breaking?
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- Waiting for newest EW fits!
- 1 GeV change in  $m_{top} \rightarrow$   
 $\sim 10$  GeV change in  $m_{higgs}$



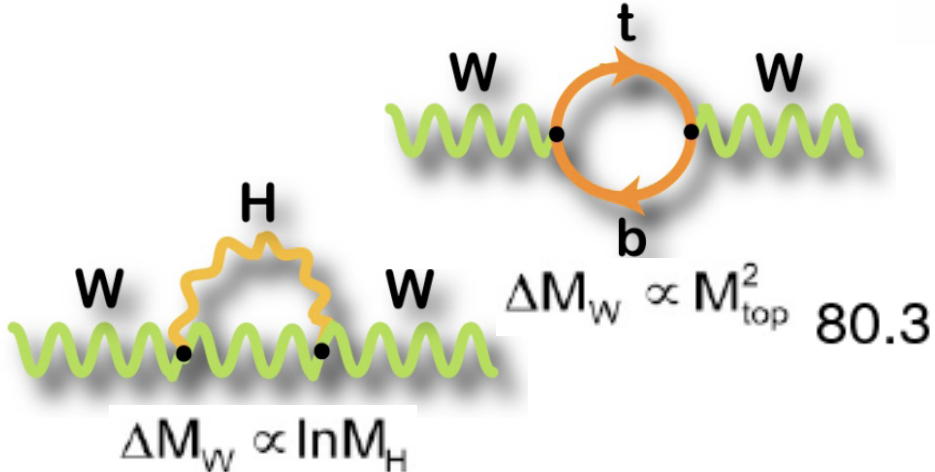


# Top Mass Measurement Motivation

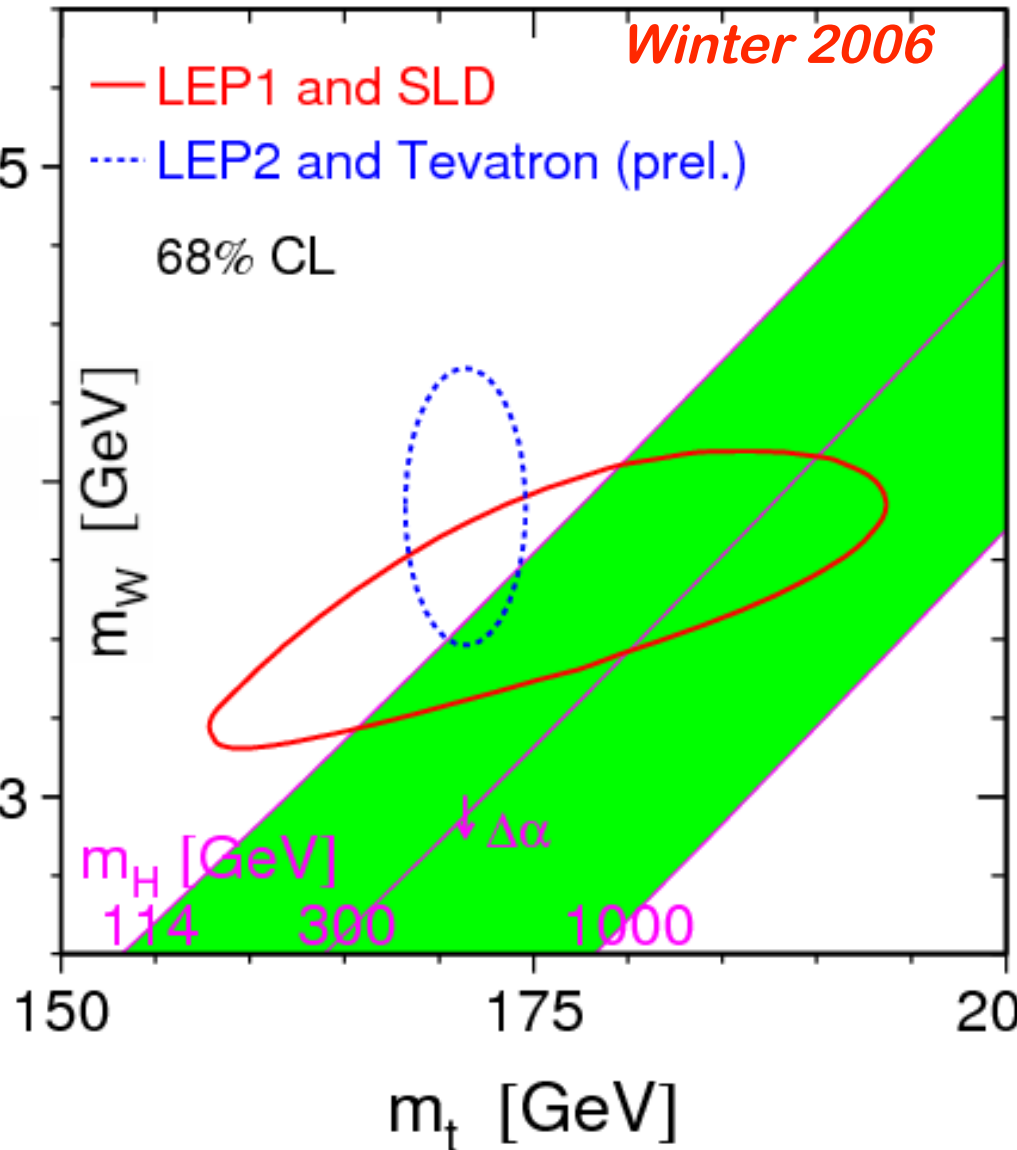


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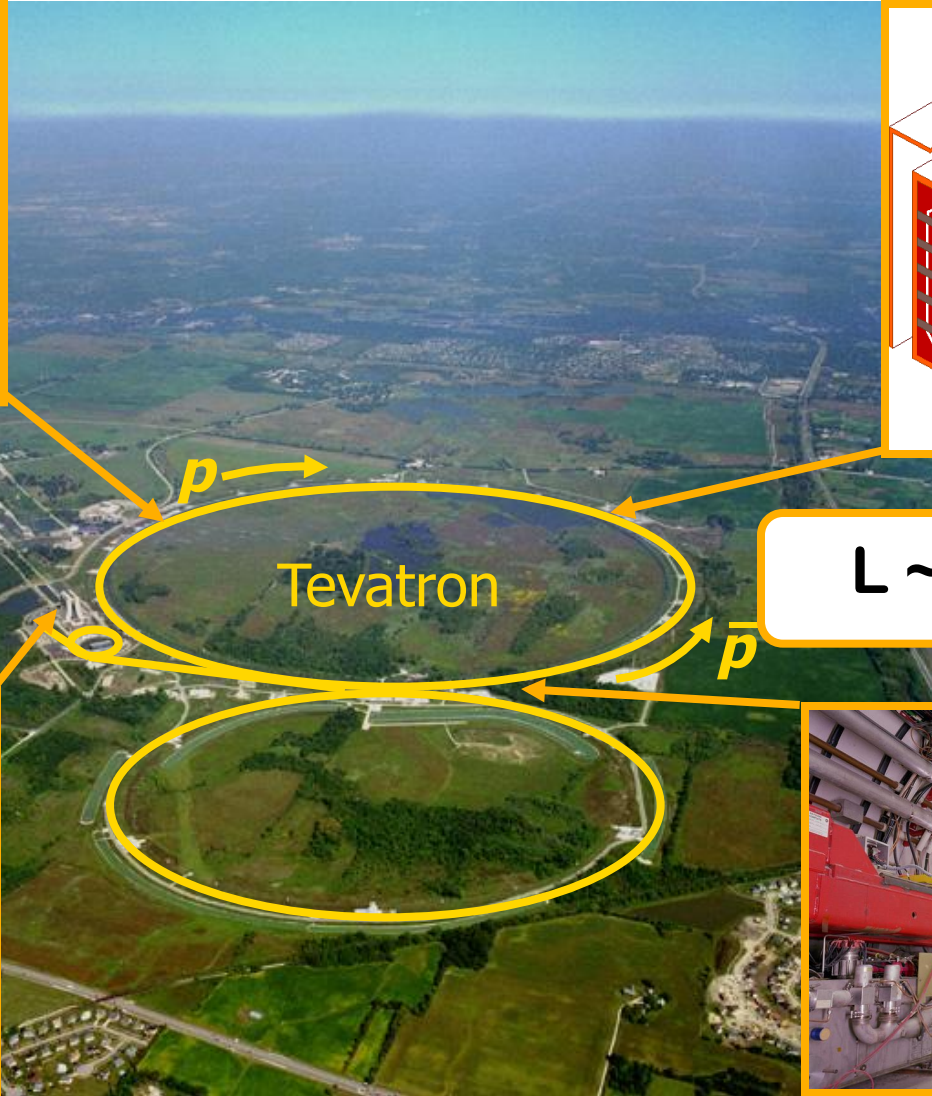
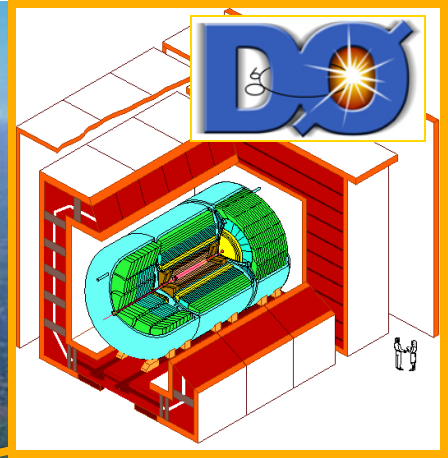
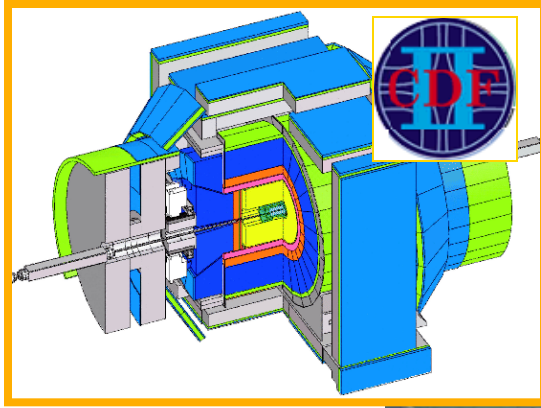


- Waiting for newest EW fits!
- 1 GeV change in  $m_{top}$   $\rightarrow$   $\sim 10$  GeV change in  $m_{higgs}$





# The Tevatron: a Top Factory



$\sqrt{s} = 1.96 \text{ TeV}$

$L \sim 7.5 \text{ fb}^{-1} \text{ p.e.}$

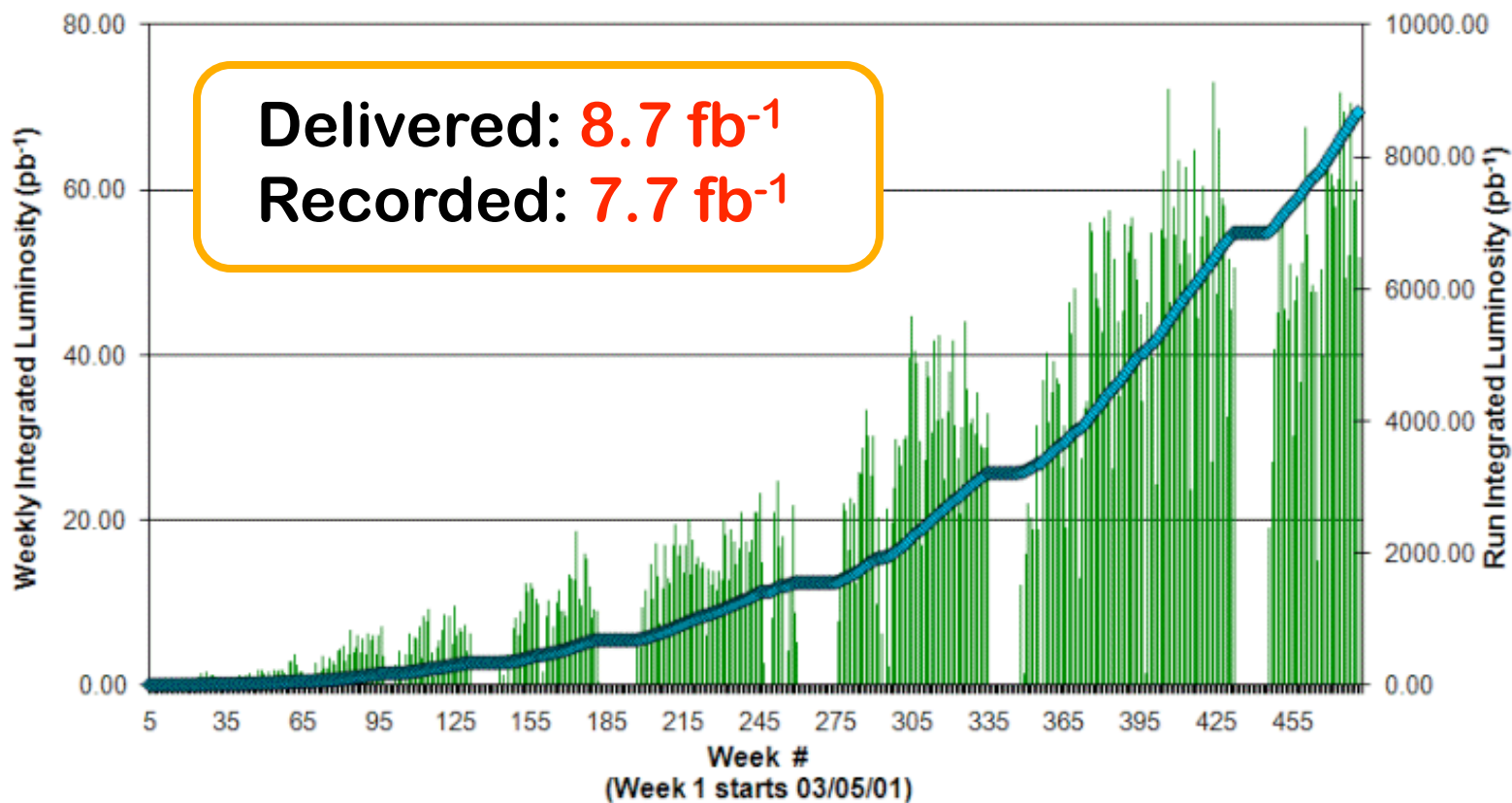




# The Tevatron Performance for the Top!



- Tevatron has shown a great performance in FY 2010!
- We keep enlarging our calibration samples
  - Better handles on experimental uncertainties:
    - e.g. Jet Energy Scale (JES), Jet Energy Resolution, etc.





- The Tevatron is a hadron collider
  - Very high backgrounds!
- Backgrounds can bias the top mass measurement

Typical Backgrounds:

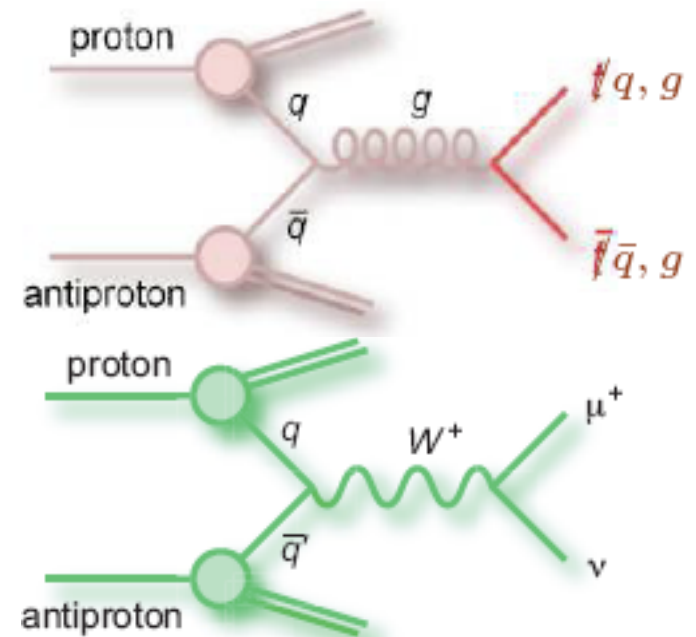
W+jets

Z+jets

QCD multijet prod'n

Diboson prod'n

Single top prod'n



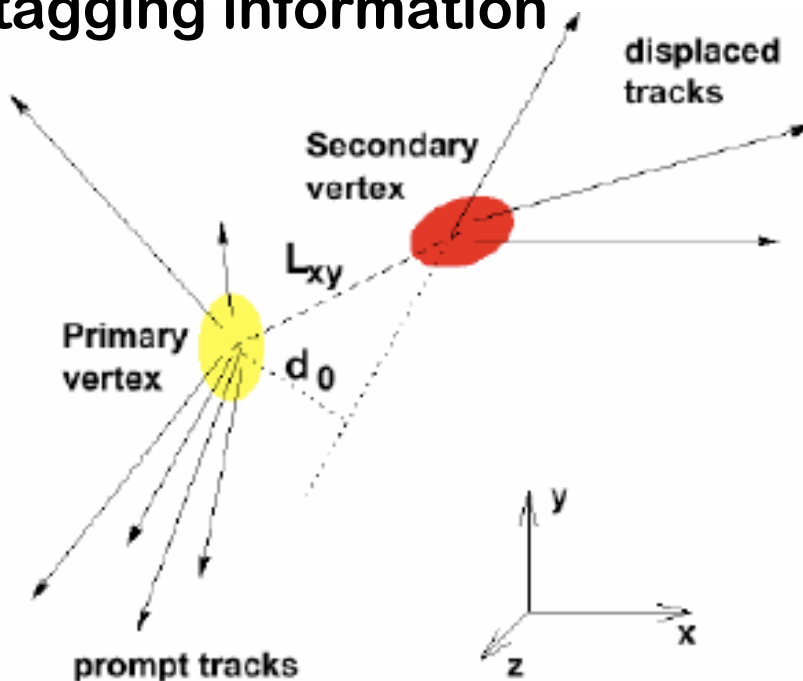
See talk by F. Deliot (top Xsec)



# Top Mass: Experimental Challenges



- The Tevatron is a hadron collider
  - Very high backgrounds!
- Backgrounds can bias the top mass measurement
- Control backgrounds using b-tagging information

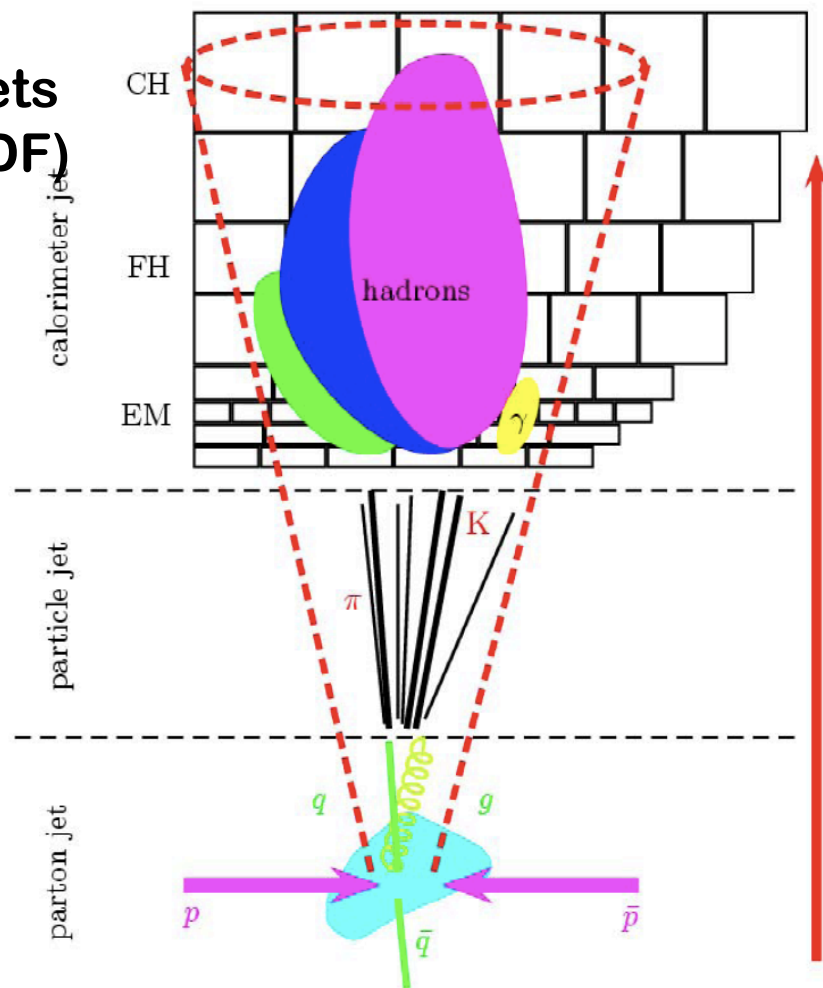


Channel	B-tags	S:B	Perm.
Dilepton	$\geq 0$	1:4	2
	$\geq 1$	4:1	2
Lepton+jets	$\geq 0$	< 1:1	12
	$\geq 1$	2.5:1	6
	$\geq 2$	10:1	2
All-hadronic	$\geq 1$	1:4	30
	$\geq 2$	4:1	6

At the same time:  
 → help combinatorics!



