

$t\bar{t}$ Cross Section Measurements At the Tevatron

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on behalf of CDF and D0 Collaborations



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fondamentales de
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saclay



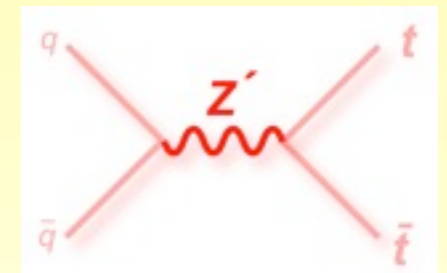
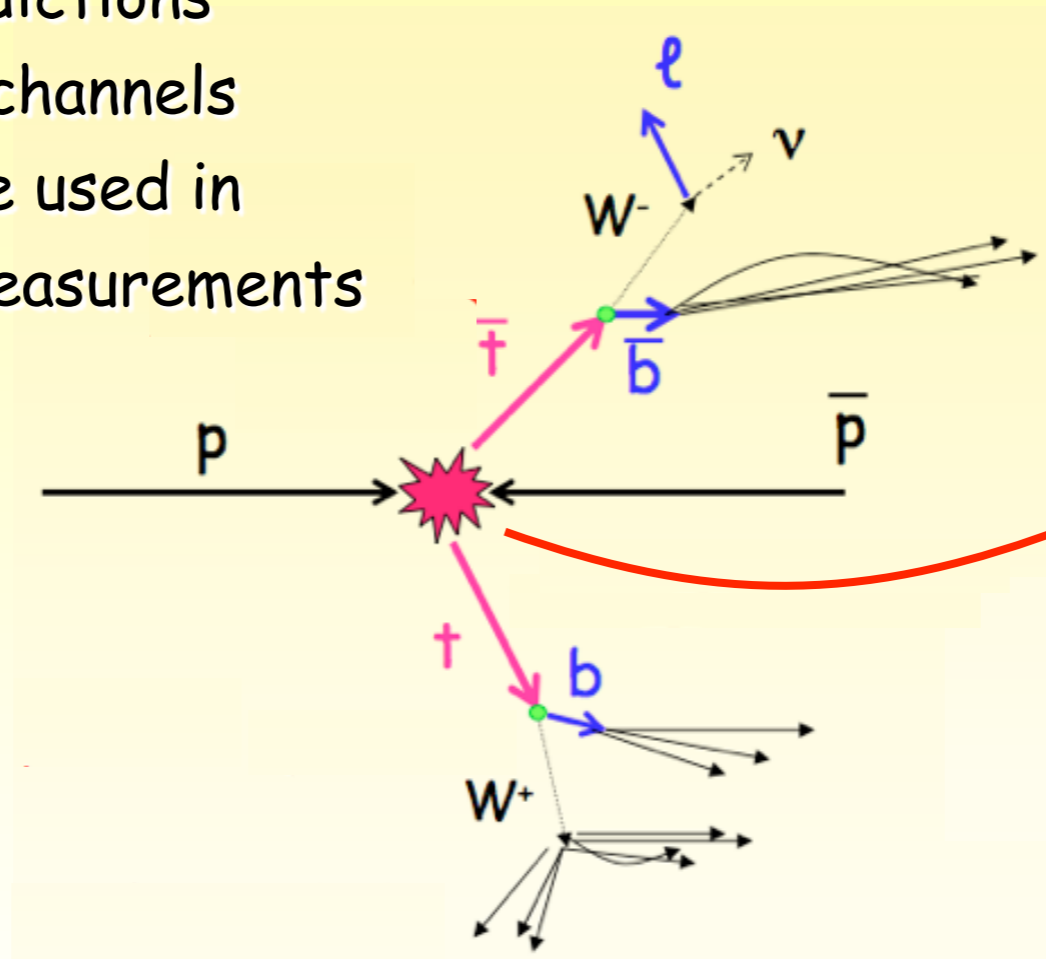
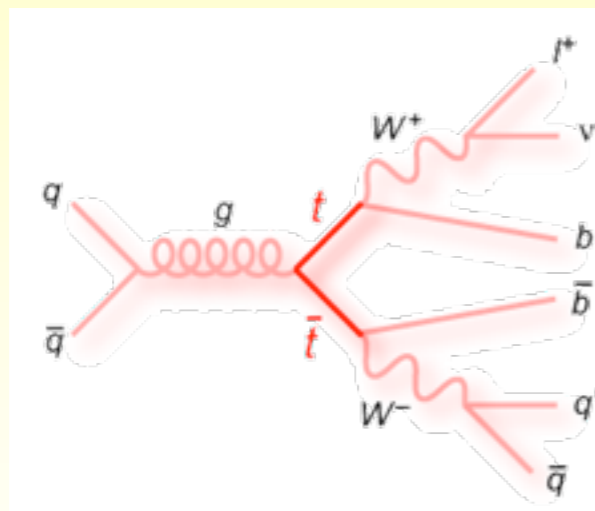
TOP 2010 International Workshop
31-MAY-2010, Bruges

Why Do We Study the Top Quark ?

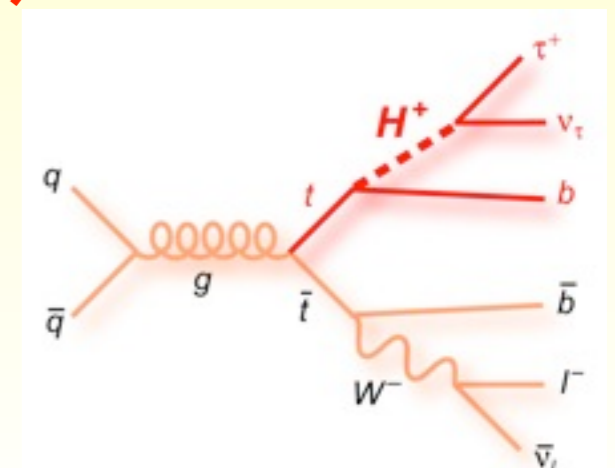
$$\mathcal{L}_{\text{Yukawa}} = -\lambda_t \overline{\psi_{Lt}} \Phi \psi_{Rt}$$

$\lambda_t \approx 1??$ $m_t \gg m_b$
 $\Gamma_t \gg \Lambda_{QCD}$

- The top quark is a special quark !
- What kind of role does it play in EW symmetry breaking ?
- Measure its strong production mechanism: $t\bar{t}$ cross section
 - compare with QCD predictions
 - measure in all possible channels
 - check $t\bar{t}$ selection to be used in the other properties measurements

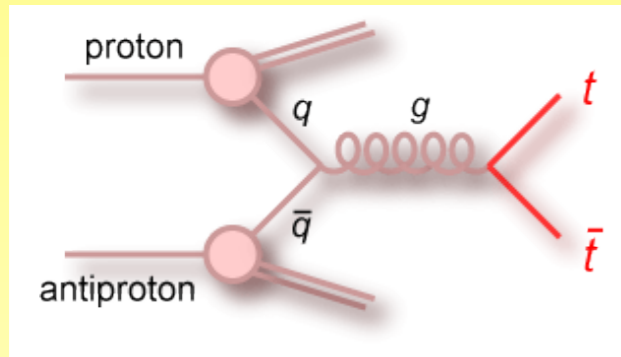


new physics ?

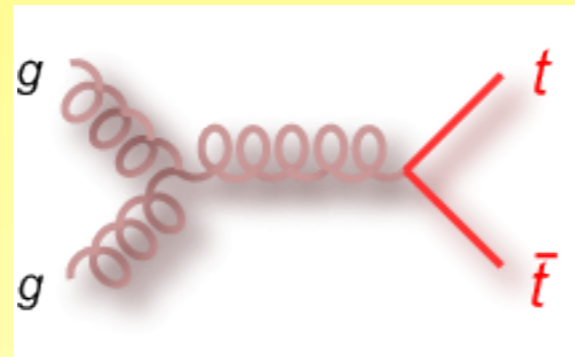


Top Strong Production and Decay At the Tevatron

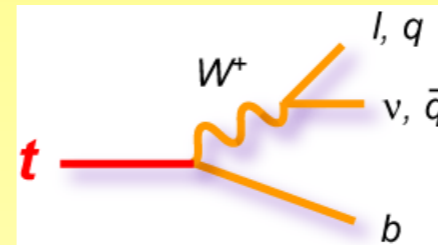
- pair production and decay:



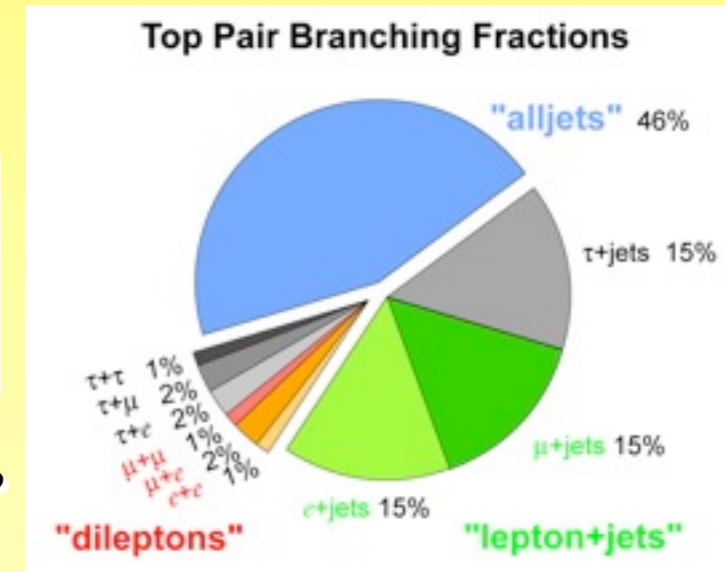
~ 85 %



~ 15 %



$B(t \rightarrow Wb) \sim 100 \%$



- theoretical computations:

$M_t = 172.5 \text{ GeV}, \sigma(t\bar{t}) \approx 7.5 \text{ pb} (\sim \text{NNLO})$

S. Moch and P. Uwer	Phys. Rev. D78 034003 (2008)	$\sigma_{t\bar{t}} = 7.46^{+0.48}_{-0.67} \text{ pb}$
Kidonakis <i>et al.</i>	Phys. Rev. D78 074005 (2008)	$\sigma_{t\bar{t}} = 7.27^{+0.76}_{-0.85} \text{ pb}$
Cacciari <i>et al.</i>	JHEP 09 127 (2008)	$\sigma_{t\bar{t}} = 7.14^{+0.76}_{-0.87} \text{ pb}$

$\Delta \sigma / \sigma \sim 8 \%$

- comparison with LHC:

$M_t = 172.5 \text{ GeV}, \sigma(t\bar{t}) \approx 161 \text{ pb} (@ 7 \text{ TeV})$

with same ℓ jets selection efficiency (4 jets): ~ 10 %

$n_{t\bar{t}}(1 \text{ fb}^{-1} \text{ in one LHC exp.}) \approx 2n_{t\bar{t}}(10 \text{ fb}^{-1} \text{ in one Tevatron exp.})$

We have large samples of $t\bar{t}$ events

A lot of our $t\bar{t}$ cross section measurements are already systematic limited

How Do We Measure the $t\bar{t}$ Cross Section ?