- We are interested in **parton-level quantities** for our top mass measurement
  - Map the energies of reco-level jets to particle jets (D0) / partons (CDF)
  - This is referred to as a Jet Energy Scale (JES) corr'n
  - With the current size of calibration samples:
    - $\sigma(\text{JES})/\text{JES} \sim 1.5\%$  (D0)
    - $\sigma(\text{JES})/\text{JES} \sim 3\%$  (CDF)
- And many more:
  - Lepton ID,  $p_T$  scale
  - Signal, background model
  - ISR, FSR
  - ...
  - → cover some in the systematics discussion





# Top Mass Measurement: Methods



- The measurements shown today are based on:
  - Template method
  - Matrix Element method

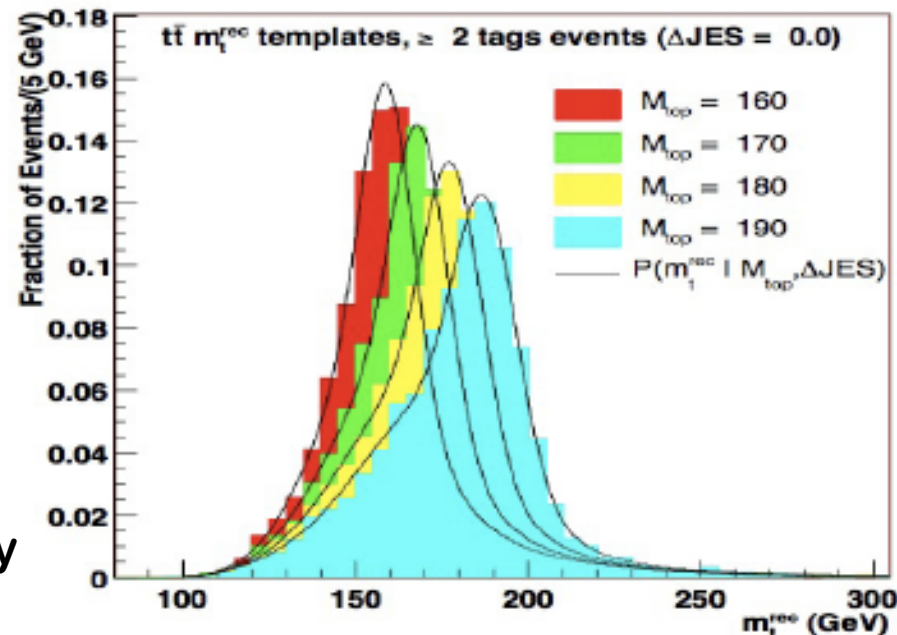


- The measurements shown today are based on:

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- **Template method:**

- Pick a set of variables  $x_i$  sensitive to  $m_{\text{top}}$
- Create **“templates” = distributions of  $x_i$  using MC**
  - For signal:  $x_i = x_i(m_{\text{top}})$
  - For background
- Maximise the likelihood of their consistence with the observation
- Advantages:
  - Few assumptions
  - fairly straight forward
  - Combination of channels easy



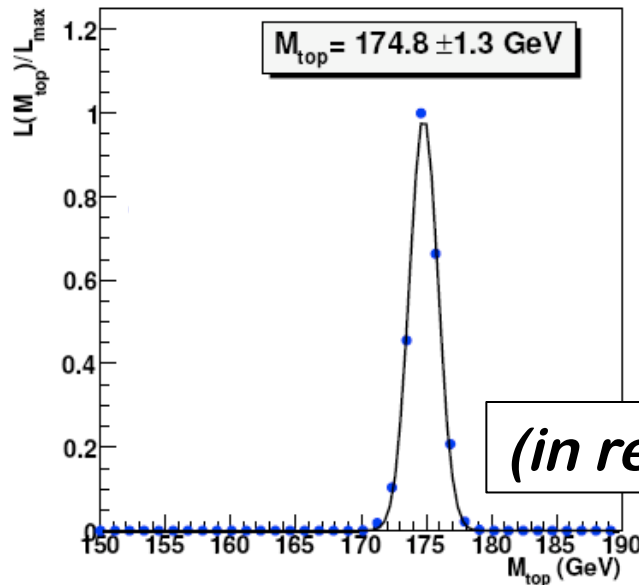
- The measurements shown today are based on:
  - Template method
  - Matrix Element method
- **Matrix Element** method:
  - Calculate p.d.f. on an event-by-event basis, pdf = pdf( $m_{\text{top}}$ ):

$$P_i(\vec{x}_i) = \frac{1}{N} \int \text{TF}(\vec{x}_i | \vec{y}_i) d\sigma(\vec{y}_i, m_t)$$

- **The clue:** calculate  $d\sigma$  with a LO matrix element:  $d\sigma \propto |\mathcal{M}|^2(\vec{m}_t)$
- Use Transfer Functions (TF) to map parton level quantities  $\vec{y}_i$  to reco level quantities  $\vec{x}_i$
- **Key advantage:**
  - We are calculating the probability for an event to be consistent with a tt decay for a given  $m_{\text{top}}$ 
    - 4-vectors with maximal topological information + correlations
  - This is the **maximally possible use of the event information**
    - → maximal statistical power

- **Matrix Element method, D0 (3.6 fb<sup>-1</sup>)**
- Extract  $m_{\text{top}}$  by maximising the likelihood for  $n$  events  $x_1 \dots$

$$\text{Likelihood} = \prod_{i=1}^n P_{\text{evt}}(x_i; m_{\text{top}}, JES, f_{\text{top}})$$



*(in reality, it's a 2D-fit:  $m_{\text{top}}$  vs JES)*

- Define the total probability for each event ( $f_{\text{top}}$  = sig. frac'n)

$$P_{\text{evt}}(x; m_{\text{top}}, JES, f_{\text{top}}) = f_{\text{top}} \cdot P_{\text{sig}}(x; m_{\text{top}}, JES) + (1 - f_{\text{top}}) \cdot P_{\text{bkg}}(x; JES)$$



# Top Mass in the Lepton+Jets Channel (I)



- The **Matrix Element** method in its full beauty:
  - The **signal probability** is the interesting bit!

$$P_{sig}(x; m_{top}, JES) = \frac{1}{\sigma_{obs}(p\bar{p} \rightarrow t\bar{t}; m_{top}, JES)} \times \sum_{perm} w_n \int_{q_1, q_2, y} \sum_{flavors} dq_1 dq_2 f(q_1) f(q_2) \frac{(2\pi)^4}{2q_1 q_2 s} \boxed{|\mathcal{M}(q\bar{q} \rightarrow t\bar{t} \rightarrow y)|^2} d\Phi_6 \boxed{W(x, y; JES)}$$

LO Matrix element

Transfer Function

Permutation weight, b-tag based

- (Background probability similar  
→ but ME for W+jets, no  $m_{top}$  dependence!)





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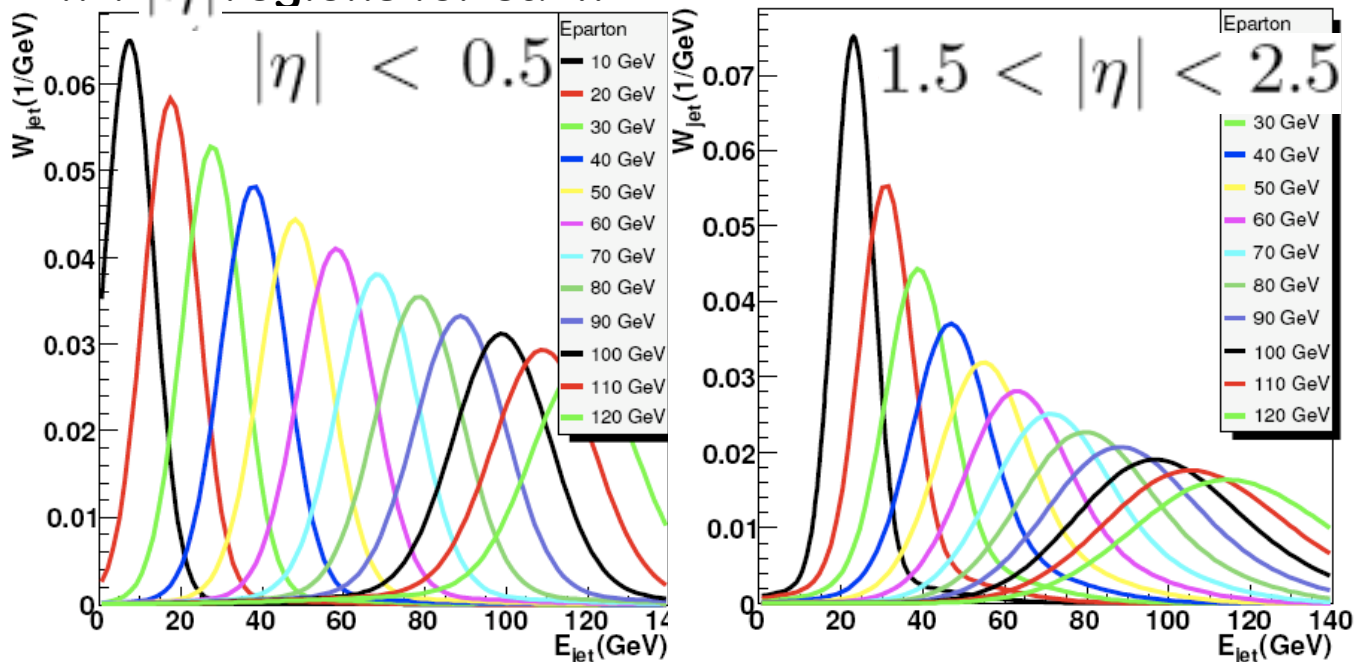
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Diagram annotations for the equation above:

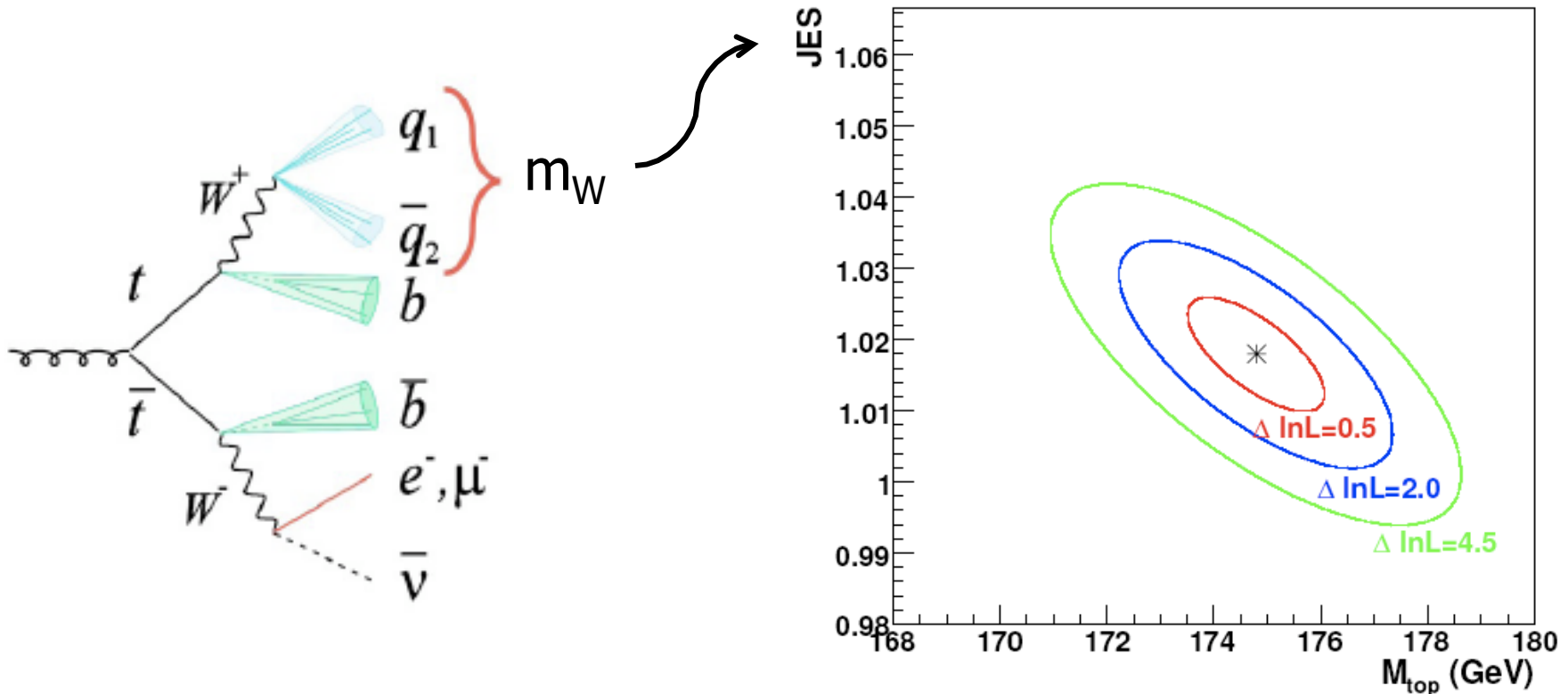
- Permutation weight, b-tag based (points to  $w_n$ )
- Bjoerken-x of incoming partons (points to  $q_1, q_2$ )
- pdfs (points to  $f(q_1) f(q_2)$ )
- Differential phase space (points to  $d\Phi_6$ )
- LO Matrix element (points to  $|\mathcal{M}(q\bar{q} \rightarrow t\bar{t} \rightarrow y)|^2$ )
- Transfer Function (points to  $W(x, y; JES)$ )

- (Background probability similar  
 → but ME for W+jets, no  $m_{top}$  dependence!)

- The **Transfer Functions**  $W(x, y; JES)$  relate parton-level quantities to reconstruction-level ones
  - By definition: normalised to unity
  - D0 uses a double-Gaussian to parametrise them
  - Treat separately:
    - Light / b-tagged jets with soft muon tag / other b-jets
    - x 4  $|\eta|$  regions for each



- Play **experimental trick**:
  - Largest experimental uncertainty is the **JES**
  - perform an **in-situ calibration of the JES**:
    - Constrain the two jets from W decay to  $m_W$
    - This allows a simultaneous extraction of  $m_{\text{top}}$  and JES!

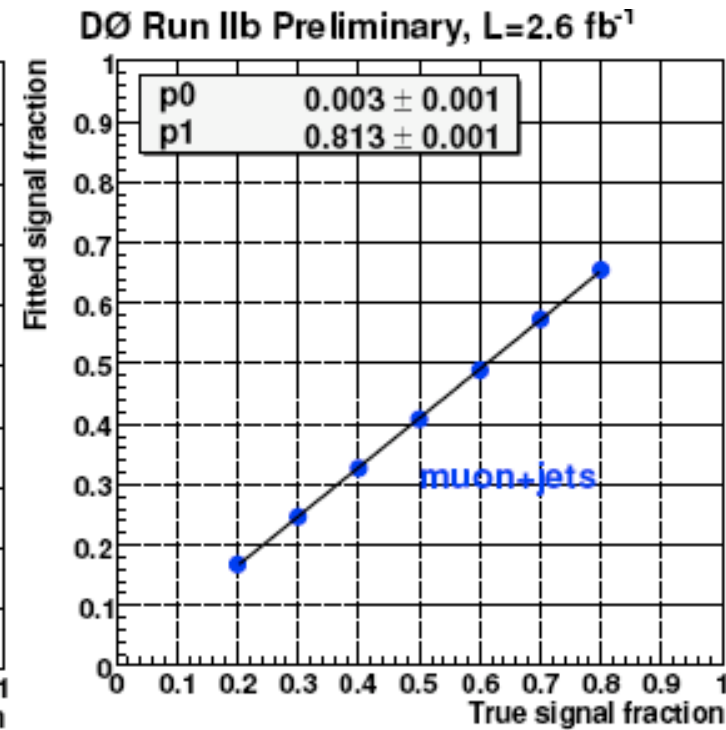
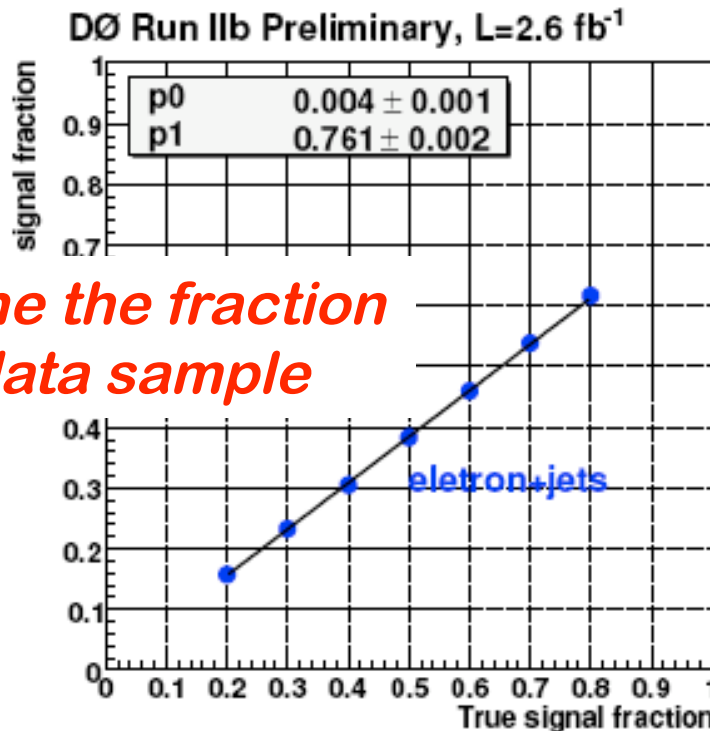