- Analysis strategy:

$$\sigma_{t\bar{t}} = \frac{N_{data} - N_{bkg}}{\epsilon_{t\bar{t}}(M_t) \int \mathcal{L} dt}$$

from MC (Alpgen+Pythia or Pythia)

analyzed integrated luminosity:

- removing poor quality data
- for the particular set of triggers used
- uncertainty: $\sim 6\%$

$$N_{data} - N_{bkg}$$

estimated by:

- event counting after selection cuts
- signal/background fit of a discriminant variable

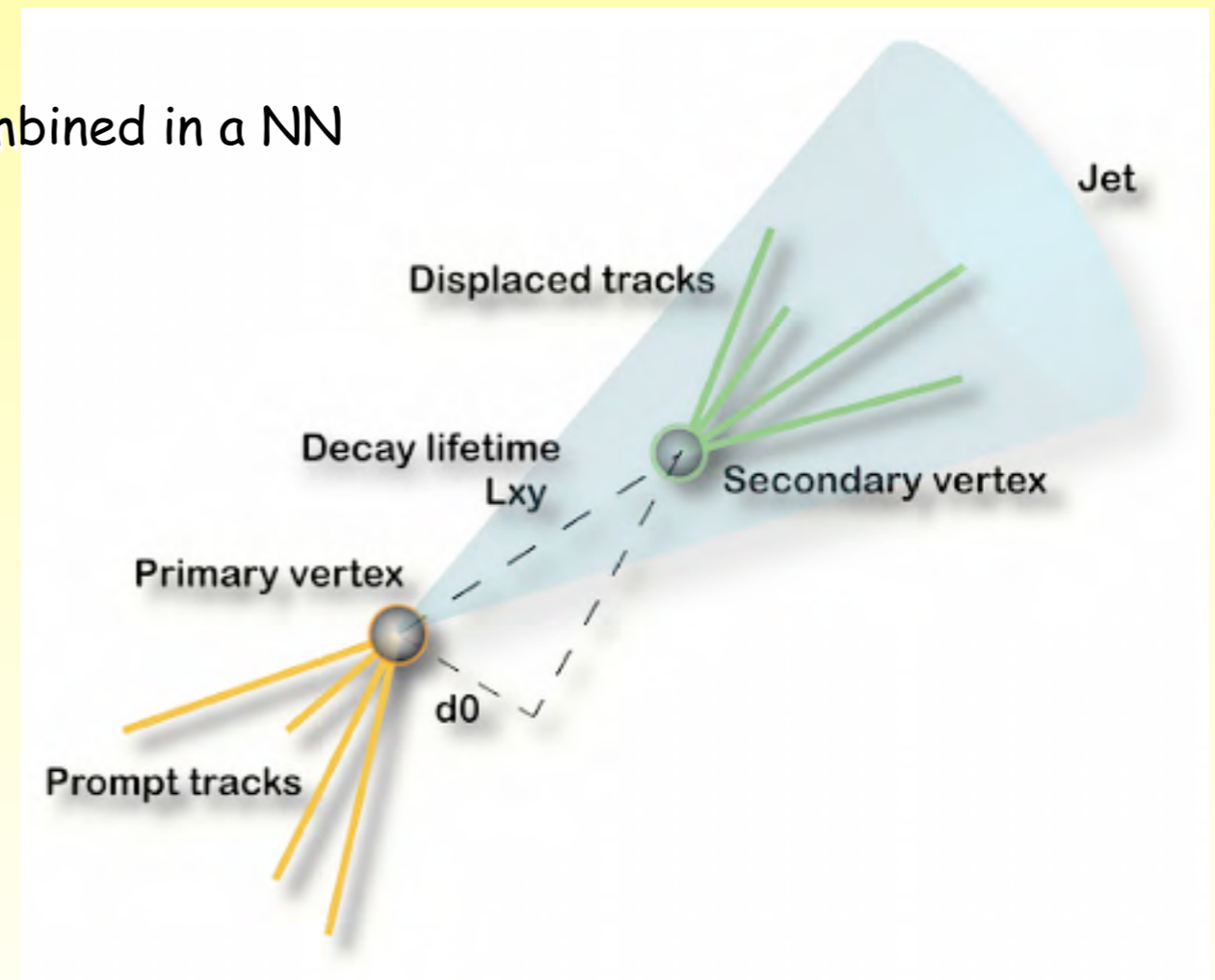
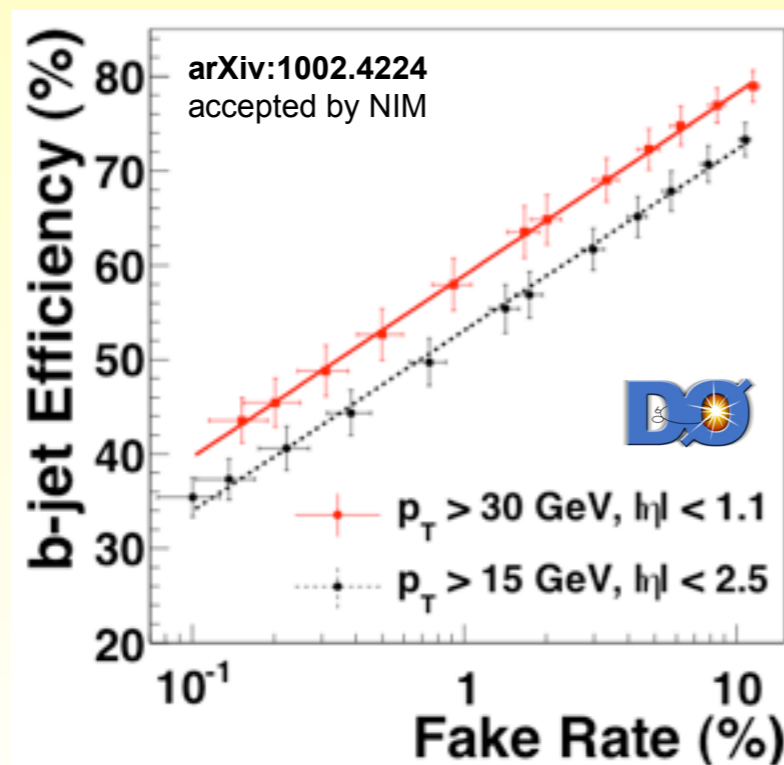
$$(\epsilon_{bkg1}\sigma_{bkg1} + \epsilon_{bkg2}\sigma_{bkg2} + \dots) \int \mathcal{L} dt$$