# Top Mass in the Lepton+Jets Channel (I)



- **Behold!** We need to calibrate the method:
  - Is the extracted **central value** not **biased**?
  - Is the **statistical uncertainty over/underestimated**?
- Study this using pseudo-experiments:
  - Draw ensembles of pseudo-experiments from MC



*Step 1: determine the fraction of signal  $f_{top}$  in data sample*

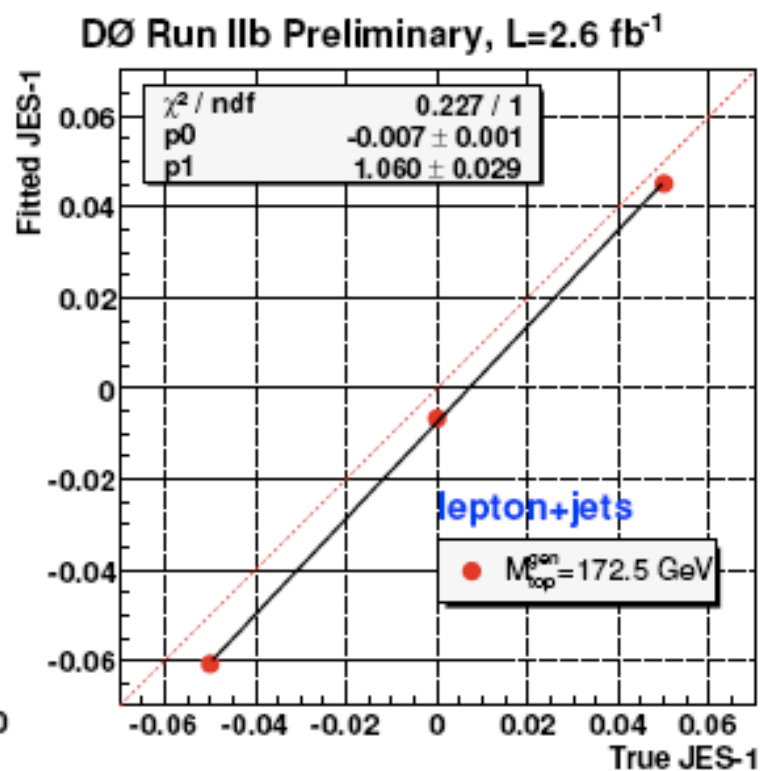
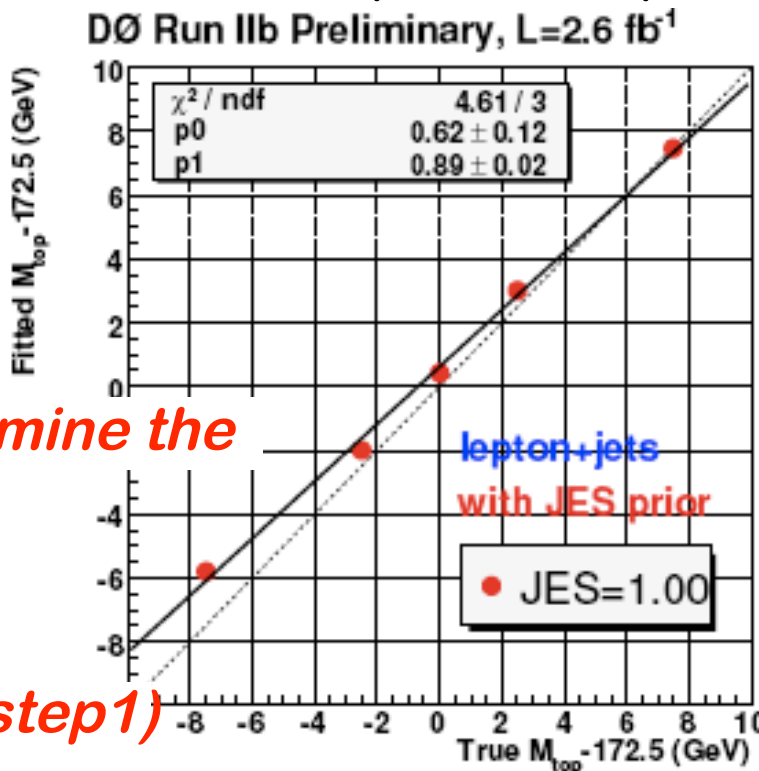




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*Step 2: determine the  $m_{\text{top}}$  and JES calibration + pull width (for  $f_{\text{top}}$  from step 1)*





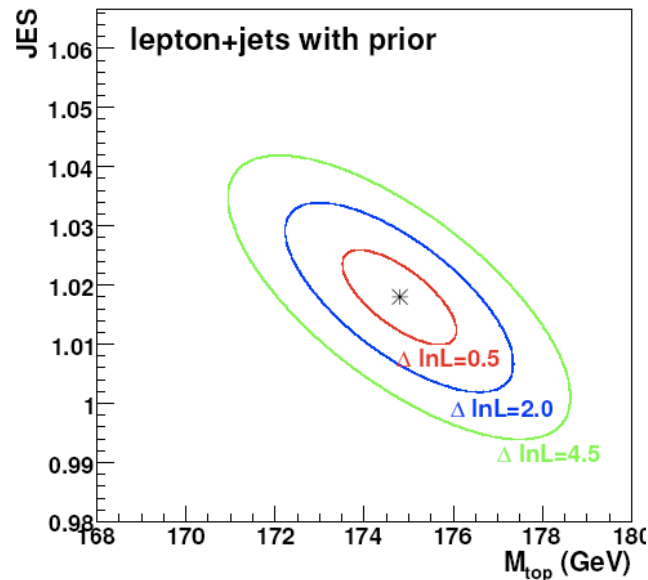
# Top Mass in the Lepton+Jets Channel (I)



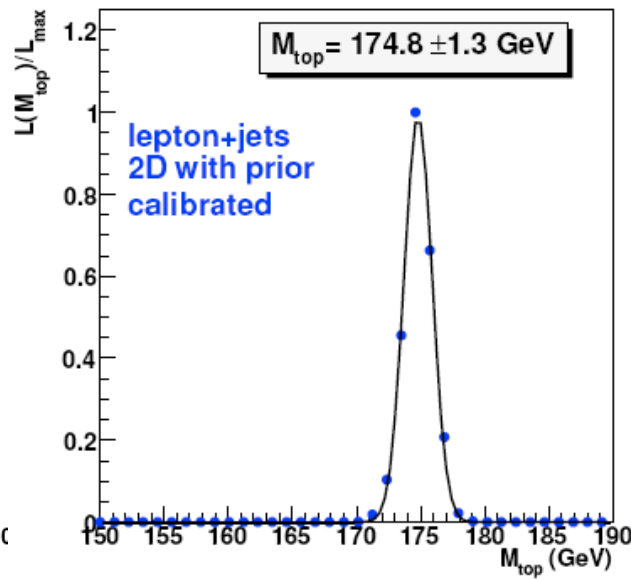
- Final result (**systematics dominated!**)
  - Combined ( $3.6 \text{ fb}^{-1}$ ):

$$m_{\text{top}} = 173.748 \pm 0.83(\text{stat}) \pm 1.62(\text{syst}) = 173.7 \pm 1.8 \text{ GeV}$$

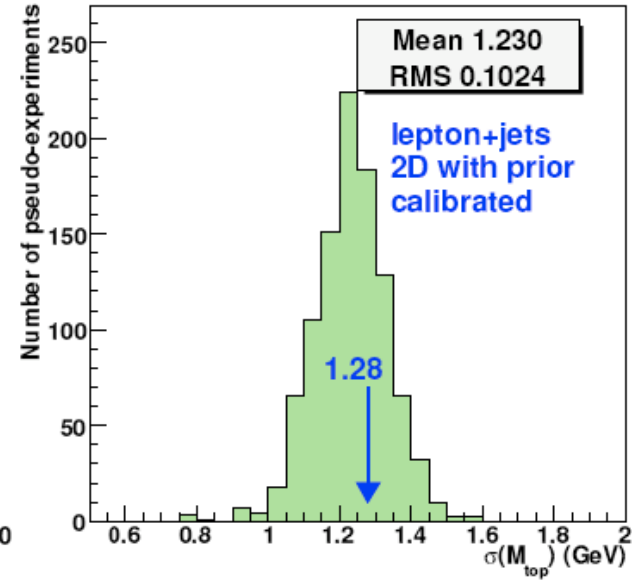
DØ Run IIb Preliminary,  $L=2.6 \text{ fb}^{-1}$



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# Top Mass in the Lepton+Jets Channel (I)



Systematics

Source	Run IIb (GeV)	Run IIa (GeV)
Higher Order Effects	$\pm 0.25$	$\pm 0.25$
ISR/FSR	$\pm 0.26$	$\pm 0.40$
Hadronization and UE	$\pm 0.58$	$\pm 0.58$
Color Reconnection	$\pm 0.40$	$\pm 0.40$
Multiple Hadron Interactions	$\pm 0.07$	$\pm 0.01$
Background Modeling	$\pm 0.03$	$\pm 0.04$
W HF factor	$\pm 0.07$	$\pm 0.09$
<i>b</i> -Modeling	$\pm 0.09$	$\pm 0.03$
PDF Uncertainty	$\pm 0.24$	$\pm 0.14$
Residual JES Uncertainty	$\pm 0.21$	$\pm 0.10$
Relative <i>b</i> /Light Response	$\pm 0.81$	$\pm 0.83$
Sample-Dependent JES	$\pm 0.56$	$\pm 0.56$
<i>b</i> -Tagging Efficiency	$\pm 0.08$	$\pm 0.15$
Trigger Efficiency	$\pm 0.01$	$\pm 0.19$
Lepton Momentum Scale	$\pm 0.17$	$\pm 0.17$
Jet Identification Efficiency	$\pm 0.26$	$\pm 0.26$
Jet Energy Resolution	$\pm 0.32$	$\pm 0.03$
QCD Background	$\pm 0.14$	$\pm 0.14$
Signal Fraction	$\pm 0.10$	$\pm 0.09$
Muon Resolution	-	$\pm 0.10$
Signal Contamination	-	$\pm 0.13$
MC Calibration	$\pm 0.20$	$\pm 0.26$
Total	$\pm 1.41$	$\pm 1.43$

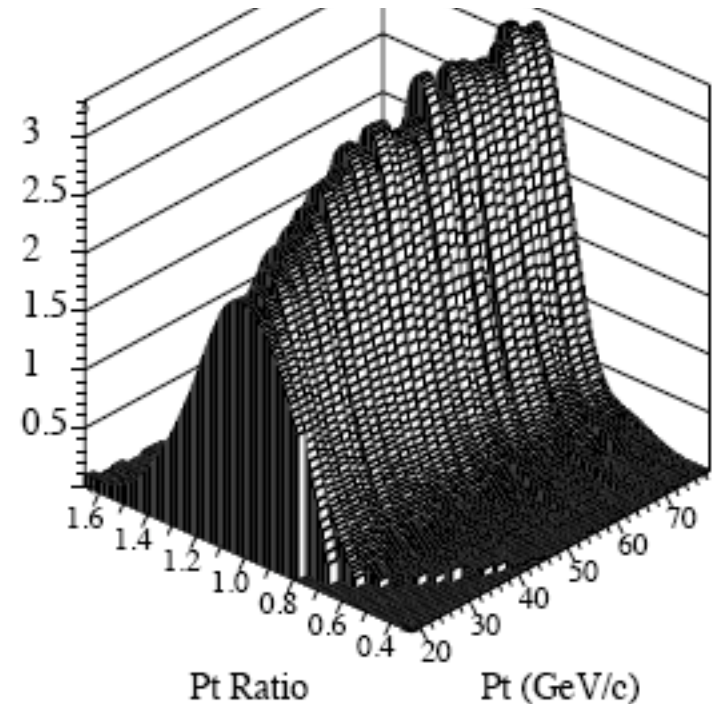
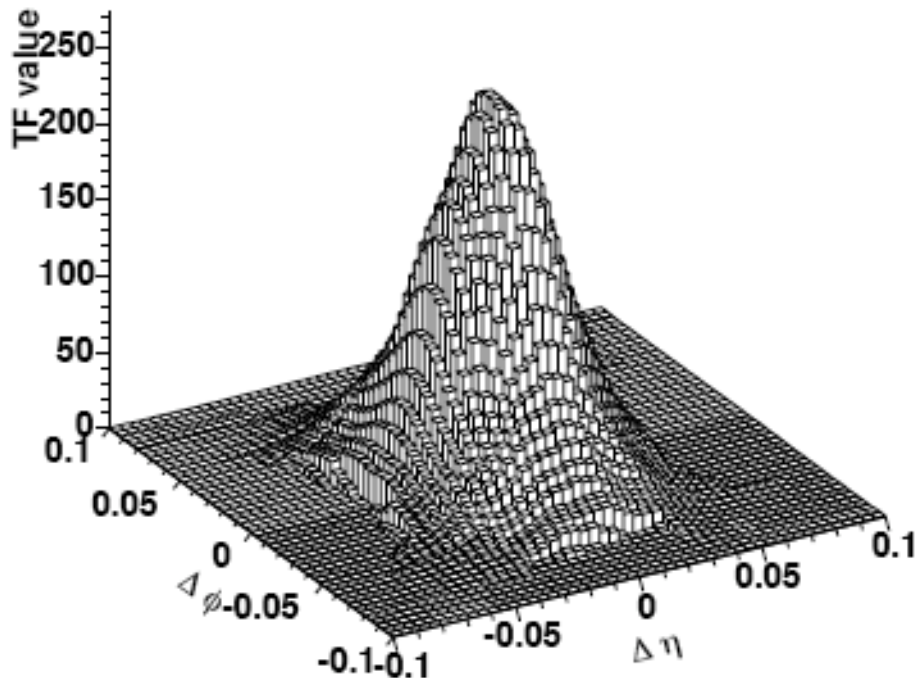
(will revisit later)



- **Matrix Element Method,  $4.8 \text{ fb}^{-1}$ , CDF**
  - Conceptually fairly similar to the D0 measurement
  - Focus only on the major differences in the following
- **More integration variables (“quasi-MC integration”):**
  - Not only energies, but also  $\eta \times \phi$  for jets (small effect)

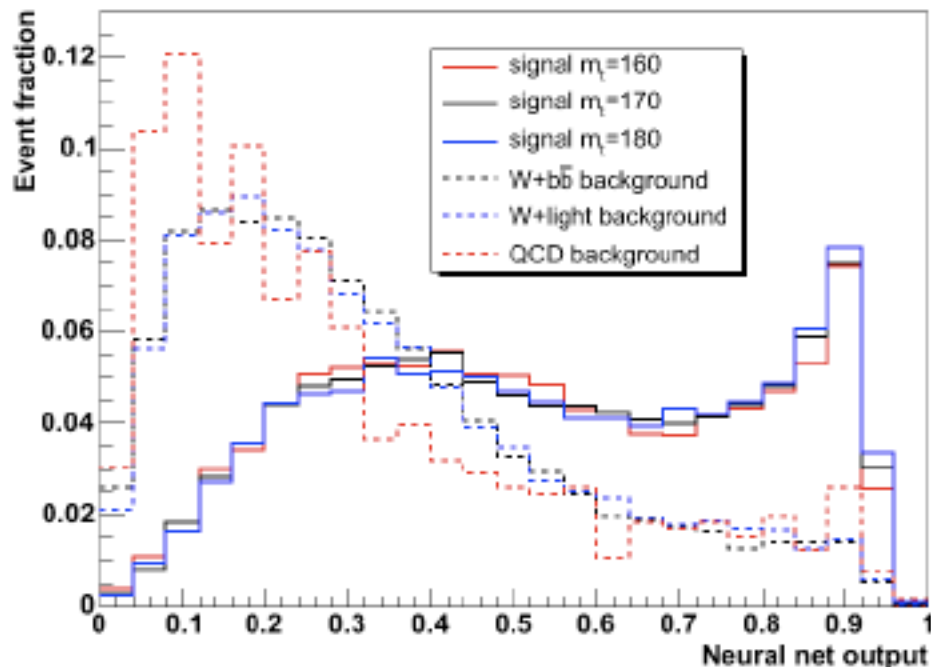
Light quark angular transfer function,  $\eta = 0$ ,  $m = 5$

- **TRFs are not fitted**





- Background fitting is done using a NN selection:



*Trained for  
 $m_{top}=170$  GeV and  $Wbb$*

*Careful check for any  
 $m_{top}$  dependence!*

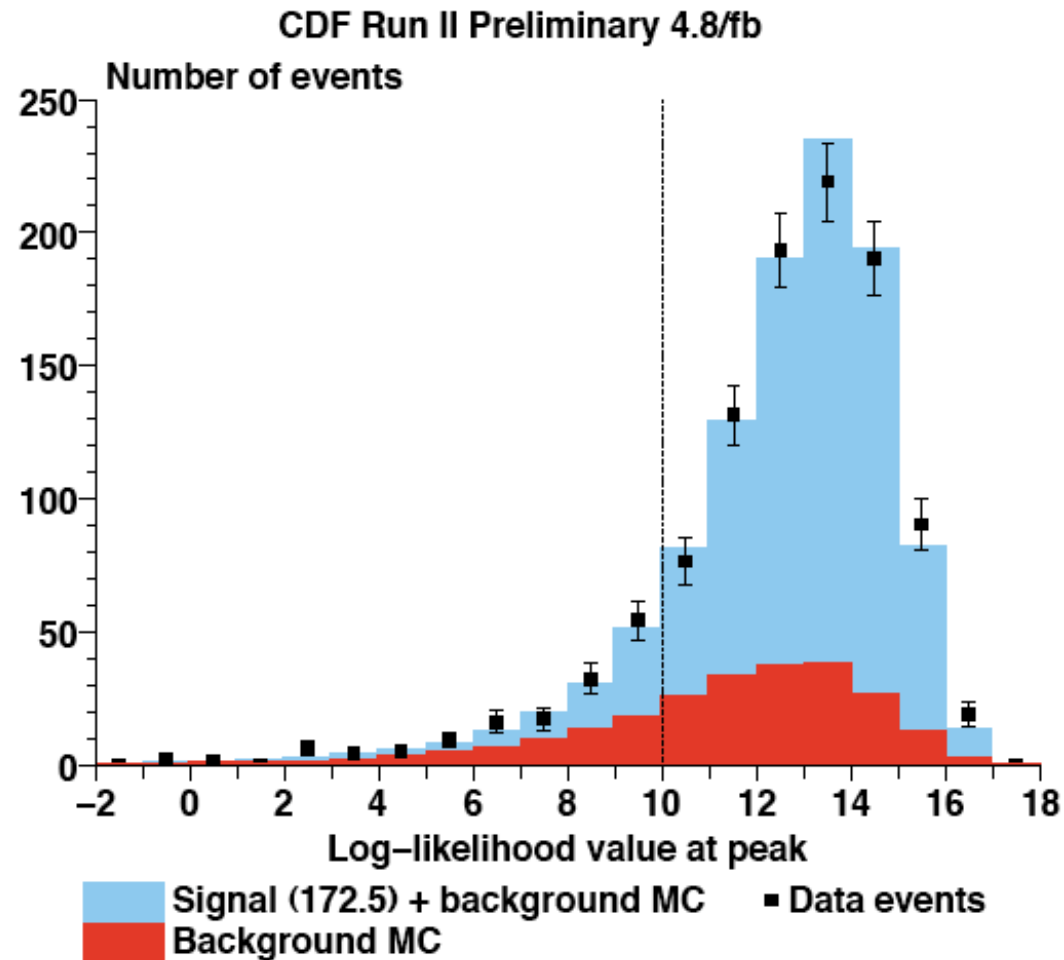
- Form total likelihood by subtracting average background likelihood scaled by  $f_{bkg}$  for the NN value of that event



# Top Mass in the Lepton+Jets Channel (II)



- For a notable fraction of signal events ( $\sim 30\%$ ):
  - One of the physics objects does not correspond to truth
  - **Remove those misreconstructed events:**
    - Require minimum LH value at peak
    - $\sim 80\%$  efficient
    - ( $\sim 96\%$  for good)
    - ( $\sim 70\%$  for bgr.)





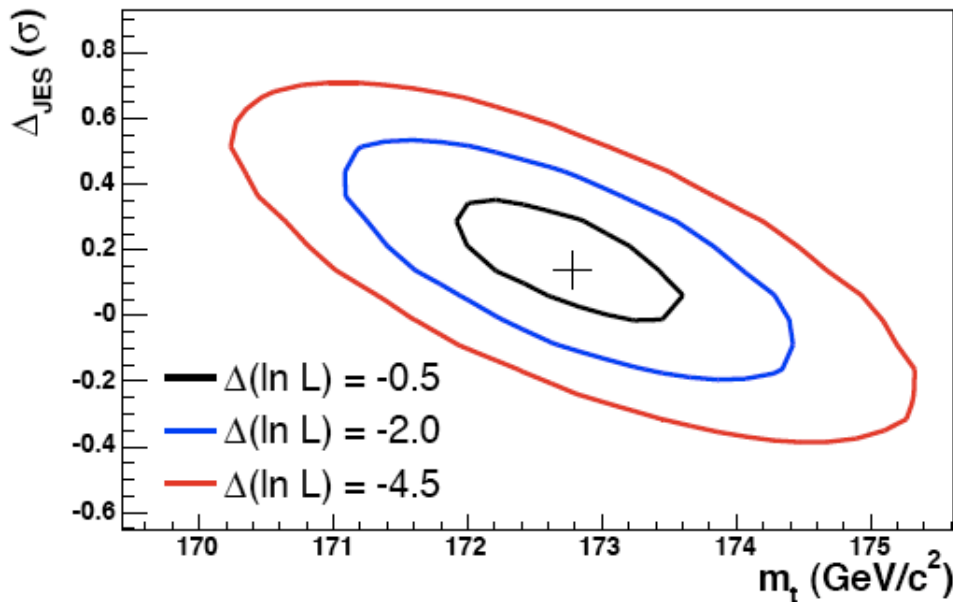
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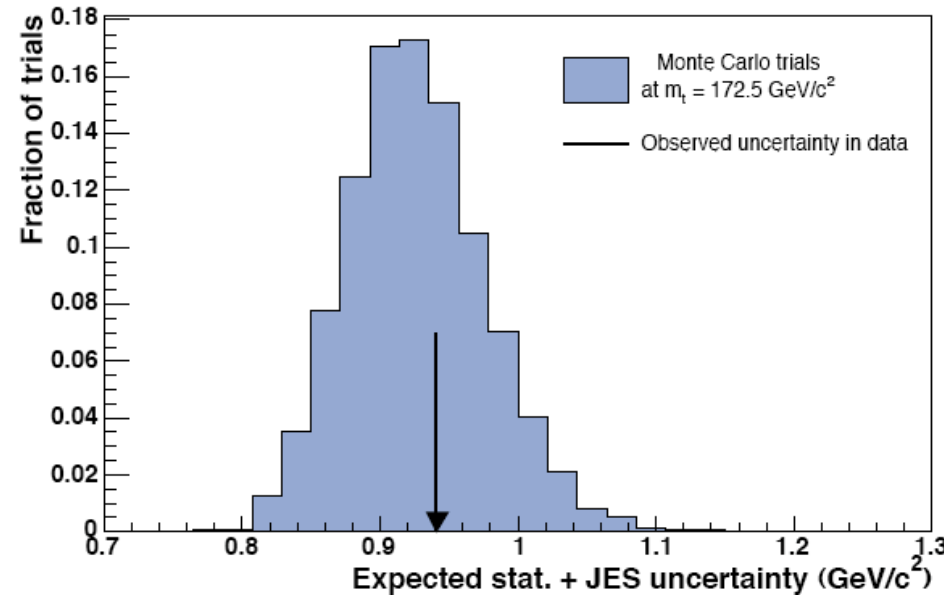
- CDF obtains:

$$m_t = 172.8 \pm 0.7 \text{ (stat.)} \pm 0.6 \text{ (JES)} \pm 0.8 \text{ (syst.) GeV}/c^2$$

CDF Run II Preliminary 4.8 fb<sup>-1</sup>



CDF Run II Preliminary 4.8 fb<sup>-1</sup>



- **World's most precise  $m_{\text{top}}$  measurement!**
- **Similar statistical uncertainty to the D0 measurement**





# Top Mass in the Lepton+Jets Channel (II)



Systematics

Systematic source	Systematic uncertainty ( $\text{GeV}/c^2$ )
Calibration	0.11
MC generator	0.25
ISR and FSR	0.15
Residual JES	0.49
<i>b</i> -JES	0.26
Lepton $P_T$	0.14
Multiple hadron interactions	0.10
PDFs	0.14
Background modeling	0.33
Gluon fraction	0.03
Color reconnection	0.37
Total	0.84

(will revisit later)





# Top Mass In the All-Hadronic Channel



- **Template method, CDF (2.9 fb<sup>-1</sup>):**
  - **Highly challenging due to immense QCD background!**
  - **Consider final states with  $6 \leq N_{\text{jets}} \leq 8$** 
    - **After multijet trigger req't:  $1.4 \times 10^7$  events, S:B ~ 1:1200**
    - **After offline preselection:  $1.7 \times 10^6$  events, S:B ~ 1:430**

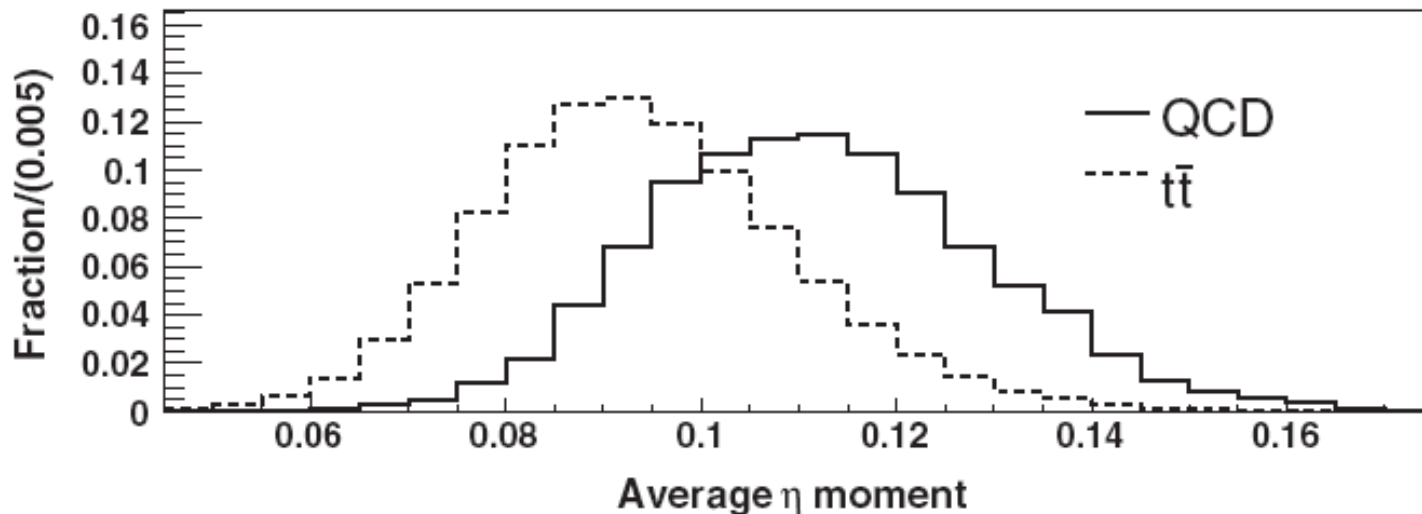




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  - Consider final states with  $6 \leq N_{\text{jets}} \leq 8$ 
    - After multijet trigger req't:  $1.4 \times 10^7$  events, S:B ~ 1:1200
    - After offline preselection:  $1.7 \times 10^6$  events, S:B ~ 1:430
  - Use multilayered NN (MLPFIT) with inputs:
    - “**traditional**” selection variables like  $\sum E_T, M_{3j}^{\min}, M_{3j}^{\max} \dots$
    - **specific variables**, e.g. 2<sup>nd</sup> moments of jets in  $\eta$  and  $\phi$ 
      - **Good discrimination between quark and gluon jets:**

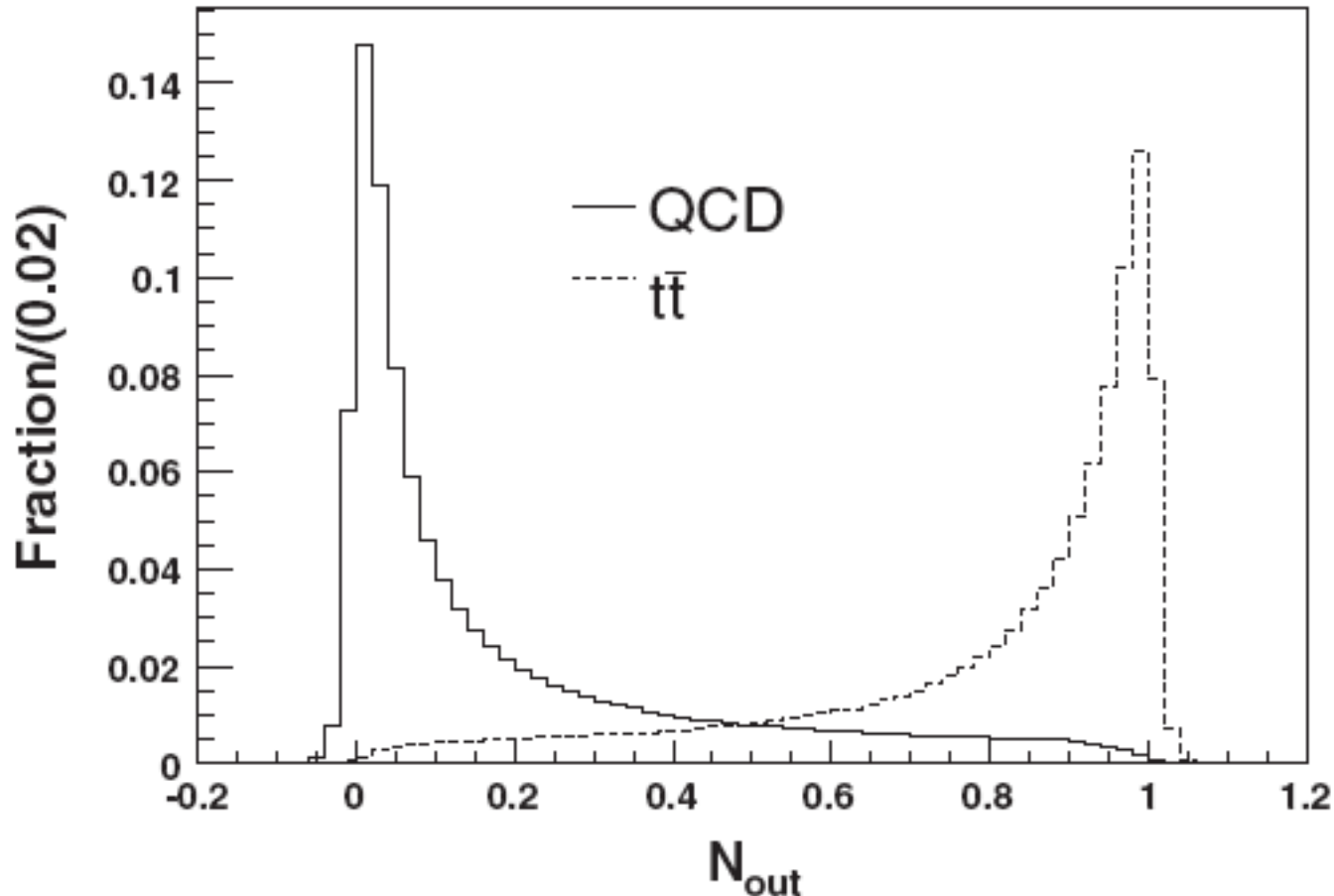




# Top Mass In the All-Hadronic Channel



- Powerful tool constructed:



- Define control region  $N_{out} < 0.25$ 
  - Derive corrections for tag rate (correl'ns for multiple tags)





# Top Mass In the All-Hadronic Channel



- Use **b-tagging** to refine **S:B** and improve **combinatorics**:
  - 30 jet-parton assignments with 1 b-tag
  - 6 assignments with 2 b-tags

- For each assignment minimise:

$$\chi^2 = \frac{(m_{jj}^{(1)} - M_W)^2}{\Gamma_W^2} + \frac{(m_{jj}^{(2)} - M_W)^2}{\Gamma_W^2} \left. \vphantom{\frac{(m_{jj}^{(1)} - M_W)^2}{\Gamma_W^2}} \right\} \text{Double } m_W \text{ constraint for JES}$$

$$+ \frac{(m_{jjb}^{(1)} - m_t^{\text{rec}})^2}{\Gamma_t^2} + \frac{(m_{jjb}^{(2)} - m_t^{\text{rec}})^2}{\Gamma_t^2} \left. \vphantom{\frac{(m_{jjb}^{(1)} - m_t^{\text{rec}})^2}{\Gamma_t^2}} \right\} \text{Constraint on } m_{\text{top}}$$

$$+ \sum_{i=1}^6 \frac{(p_{T,i}^{\text{fit}} - p_{T,i}^{\text{meas}})^2}{\sigma_i^2} \left. \vphantom{\sum_{i=1}^6} \right\} \text{Consistence of fitted 4-momenta with measured ones}$$

- Pick assignment with minimal  $\chi^2$
- Now we are able to reconstruct  $m_{\text{top}}$  and  $m_W$ !



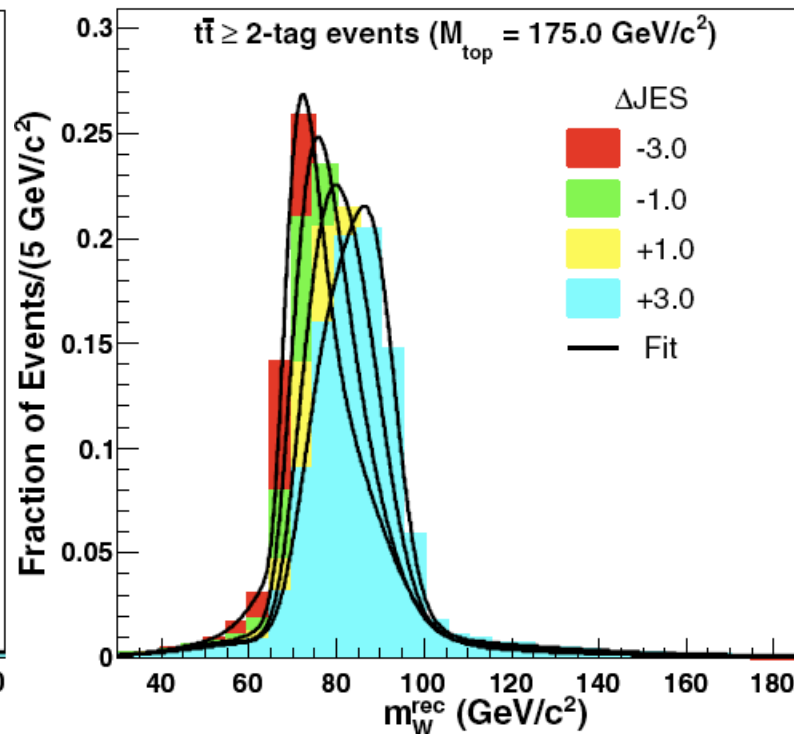
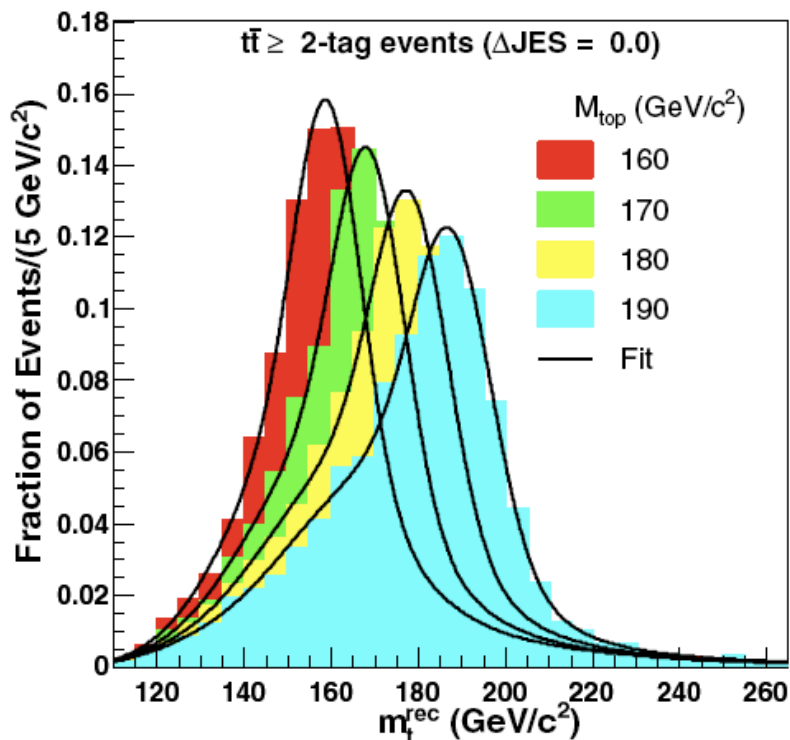




# Top Mass In the All-Hadronic Channel



- Select events for the measurement:
  - With  $N_{\text{out}} > 0.90$  and  $\chi^2 < 6$  for 1 b-tag (S:B ~ 1:4)
  - With  $N_{\text{out}} > 0.88$  and  $\chi^2 < 5$  for 2+ b-tags (S:B ~ 1:1)
- Maximise binned likelihood for (+ tons of crosschecks):
  - $m_{\text{top}}$ ,  $m_W$ ,  $n_{\text{signal}}$  events,  $n_{\text{background}}$  events (+ Xsec meas't)