Channel	topological		b-tagging	
	counting	fit	counting	fit
l jets		X	X	
ll	X		X	
$l\tau$			X	
all had				X

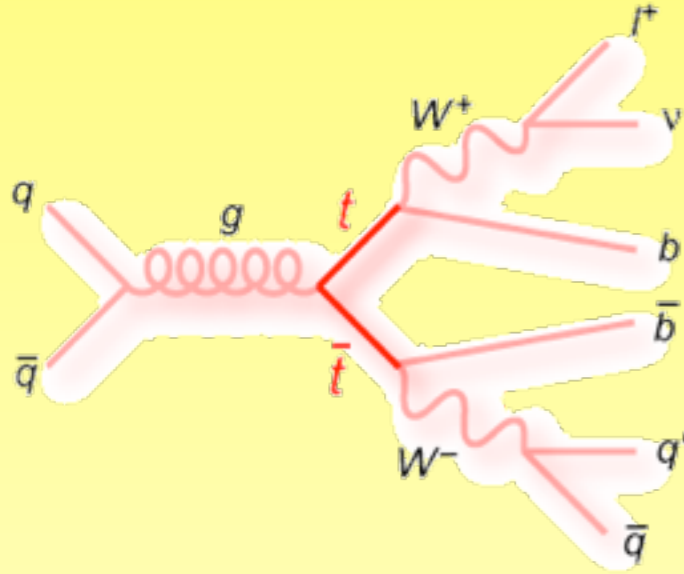
b Jet Tagging

- utilize b-jets special properties to separate them from light/gluon jets:
 - long b-hadrons decay length
 - b-hadrons semileptonic decay
- 3 main b-tagging algorithms:
 - impact parameter based
 - secondary vertex reconstruction
 - soft lepton tag

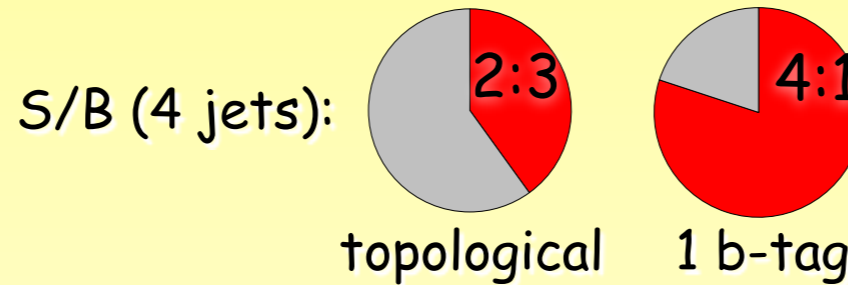
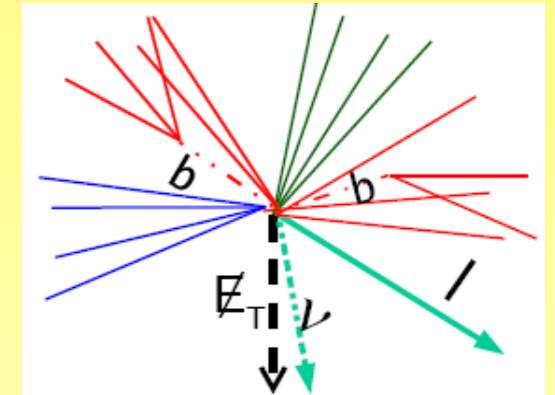
} combined in a NN



Lepton + Jets Channel



- signature:
 - high pt isolated lepton
 - large Missing Et (MET)
 - 4 jets (2 b-jets)



- main backgrounds:

- W+jets (W+light, W+HF)
- multijets
- electroweak (Z+jets, diboson, single top)

shape from MC (Alpgen), total among fitted to Data

no reliable estimation from MC
 DO: data matrix method
 CDF: fit the low part of the MET distribution

using MC (Alpgen or Pythia, single top: CompHep or Madgraph)
 normalized to the NLO cross sections