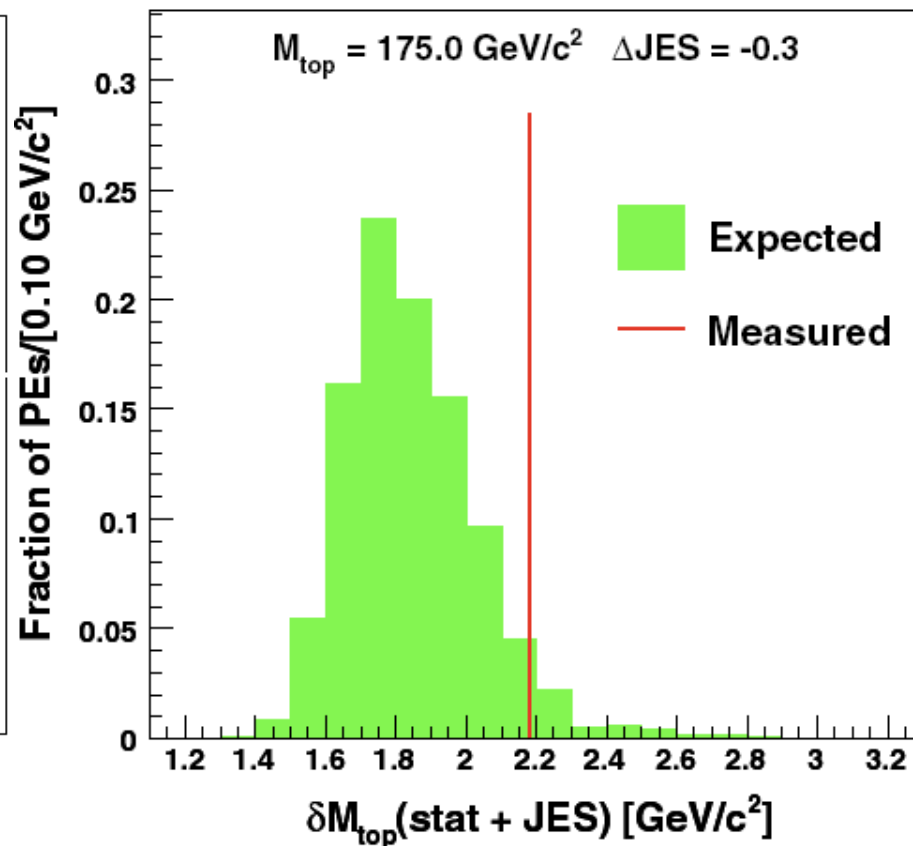
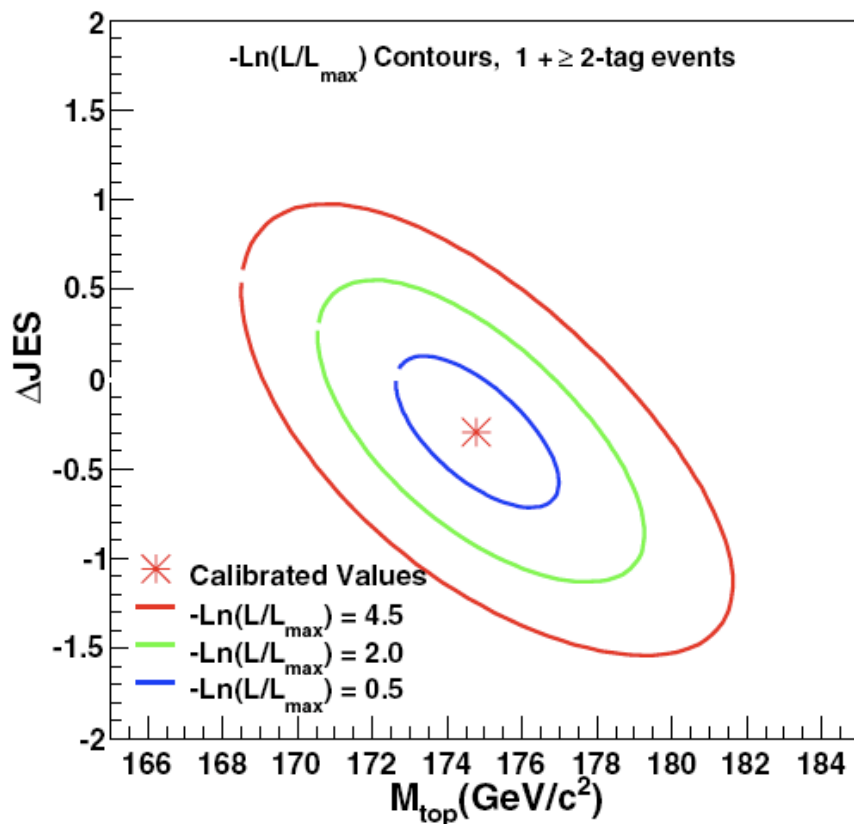


# Top Mass In the All-Hadronic Channel



- After calibration with ensemble testing techniques:

$$M_{\text{top}} = 174.8 \pm 1.7(\text{stat}) \pm 1.6(\text{JES}) \pm_{-1.0}^{+1.2}(\text{syst}) \text{ GeV}/c^2$$



- Strongest contribution to world average after l+jets!

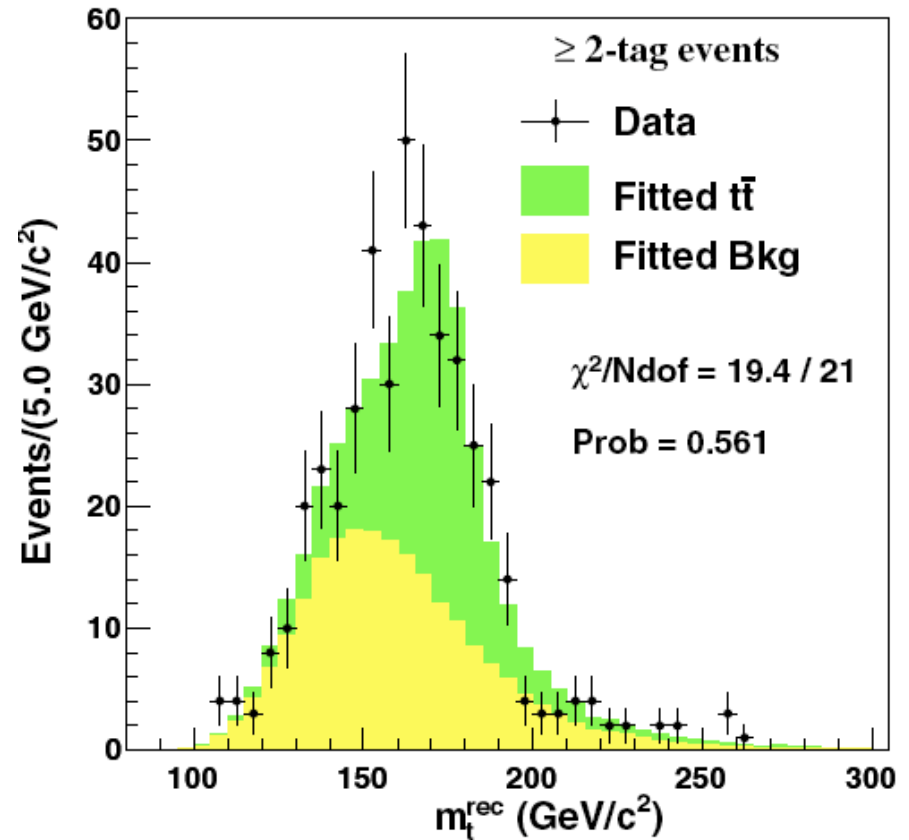
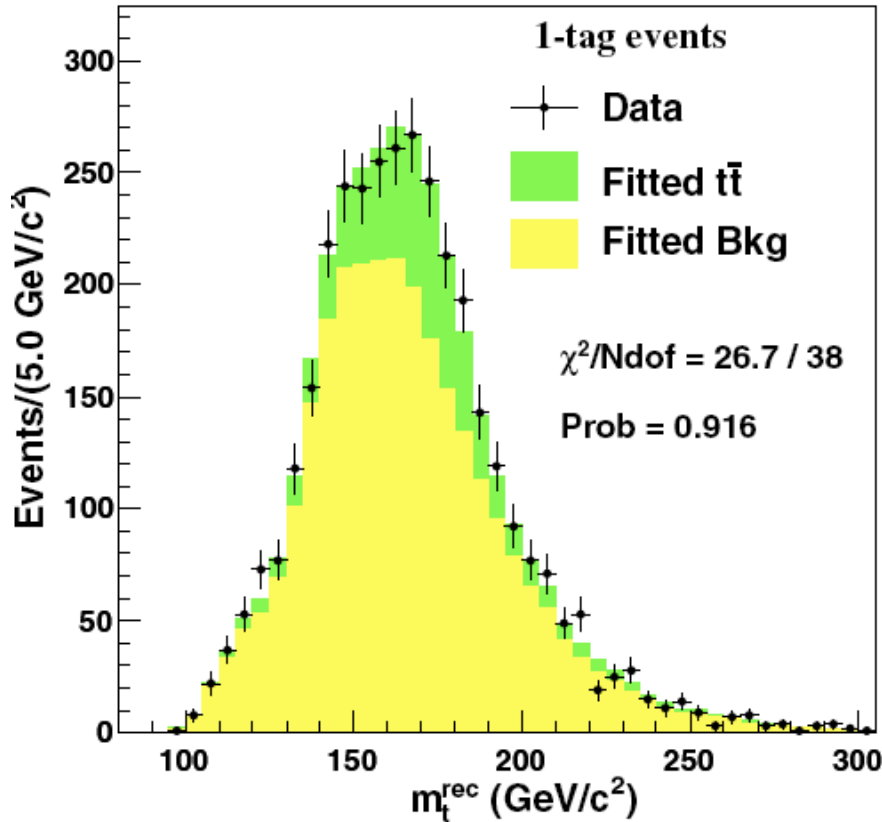




# Top Mass In the All-Hadronic Channel



- Overall crosscheck looks good:



- Extract top cross section of:

$$\sigma_{t\bar{t}} = 7.2 \pm 0.5(\text{stat}) \pm 0.4(\text{lum}) \text{ pb}$$

- (For  $M_{\text{top}} = 175 \text{ GeV}/c^2$   $\Delta\text{JES} = -0.3$ )





# Top Mass In the All-Hadronic Channel



Systematics

Source	$\delta M_{\text{top}}^{\text{syst}}$ (GeV/ $c^2$ )	$\delta \Delta \text{JES}^{\text{syst}}$
Residual bias	+0.8 -0.4	+0.18 -0.24
2D calibration	<0.1	<0.01
Generator	0.3	0.25
ISR/FSR	0.1	0.06
<i>b</i> -jet energy scale	0.2	0.04
<i>b</i> -tag SF $E_T$ dependence	0.1	0.01
Residual JES	0.5	...
PDF	+0.3 -0.2	+0.05 -0.04
Multiple $p\bar{p}$ interactions	0.2	0.01
Color reconnection	0.4	0.08
Statistics of templates	0.3	0.07
Background shape	0.1	0.02
Total	+1.2 -1.0	+0.34 -0.37





# Top Mass in the Dilepton Channel



- **Matrix Element method, D0 (3.6 fb<sup>-1</sup>)**
  - Similar approach to l+jets channel
  - However, the kinematics is not overconstrained
  - Cannot fit for JES simultaneously
  - D0 obtains (ll for Run IIa, emu for Run IIb):

$$m_{\text{top}}^{\ell\ell} = 174.7 \pm 2.9 \text{ (stat.)} \pm 2.4 \text{ (sys.) GeV}$$

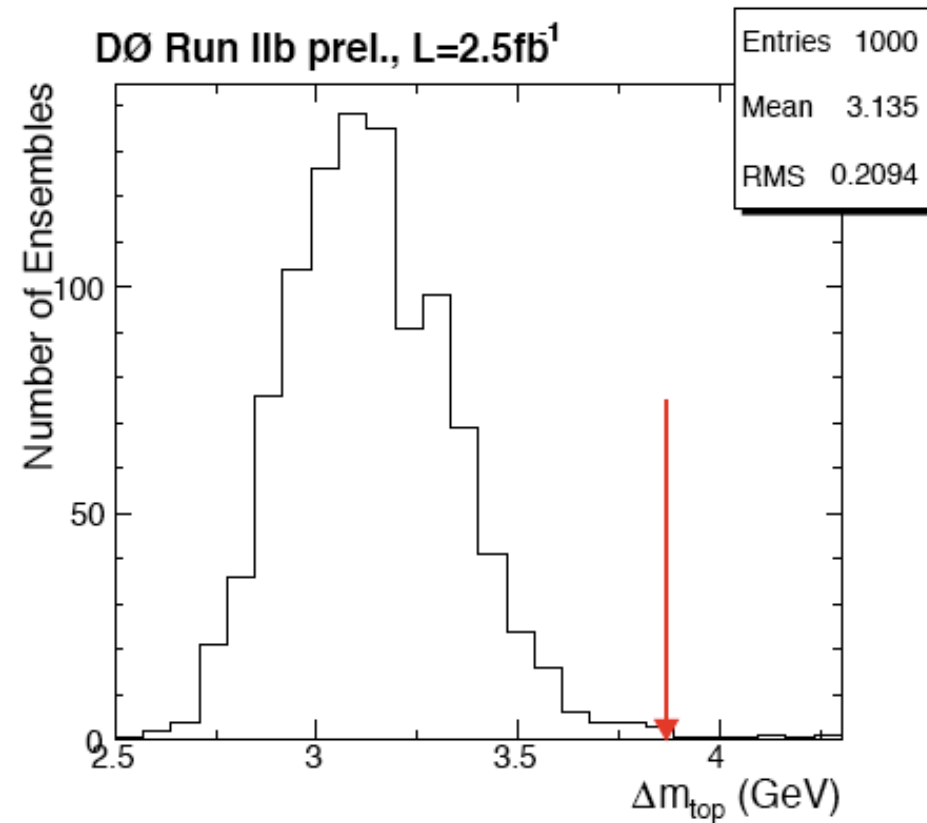
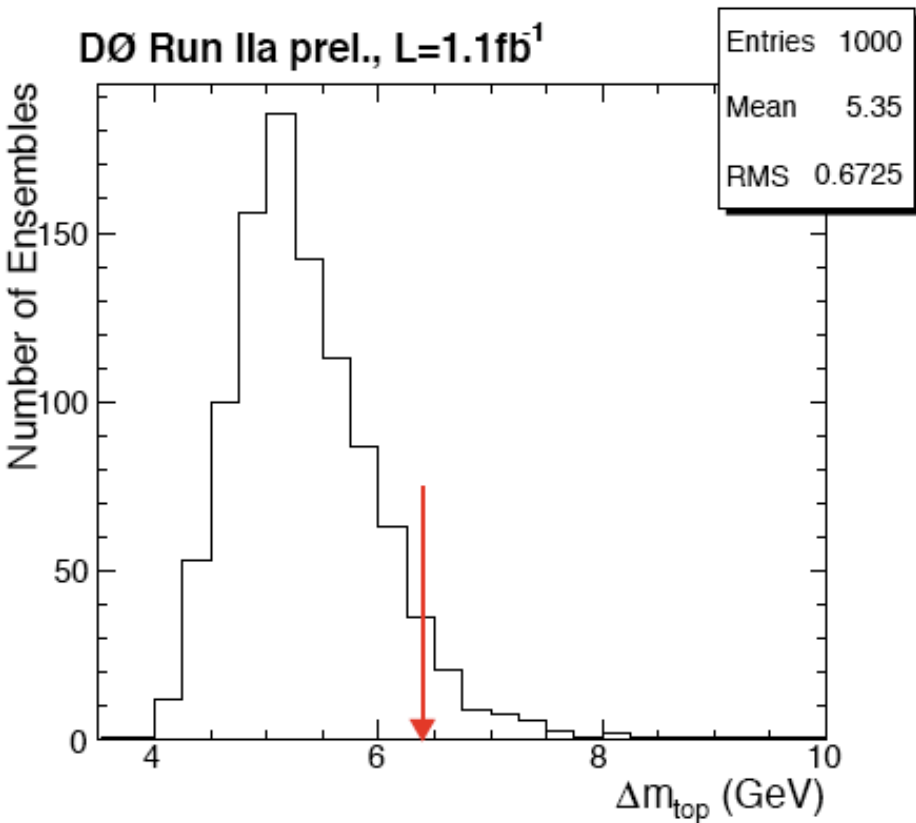




# Top Mass in the Dilepton Channel



- D0 was rather unlucky with its data:





# Tevatron Top Mass Combination



- Lepton + jets mass measurements dominate world average

Parameter	Value (GeV/c <sup>2</sup> )	Correlations
$M_t^{\text{all-j}}$	$175.1 \pm 2.6$	1.00
$M_t^{\text{l+j}}$	$172.7 \pm 1.3$	0.20 1.00
$M_t^{\text{di-l}}$	$171.4 \pm 2.7$	0.19 0.50 1.00

- Results are consistent

- $(\chi^2 \text{ probability} = 76\%)$

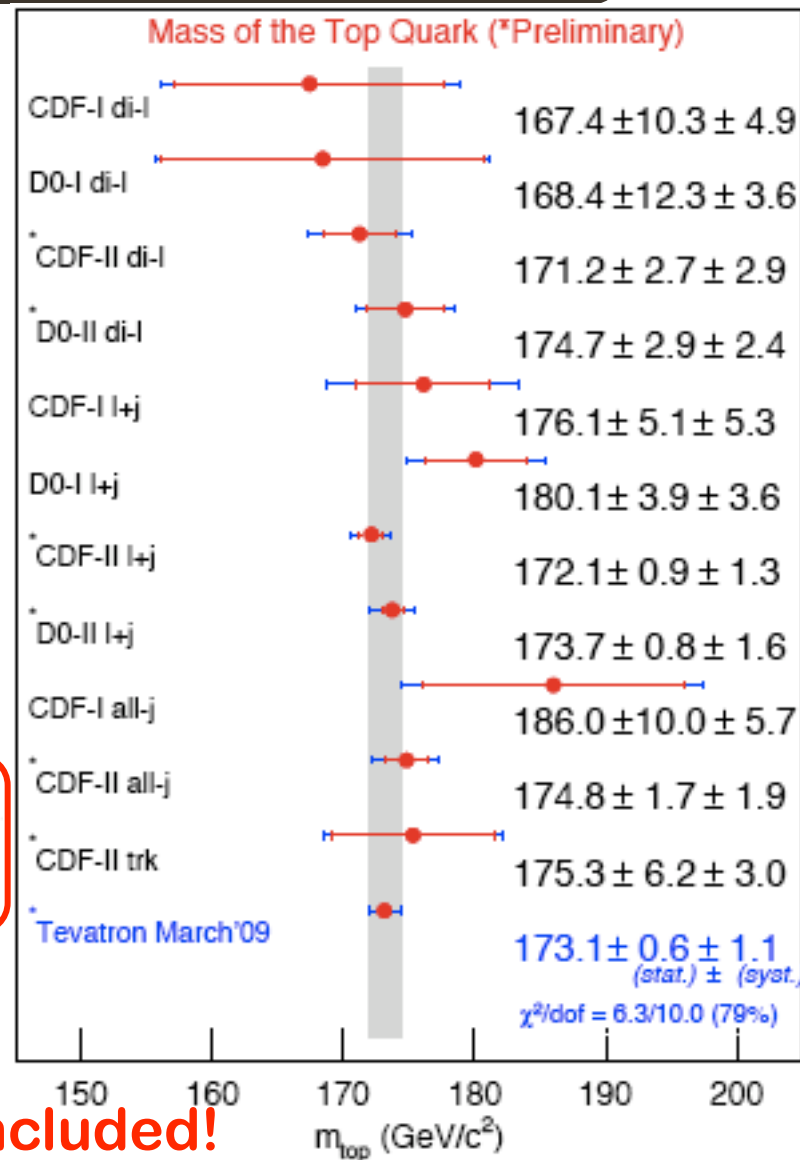
- World average:

$$M_t = 173.1 \pm 0.6 \text{ (stat.)} \pm 1.1 \text{ (syst.) GeV/c}^2$$

$$M_t = 173.1 \pm 1.3 \text{ GeV/c}^2$$

- Top mass known to 0.75% prec'n
- Approaching 1 GeV!