Multijet Background Estimation

- the matrix method:

sample with loose isolated lepton:

$$N_{loose} = N_{QCD} + N_{signal}$$

subsample with tight isolated lepton:

$$N_{tight} = \epsilon_{QCD} N_{QCD} + \epsilon_{signal} N_{signal}$$



low MET sample

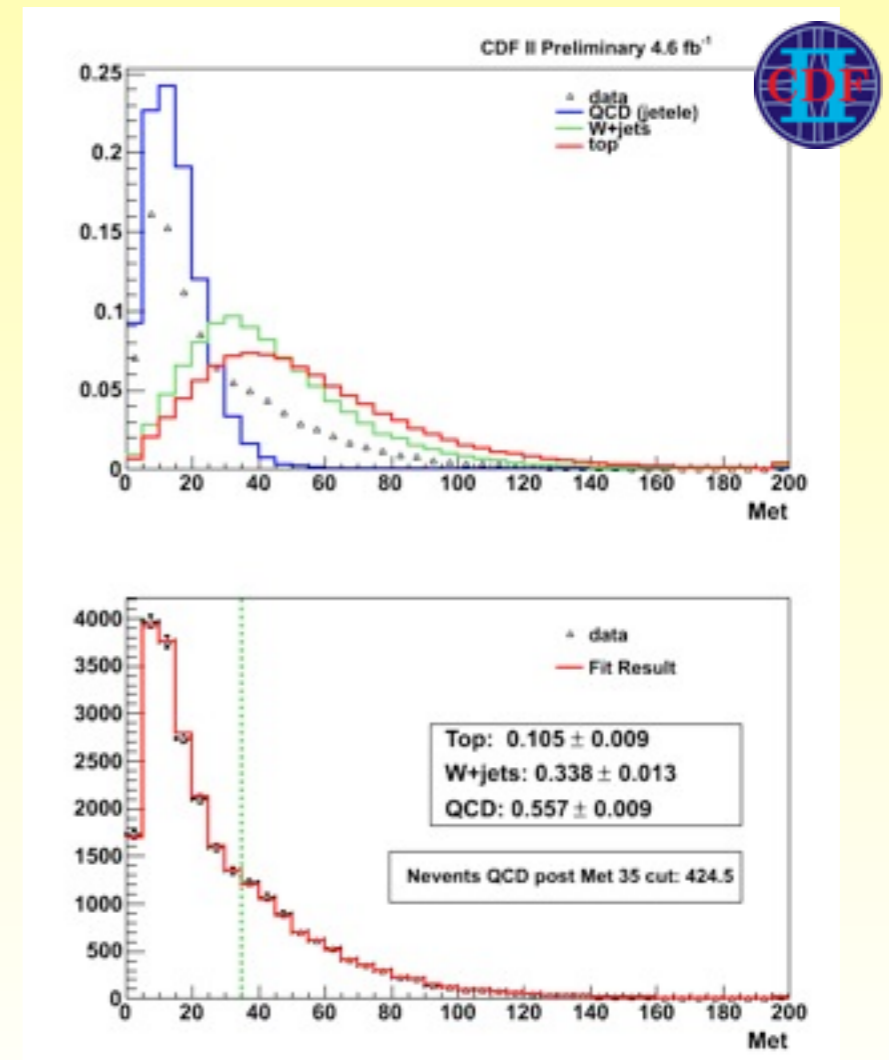
W+jets, $t\bar{t}$, ...

from W MC

$$N_{QCD} = \frac{\epsilon_{signal} N_{loose} - N_{tight}}{\epsilon_{signal} - \epsilon_{QCD}}$$

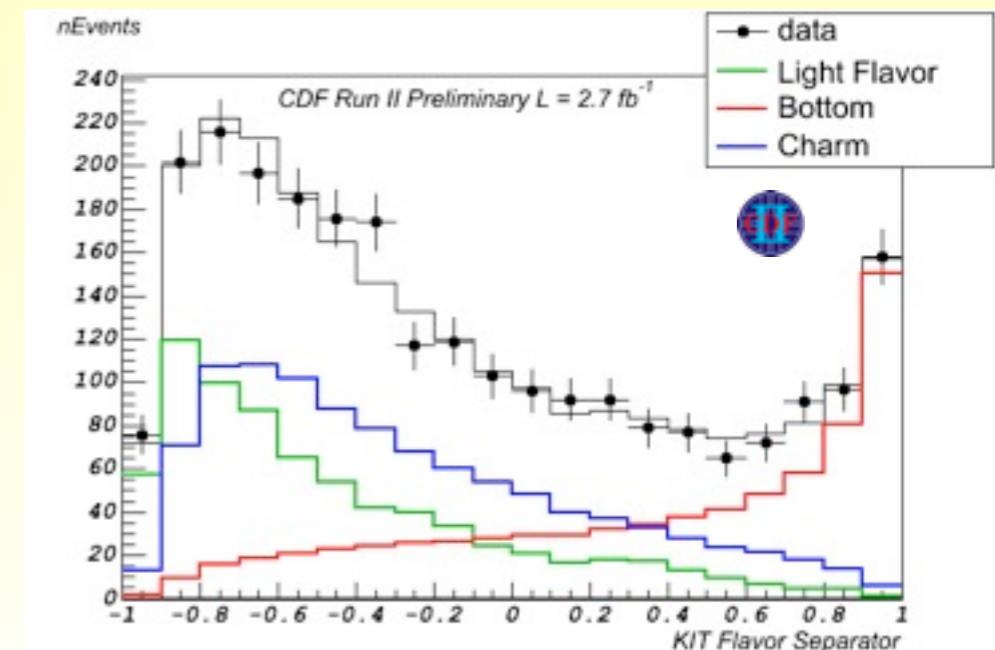
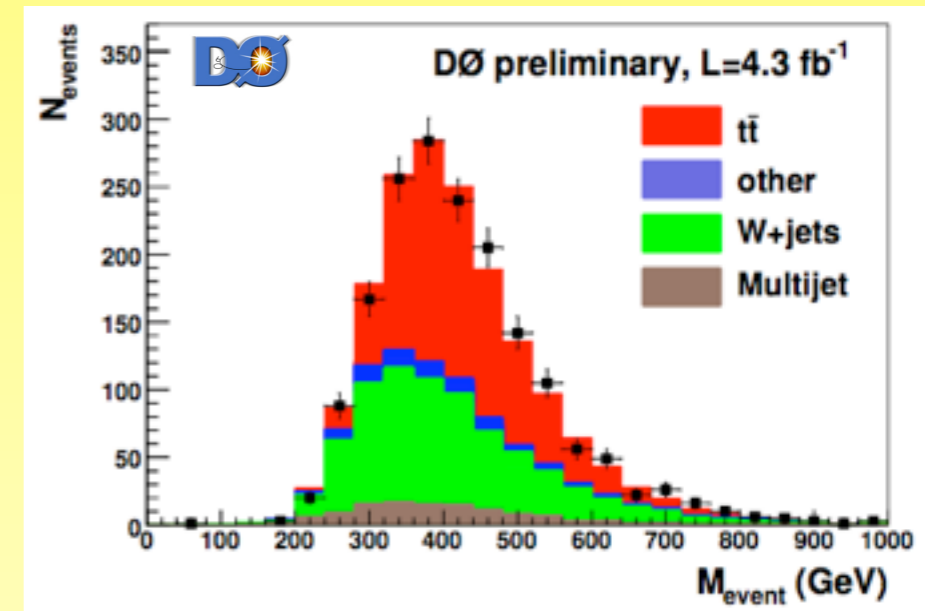
- fit the low part of the MET distribution:

- templates: multijets (data that fails lepton ID criteria), W+jets (Alpgen) and $t\bar{t}$ (Pythia)
- fit the low MET part
- extract fraction of multijets in the high MET part



W+jets Normalization

- normalize to data before b-tagging:
 - shape from Alphen
 - $N_{W+jets} = N_{data} - N_{t\bar{t}} - N_{QCD} - N_{EW}$
 - in each jet multiplicity
- normalization of the W+heavy flavor fraction in W+jets:
 - W+HF cross section underestimated in the MC
 - W+HF content measured in data in the 1 or 1-2 jet event sample
 - NN trained to separate W+light from W+HF
 - scale the W+HF fraction to match the data (normalization extrapolated to higher jet multiplicities)





Lepton + Jets Topological Cross Section



- signal/background discrimination:
 - $t\bar{t}$ more energetic, central and isotropic than W +jets and multijets
 - NN (CDF) or BDT (DØ) input variables: H_t , aplanarity, sphericity, ...
- cross section measurement:
 - template fit of $t\bar{t}$ and W +jets to the discriminant output

$\Delta \sigma / \sigma$ in %	
Systematic	$t\bar{t}_{ANN}$
Luminosity	5.8
b -tag modeling	-
W +HF correction	-
Jet energy scale	2.9
Monte Carlo generator	2.6
Initial/final state radiation	0.4
PDF	0.9
Background shape model	1.9
Lepton ID/trigger	1.3
Total	7.5

channel	$\sigma_{t\bar{t}}$ [pb]
e +jets	$6.53^{+0.79}_{-0.69}$ (stat+syst)
μ +jets	$8.37^{+1.08}_{-0.93}$ (stat+syst)
ℓ +jets	$7.70^{+0.79}_{-0.70}$ (stat+syst)