- World's most precise meas't NOT included!

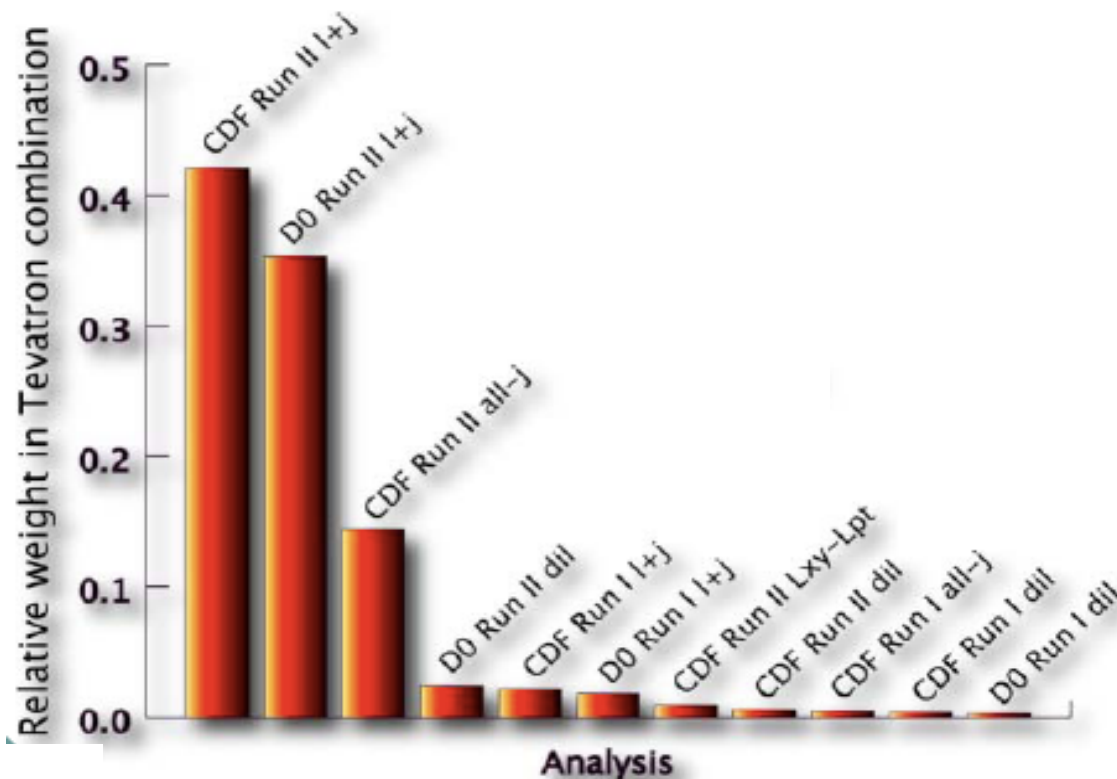




# Tevatron Top Mass Combination



	Run I published					Run II preliminary					
	CDF			DØ		CDF				DØ	
	l+j	di-l	all-j	l+j	di-l	l+j	di-l	all-j	trk	l+j	di-l
Pull	+0.4	-0.5	+1.1	+1.4	-0.4	-0.9	-0.5	+0.7	+0.3	0.5	+0.4
Weight [%]	-2.4	-0.5	-0.6	+2.0	+0.3	+47.4	+0.7	+16.2	-0.1	+39.8	-2.7







# Top Quark Mass Systematics



*Discuss most significant systematic uncertainties for ME analyses in  $l+jets$  in the following...*

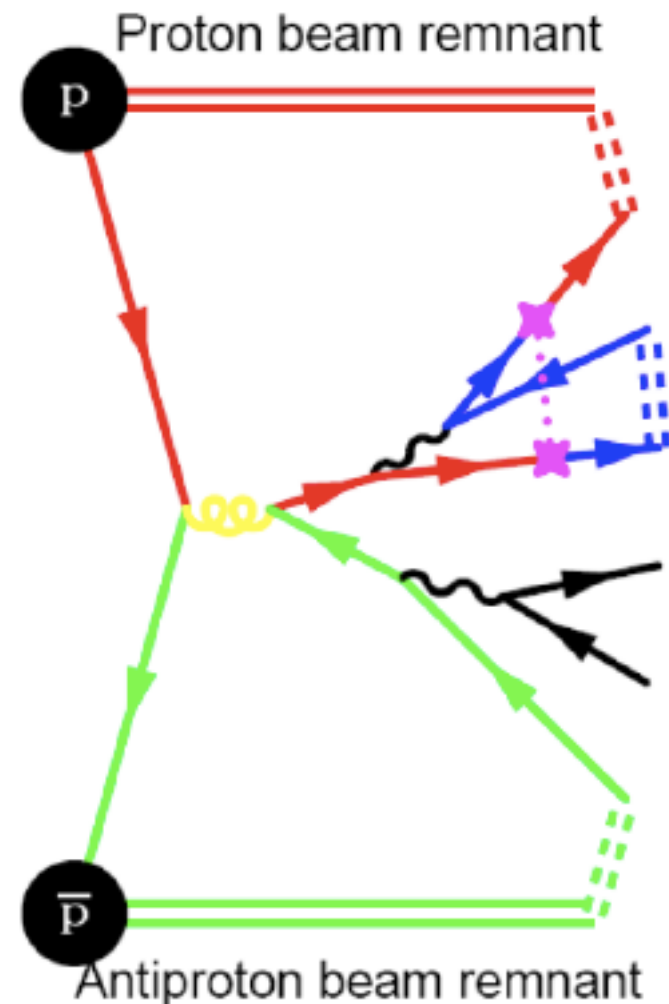
Source	Run IIb (GeV)	Run IIa (GeV)
Higher Order Effects	$\pm 0.25$	$\pm 0.25$
ISR/FSR	$\pm 0.26$	$\pm 0.40$
Hadronization and UE	$\pm 0.58$	$\pm 0.58$
Color Reconnection	$\pm 0.40$	$\pm 0.40$
Multiple Hadron Interactions	$\pm 0.07$	$\pm 0.01$
Background Modeling	$\pm 0.03$	$\pm 0.04$
W HF factor	$\pm 0.07$	$\pm 0.09$
$b$ -Modeling	$\pm 0.09$	$\pm 0.03$
PDF Uncertainty	$\pm 0.24$	$\pm 0.14$
Residual JES Uncertainty	$\pm 0.21$	$\pm 0.10$
Relative $b$ /Light Response	$\pm 0.81$	$\pm 0.83$
Sample-Dependent JES	$\pm 0.56$	$\pm 0.56$
$b$ -Tagging Efficiency	$\pm 0.08$	$\pm 0.11$
Trigger Efficiency	$\pm 0.01$	$\pm 0.11$
Lepton Momentum Scale	$\pm 0.17$	$\pm 0.11$
Jet Identification Efficiency	$\pm 0.26$	$\pm 0.20$
Jet Energy Resolution	$\pm 0.32$	$\pm 0.01$
QCD Background	$\pm 0.14$	$\pm 0.14$
Signal Fraction	$\pm 0.10$	$\pm 0.01$
Muon Resolution	-	$\pm 0.10$
Signal Contamination	-	$\pm 0.11$
MC Calibration	$\pm 0.20$	$\pm 0.20$
Total	$\pm 1.41$	$\pm 1.41$

Systematic source	Systematic uncertainty (GeV/ $c^2$ )
Calibration	0.11
MC generator	0.25
ISR and FSR	0.15
Residual JES	0.49
$b$ -JES	0.26
Lepton $P_T$	0.14
Multiple hadron interactions	0.10
PDFs	0.14
Background modeling	0.33
Gluon fraction	0.03
Color reconnection	0.37
Total	0.84



- **Colour reconnection is a recent addition**

- See paper by P. Skands and D. Wicke [arXiv:0807.3248]
- Hadronisation regions of jets from  $W$  and  $b$  decay can overlap:
  - Possible effect on  $m_{\text{top}}$  due to colour reconnection
- Evaluate by comparing signal with colour reconnection on/off
- Systematic about 0.4 GeV
  - Both D0 and CDF





## Systematics: ISR / FSR



- **Initial and final state radiation** (ISR/FSR) may bias the top mass measurement
  - It is partly the source for “misreconstructed” events
- **ISR** and **FSR** can be **separated** in **Drell-Yan** processes
- CDF did a study to determine the amount of ISR / FSR (CDF note 6804)
  - Derived Pythia tunes with amount of ISR is central +/-  $\Delta$
  - Evaluate systematics as the difference of  $m_{\text{top}}$  for those
  - Both D0 and CDF obtain a systematic of a similar magnitude
    - Likely to be larger at the LHC





# Systematics: Hadronisation and UE



- Pythia and Herwig have different models for
  - Hadronisation
  - Underlying Event (UE)
- In general: rerun MC with Pythia and Herwig showering
- **D0:**
  - “Hadronisation and UE”:
    - Compare alpgen signal samples
      - Hadronised with Pythia
      - Hadronised with Herwig
- **CDF:**
  - “MC Generator”:
    - Compare:
      - Pythia signal samples hadronised with Pythia
      - Herwig signal samples hadronised with Herwig





# Systematics: Residual JES



- Besides the global JES factor (which is fitted) there could remain a JES dependence **differential in  $\eta \times \phi$** 
  - The JES corrections are parametrised in  $\eta \times \phi$
  - Scale the individual jet energies by the uncertainty  $\sqrt{\text{data}^2 + \text{MC}^2}(\eta, \phi)$  on the JES parametrisation
  - Preserve overall correction magnitude
    - Only differential changes “simulated”
- **D0:**
  - “Residual JES Uncertainty”
- **CDF:**
  - “Residual JES”



- The **JES** of **light quark jets** and **heavy flavour jets** does not need to be the same
    - For b-jets the response may be different:
      - higher mass → out of cone corrections different?
      - Shower particle composition different
      - escaping neutrinos
  - **D0:**
    - “Relative b/light response”
  - **CDF:**
    - “bJES”
- *N.B.: in CDF’s bJES also the b-jet fragmentation is included (in the table on slide 38)*

- The JES does not need to be the same for **jets** from **light quarks** and **gluons**
  - JES corr's derived in a sample dominated by quark jets
  - In signal MC: predominantly quark jets
  - In W+jets background: predominantly gluon jets
  - Systematic: evaluate  $m_{\text{top}}$  with background sample JES shifted or not
- Currently, only D0 evaluates this systematic (AFAIK)
  - Magnitude: 0.56 GeV
  - However, we have indications that the current evaluation scheme is somewhat pessimistic
  - Stay tuned...



# Summary

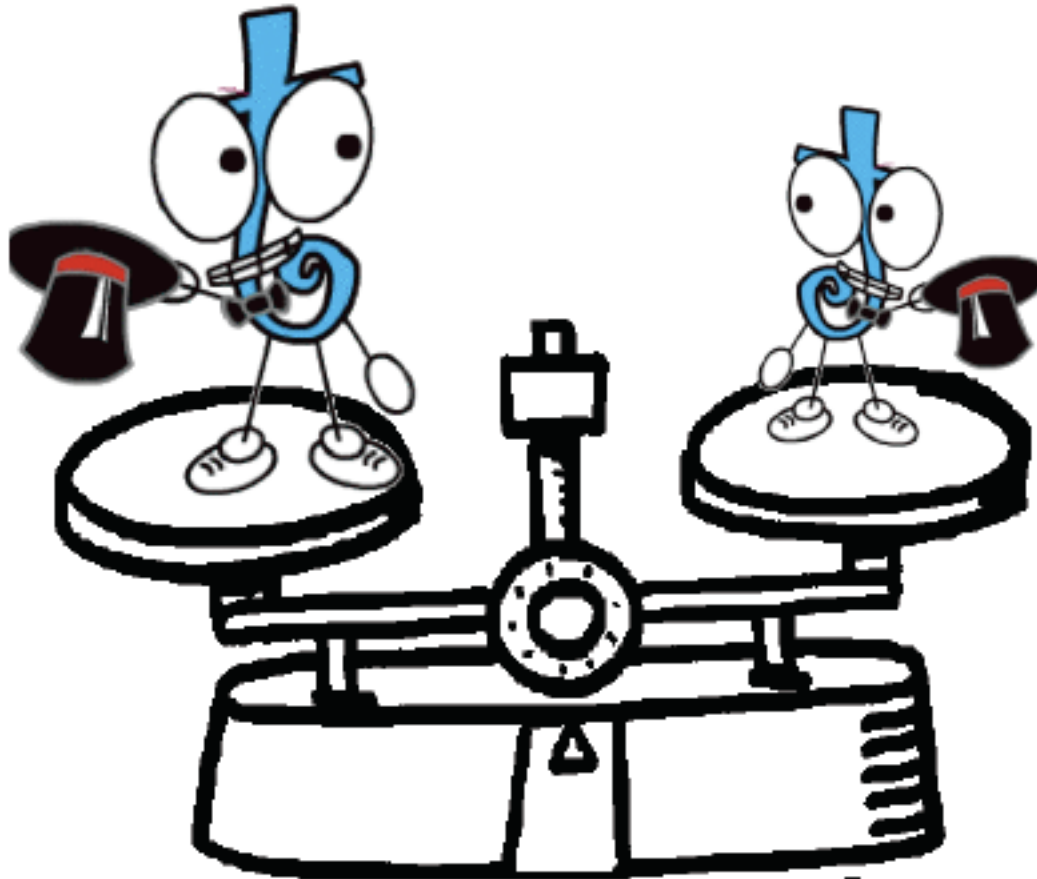


- The **top quark mass** is a very **intriguing SM parameter!**
- The **Tevatron** and its experiments are in a **great shape**
- We keep **refining** the precision of our **top quark mass measurements!**
  - Most **precise** measurements with the **Matrix Element** method in the **l+jets channel**
  - Followed by the **all-hadronic** channel + the **Template Method**
  - Notable contribution from the **dilepton** channel
  - Interesting alternative methods on the market (*not shown*)
- Our measurements are **systematically limited** since years
  - Lots of work went into the understanding the systematics
  - And **unifying** their **treatment across experiments!**





We are looking ahead to more exciting measurements from the Tevatron!



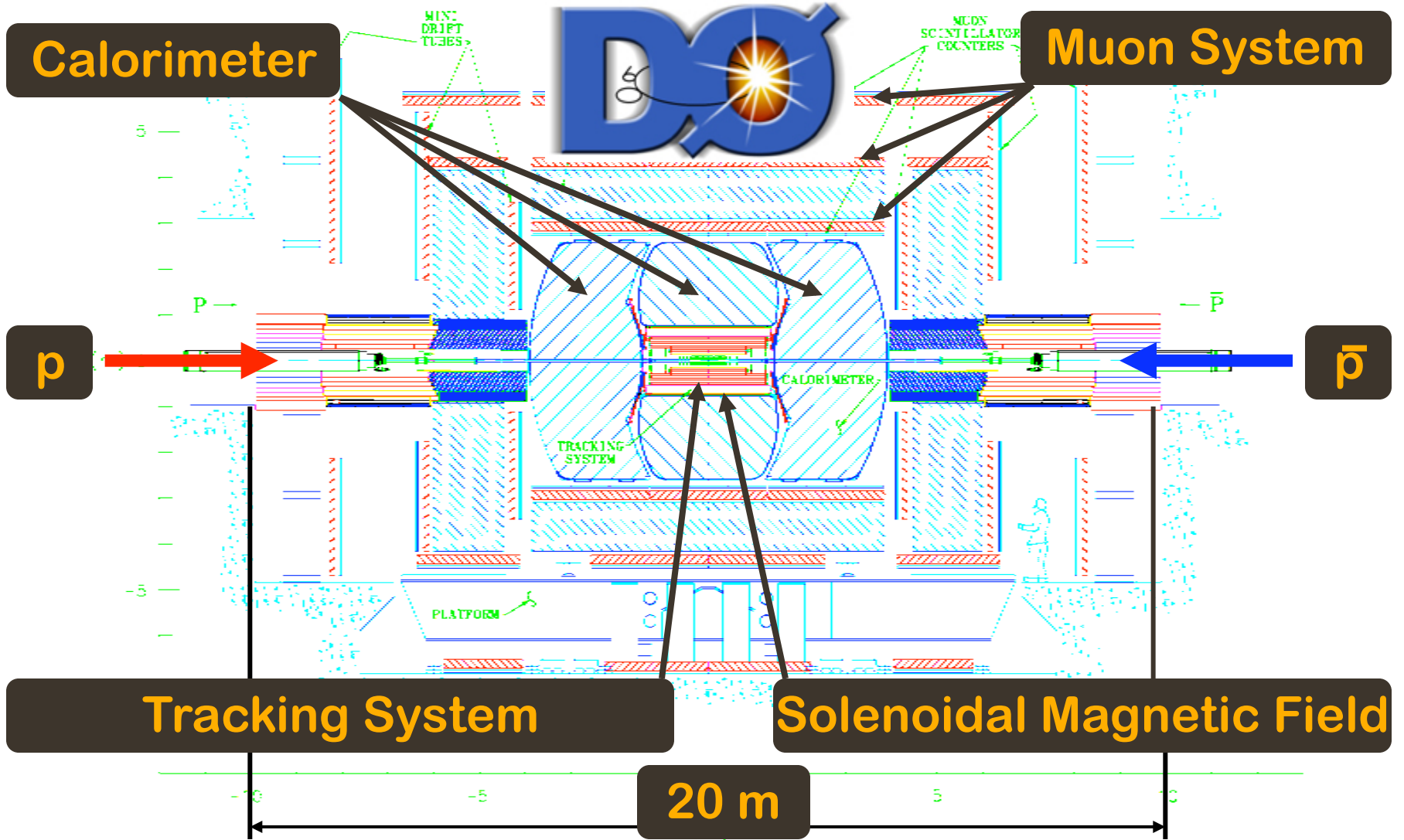
# Bonus slides

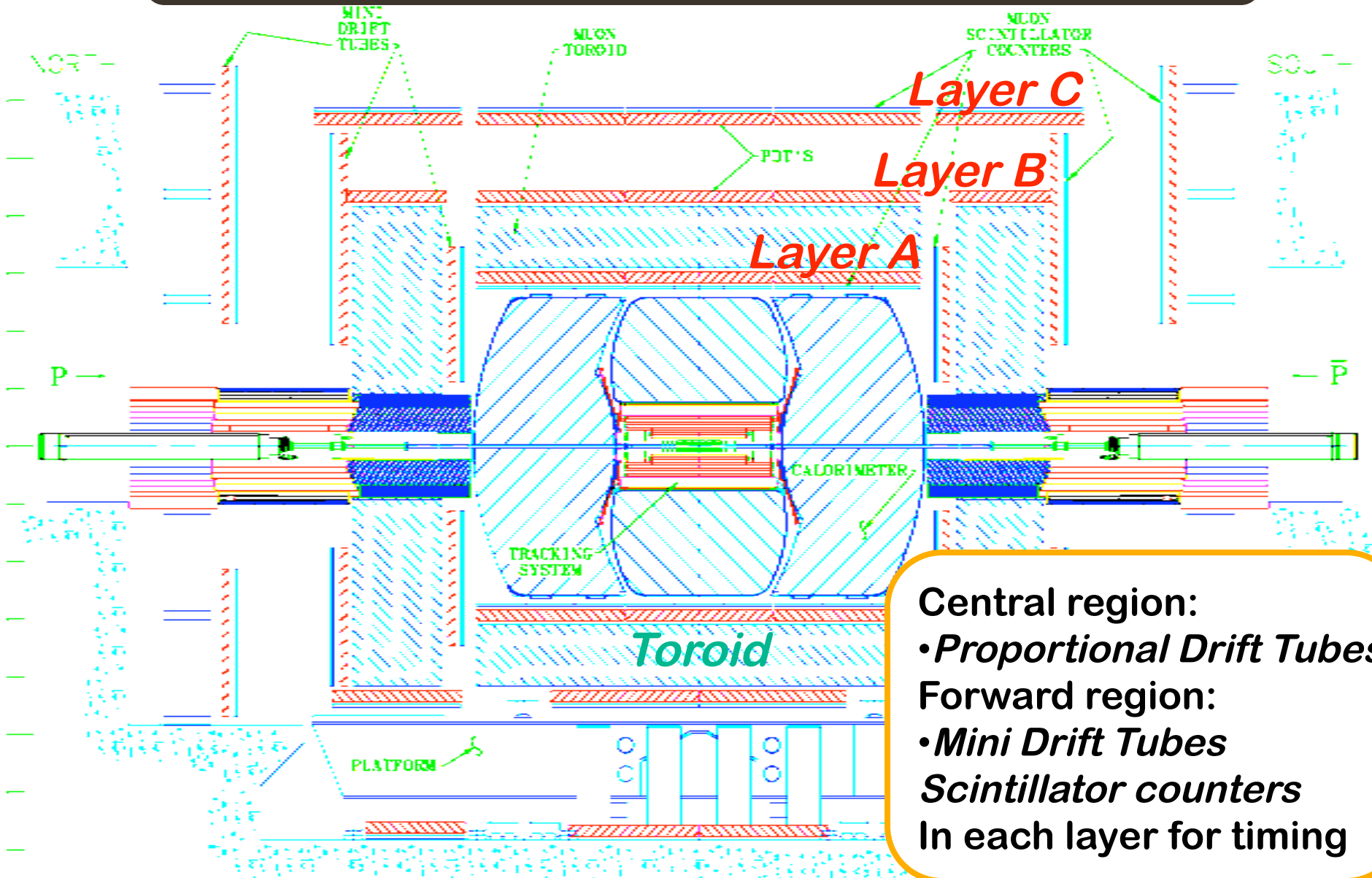


GAME OVER



# The DØ Detector





**Central region:**

- *Proportional Drift Tubes*

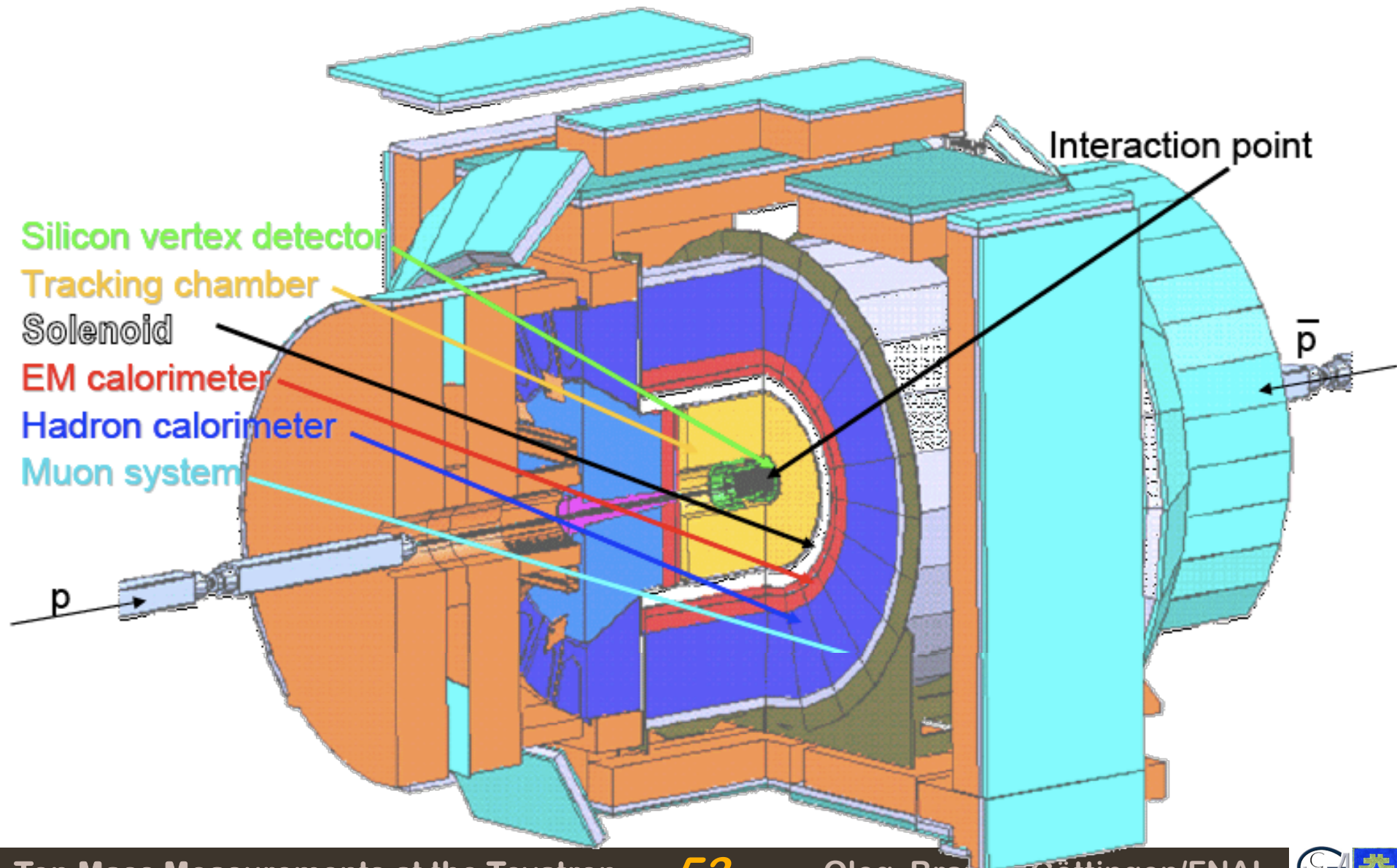
**Forward region:**

- *Mini Drift Tubes*
- *Scintillator counters*

**In each layer for timing**



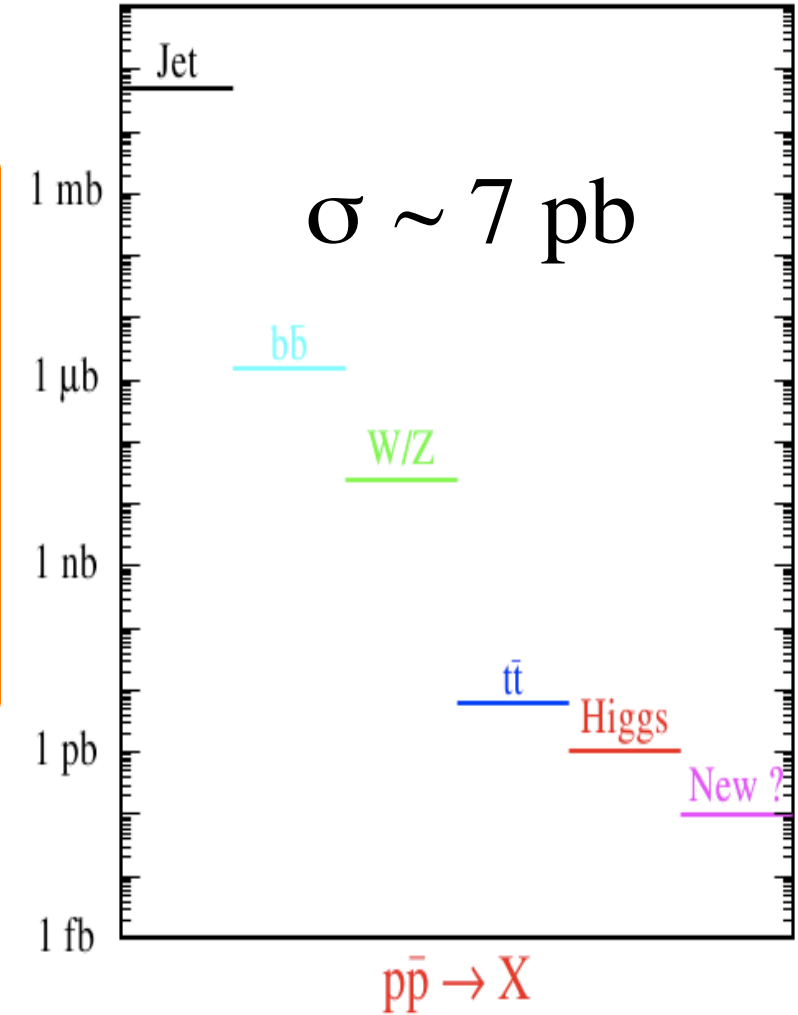
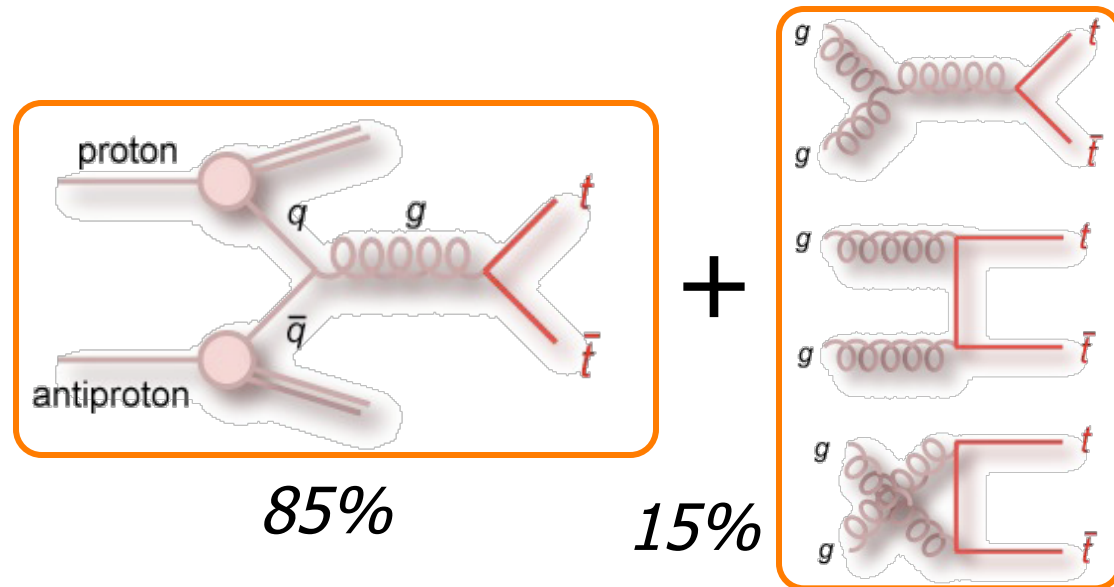
# The CDF Detector



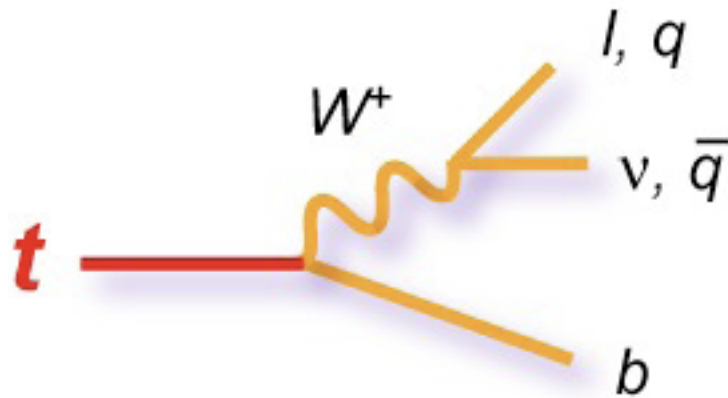
- tt pairs produced via strong interaction at the Tevatron:

Cross Section

E

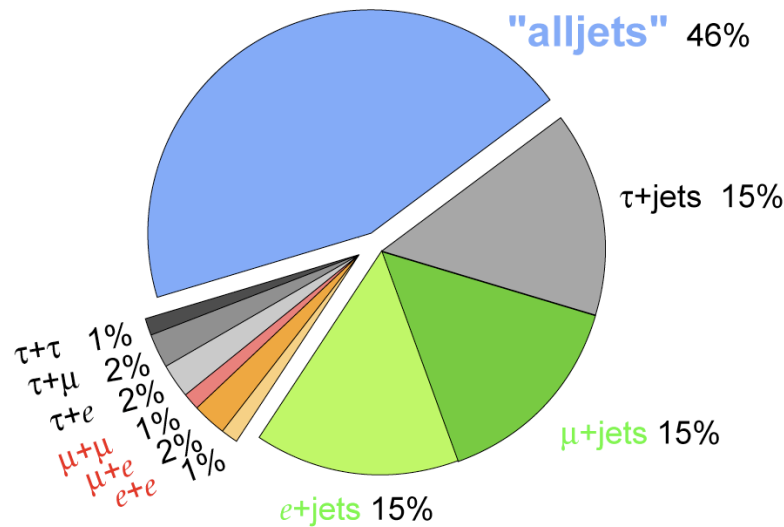


- In the SM:
  - $|V_{tb}| = 0.9990-0.9992$   
@ 95% C.L. assuming  
3 CKM generations
- Characterise  $t\bar{t}$  final states  
by top decays!



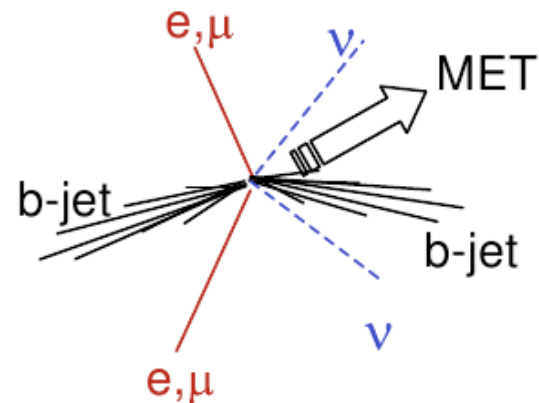
- In the SM:
  - $|V_{tb}| = 0.9990-0.9992$   
@ 95% C.L. assuming  
3 CKM generations
- Characterise  $t\bar{t}$  final states  
by top decays!

### Top Pair Branching Fractions

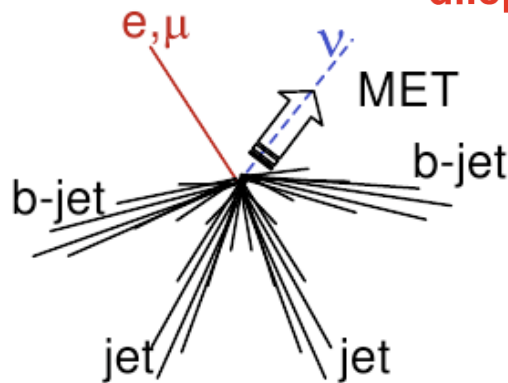


"dileptons"

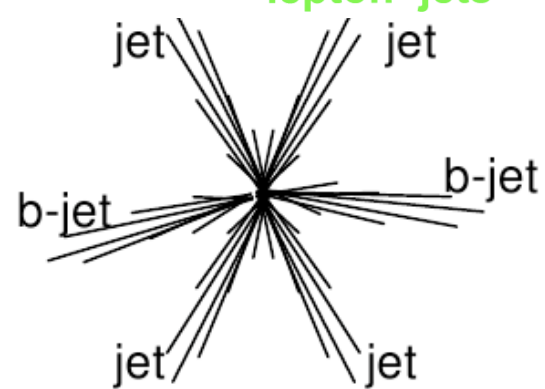
"lepton+jets"



**Dilepton**  
(BR~5%, low bckg)



**Lepton+jets**  
(BR~30%, moderate bckg)



**All-hadronic**  
(BR~46%, huge bckg)

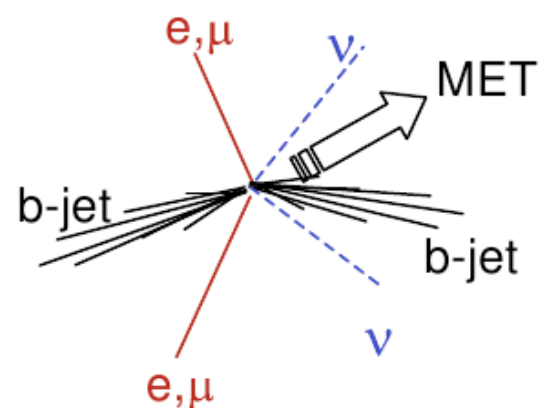




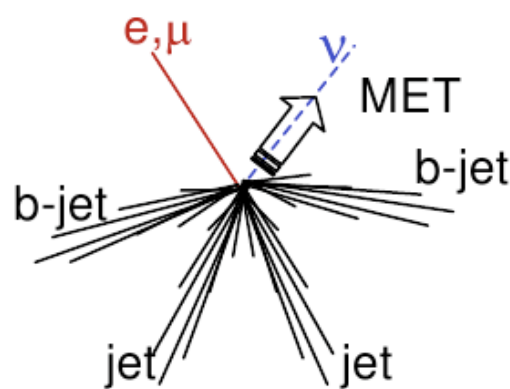
# Typical $t\bar{t}b\bar{b}$ preselection



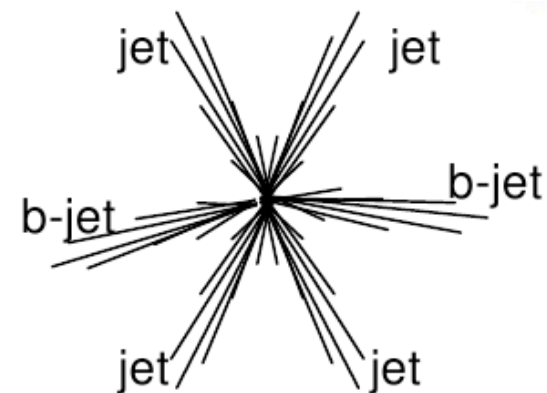
Dilepton	Lepton+jets	All-hadronic
2 high- $p_T$ leptons	1 high- $p_T$ lepton ( $>20$ GeV)	No leptons
Missing $E_T$	Missing $E_T$ ( $>40$ GeV)	No missing $E_T$
2 jets	4 jets ( $> 20$ GeV)	6 jets
$\geq 0$ b-tags	$\geq 1$ b-tag	$\geq 1$ b-tag
S/B:		