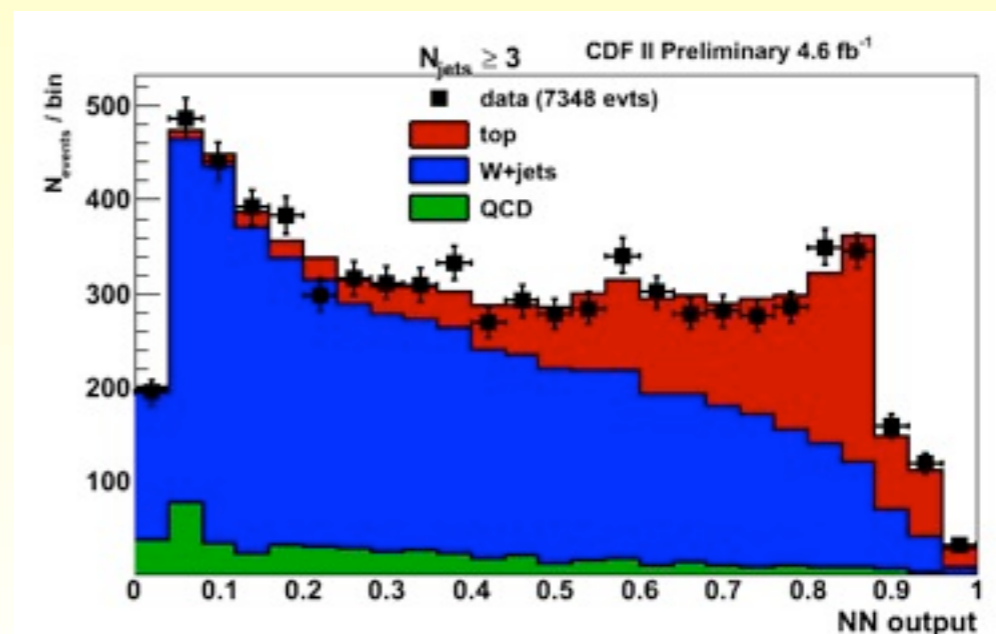
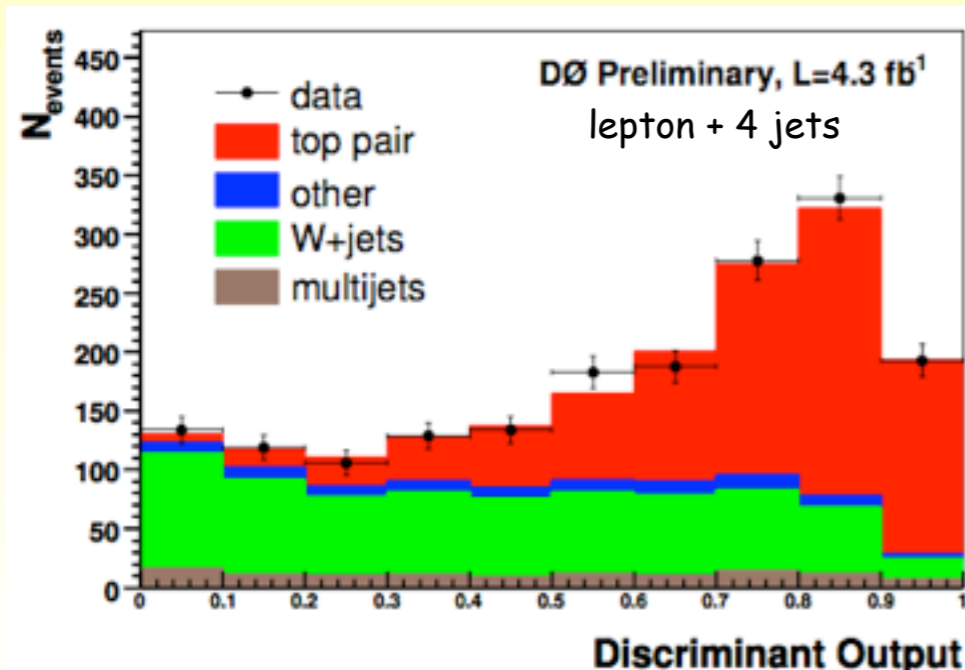
$M_t = 172.5 \text{ GeV}$



$$\sigma_{t\bar{t}} = 7.71 \pm 0.37(\text{stat}) \pm 0.36(\text{sys}) \pm 0.45(\text{lumi})\text{pb}$$

$M_t = 172.5 \text{ GeV}$

$\Delta \sigma / \sigma \sim 9 \%$



Lepton + Jets Cross Section Using b-tagging

- counting by number of jets and b-tag jets:
 - b-tagging mistag rate measured in data, parametrization applied to W+jets

channel	$\sigma_{t\bar{t}}$ [pb]
e+jets	$7.41^{+1.07}_{-0.96}$ (stat+syst)
μ +jets	$8.60^{+1.27}_{-1.06}$ (stat+syst)
ℓ +jets	$7.93^{+1.04}_{-0.91}$ (stat+syst)