**Dilepton**  
(BR~5%, low bckg)



**Lepton+jets**  
(BR~30%, moderate bckg)



**All-hadronic**  
(BR~46%, huge bckg)

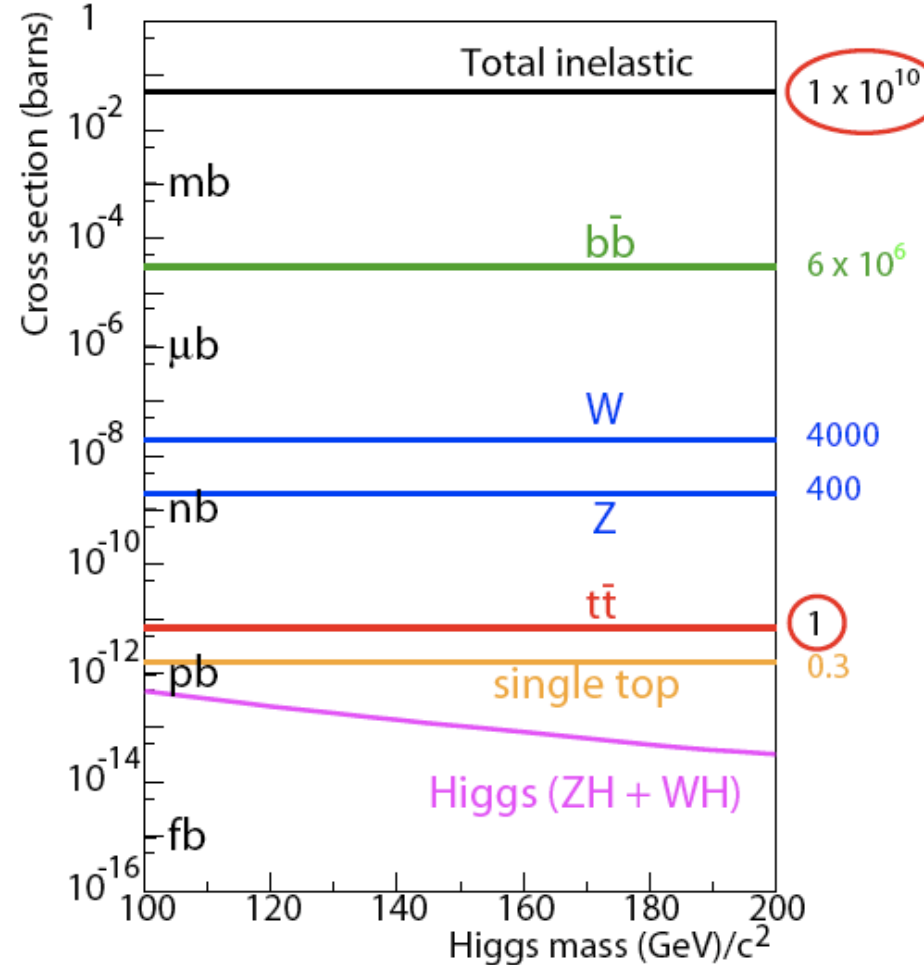
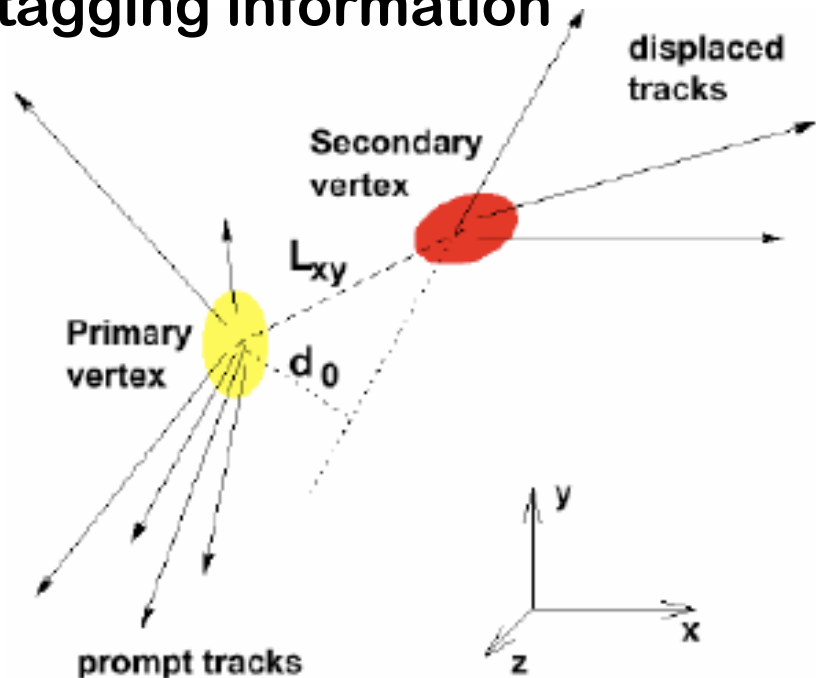




# Top Mass: Experimental Challenges



- The Tevatron is a hadron collider
  - Very high backgrounds!
- Backgrounds can bias the top mass measurement
- Control backgrounds using b-tagging information



See talk by F. Deliot (top Xsec)





# Top Mass in the Lepton+Jets Channel (I)



- Template method, CDF (4.8 fb<sup>-1</sup>)
  - Use two observables to maximise sensitivity to top mass:
    - $m_{\text{top}}(1) \rightarrow$  top mass of best  $\chi^2$  fit
    - $m_{\text{top}}(2) \rightarrow$  top mass of second best  $\chi^2$  fit

- Define the  $\chi^2$  as:
  - Consistency w/ meas'd  $p_T$  values
  - Consistency w/ underlying event

$$\chi^2 = \sum_{i=l,4jets} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(U_j^{fit} - U_j^{meas})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{\ell\nu} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - m_t^{\text{reco}})^2}{\Gamma_t^2} + \frac{(M_{b\ell\nu} - m_t^{\text{reco}})^2}{\Gamma_t^2}$$

Consistency w/ known W mass w/ exp. resol'n

Consistency w/ reconstructed  $m_{\text{top}}$  within experimental resolution

- $\chi^2 = \chi^2(m_{\text{reco}}(\text{top}), \text{JES})$
- Drop events with  $\chi^2 > 9!$

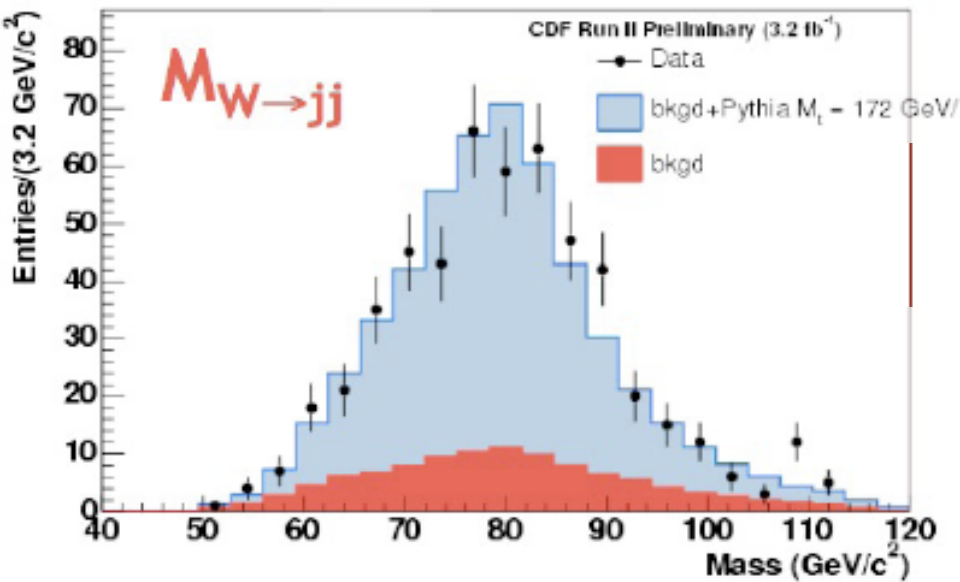




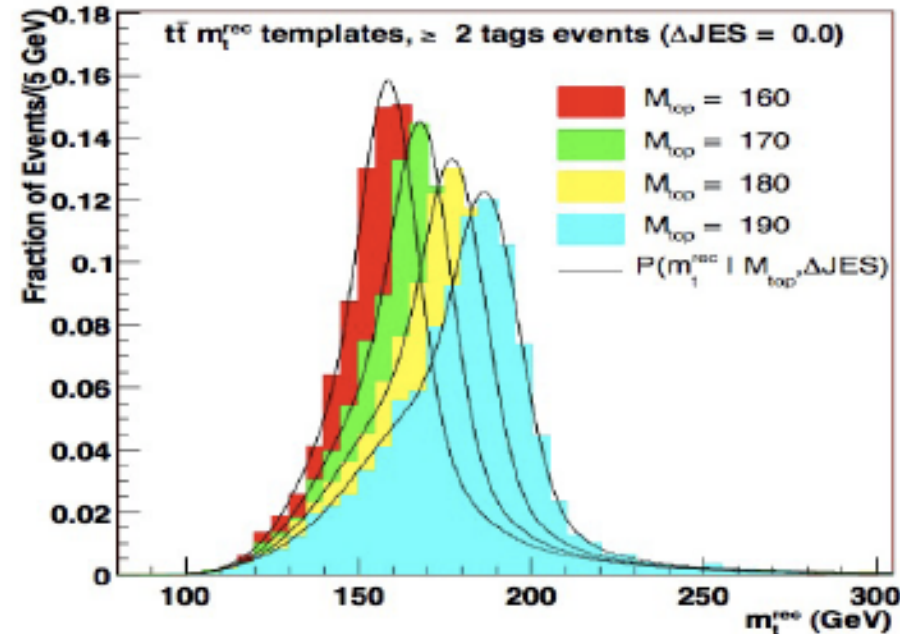
# Top Mass in the Lepton+Jets Channel (I)



- Play experimental trick:
  - Largest experimental uncertainty is the JES
  - perform an in-situ calibration of the JES via the  $\chi^2$  fit



- Construct  $m_{top}$ -dependent  $\rightarrow$  templates



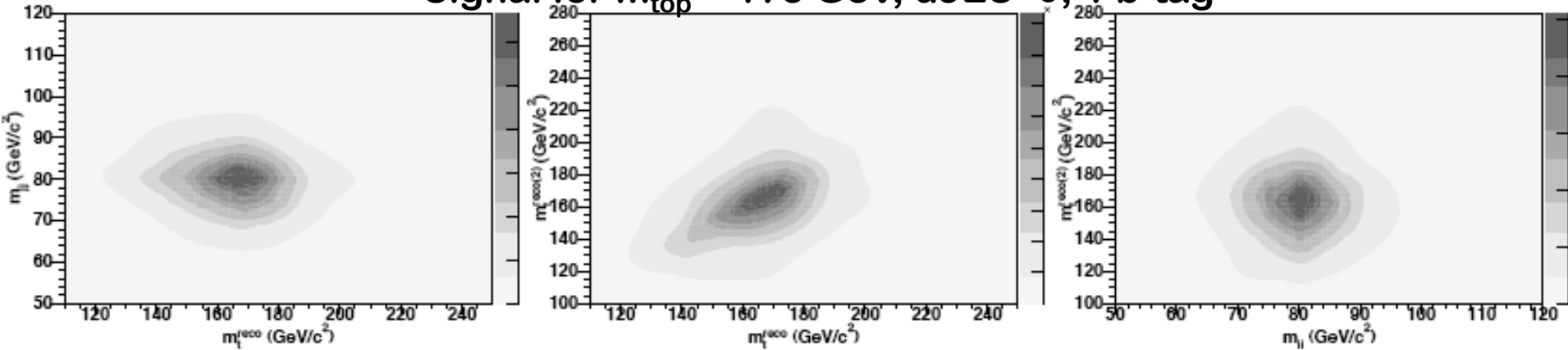


# Top Mass in the Lepton+Jets Channel (I)

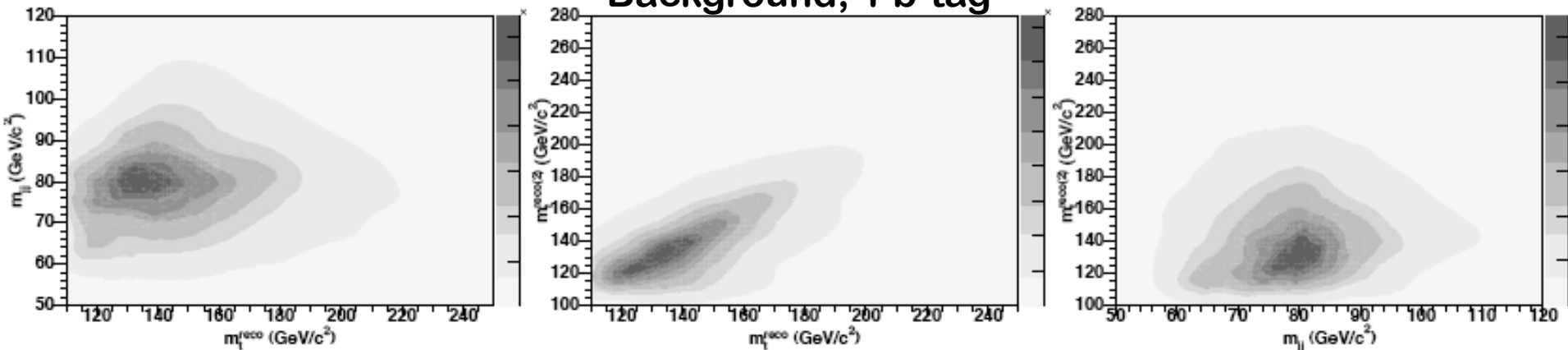


- In reality, matters with 3D-pdf are a bit more complicated:
  - Look at 2D projections of 3D pdf:

Signal for  $m_{\text{top}} = 175 \text{ GeV}$ ,  $d\text{JES}=0$ , 1 b-tag



Background, 1 b-tag

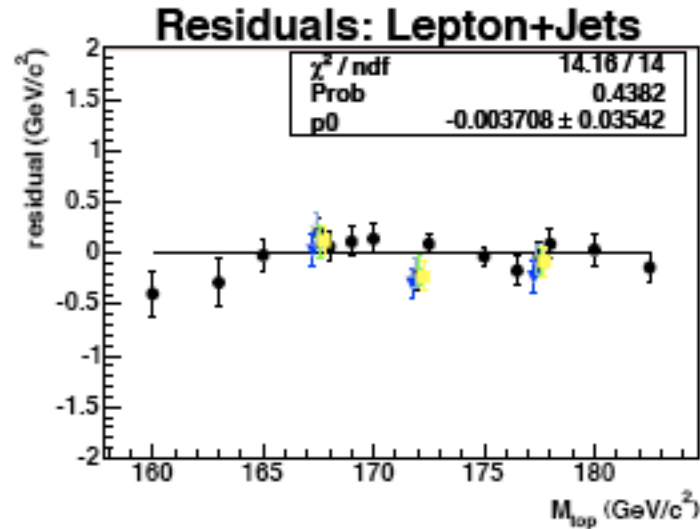
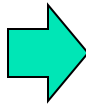
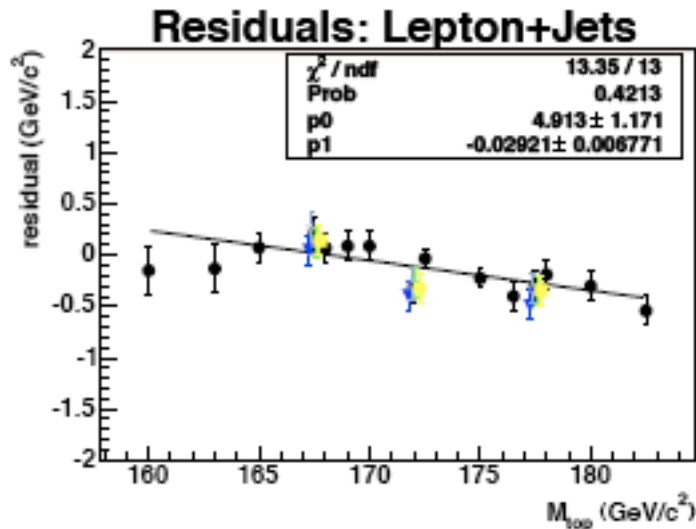




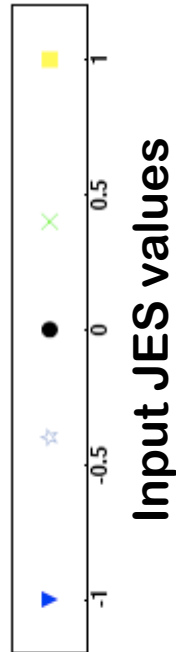
# Top Mass in the Lepton+Jets Channel (I)



- Not quite ready to extract the top mass yet
  - Need to calibrate the method (ensemble tests):
    - Possible biases due to simulation, acceptance, ... effects
    - Over/underestimation of statistical uncertainty



- Correct for residual slope: +3%
- Inflate statistical uncertainties by 4.1%



- We obtain:

$$M_{\text{top}} = 172.2 \pm 1.2 \text{ (stat.)} \pm 1.0 \text{ (syst.) GeV}/c^2 = 172.2 \pm 1.5 \text{ GeV}/c^2$$



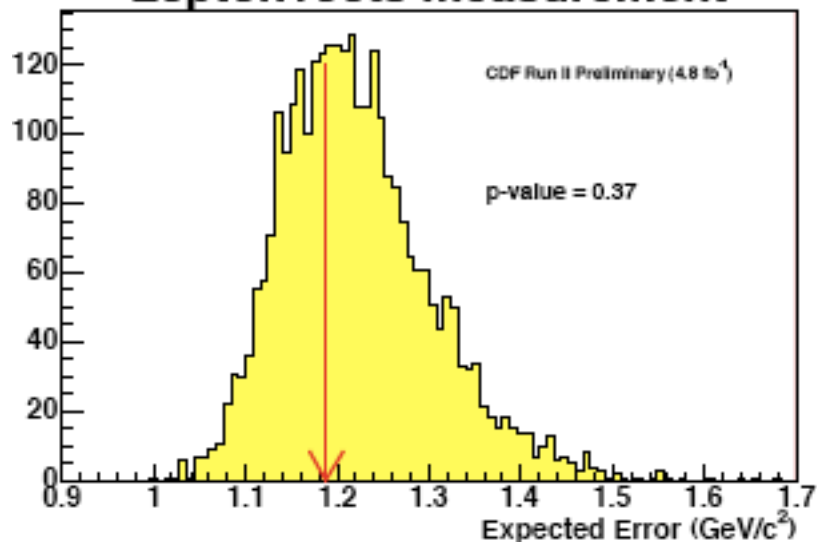


# Top Mass in the Lepton+Jets Channel (I)



## ■ Did we get lucky?

### Lepton+Jets measurement



## Systematic Uncertainties

CDF II Preliminary 4.8 fb<sup>-1</sup>

Systematic	LJ
Residual JES	0.6
Generator:	0.7
PDFs	0.1
b jet energy	0.2
Background shape	0.1
gg fraction	<0.1
Radiation	0.1
MC statistics	0.1
Lepton energy	<0.1
MHI	0.1
Color Reconnection	0.2
<b>Total systematic</b>	<b>1.0</b>