$M_t = 172.5 \text{ GeV}$

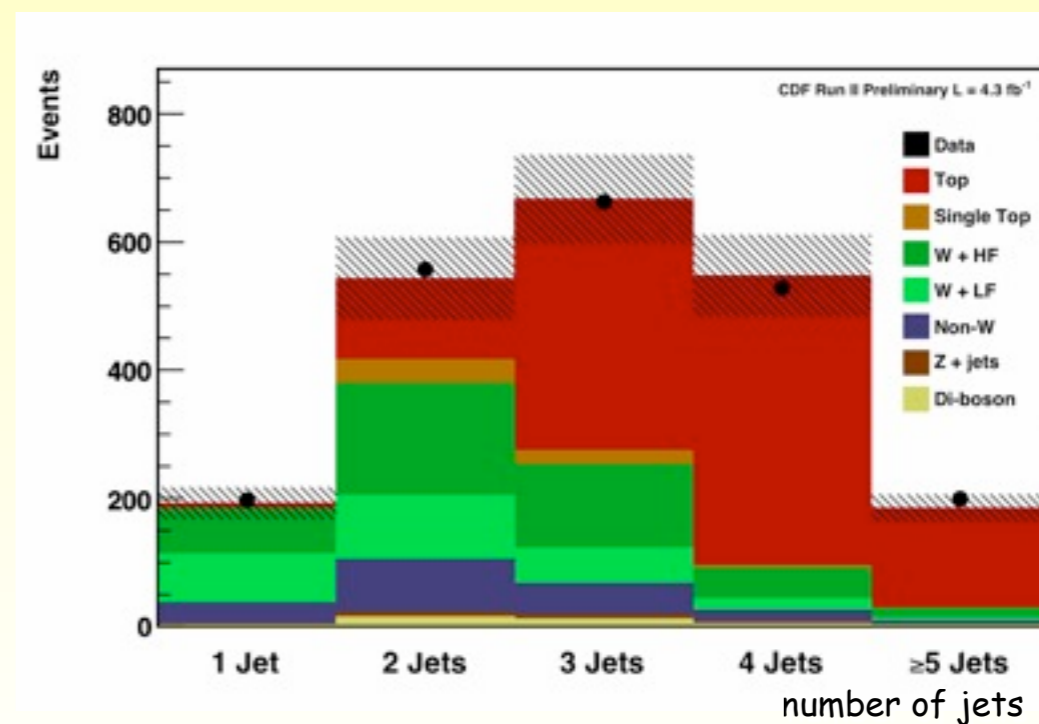
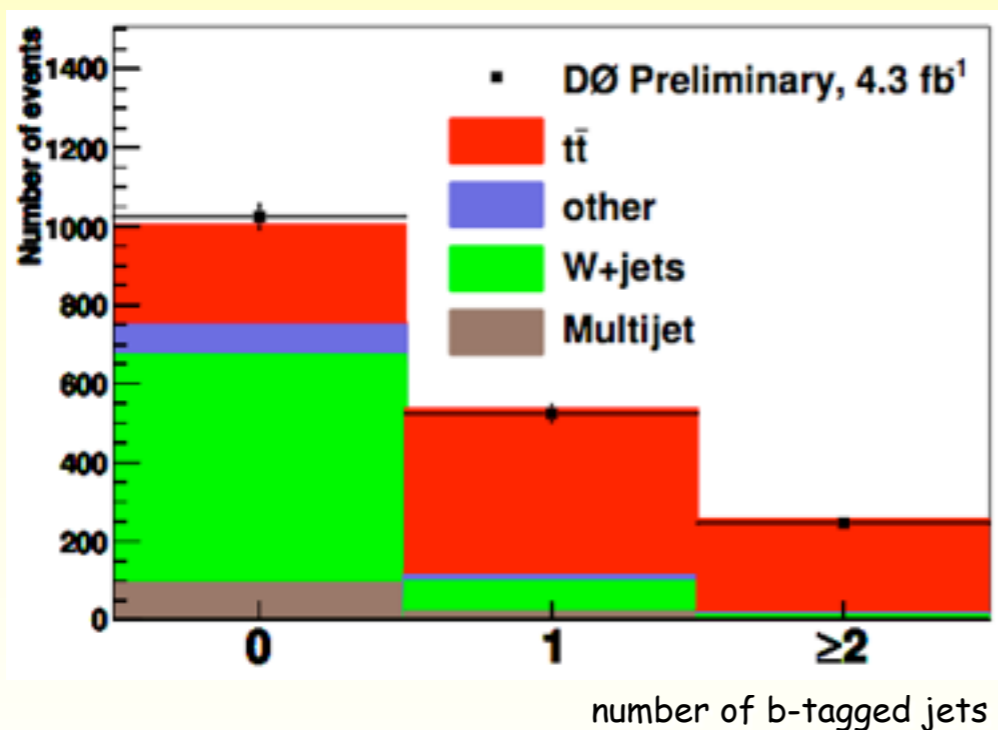
channel	sample	1 b-tag	≥ 2 b-tags
e+3 jets	W+jets	245 ± 25	20 ± 4
	Multijet	49 ± 8	4 ± 1
	Z+jets	20 ± 6	2 ± 1
	Other	29 ± 5	6 ± 1
	$t\bar{t}$	302 ± 25	120 ± 14
Total		645 ± 33	153 ± 16
	Observed	648	154
e+4 jets	W+jets	41 ± 10	5 ± 1
	Multijet	15 ± 3	1 ± 0.2
	Z+jets	4 ± 2	0.4 ± 0.2
	Other	5 ± 1	1 ± 0.4
	$t\bar{t}$	229 ± 32	136 ± 19
Total		294 ± 25	144 ± 19
	Observed	289	127



$$\sigma_{t\bar{t}} = 7.22 \pm 0.35(\text{stat}) \pm 0.56(\text{sys}) \pm 0.44(\text{lumi})\text{pb}$$

$M_t = 172.5 \text{ GeV}$

$\Delta \sigma / \sigma \sim 11 \%$



$t\bar{t}/Z$ Cross Section

submitted to PRL

- luminosity largest systematic uncertainty:
 - from luminosity detector acceptance and $p\bar{p}$ inelastic cross section
- remove luminosity uncertainty doing the ratio with the Z cross section:
 - $Z \rightarrow \ell\ell$ cross section measured with the same trigger
 - correlation of systematic uncertainties taken into account
 - multiply by the theoretical Z cross section:

$$\sigma_{t\bar{t}} = \left(\frac{\sigma_{t\bar{t}}}{\sigma_Z} \right)_{exp} (\sigma_Z)_{th}$$

$$(\sigma_{Z/\gamma^* \rightarrow \ell\ell})_{th} = 251.3 \pm 5.0 \text{ pb}$$

Eur. Phys. J. **C35**, 325 (2004)

- combination of the topological and b-tagging cross sections using BLUE

Systematic	$t\bar{t}_{tag}$	$t\bar{t}_{ANN}$	$Z/\gamma^* \rightarrow \ell\ell$
Luminosity	6.1	5.8	5.9
b-tag modeling	4.7	-	-
W+HF correction	4.0	-	-
Jet energy scale	4.1	2.9	-
Monte Carlo generator	2.7	2.6	-
Initial/final state radiation	0.6	0.4	-
PDF	0.6	0.9	1.4
Background shape model	0.2	1.9	0.3
Lepton ID/trigger	1.3	1.3	1.1
Total	10.0	7.5	6.2
Total $\sigma_{t\bar{t}}/\sigma_{Z/\gamma^* \rightarrow \ell\ell}$	8.2	4.7	



$$\text{topo : } \sigma_{t\bar{t}} = 7.82 \pm 0.38(\text{stat}) \pm 0.37(\text{sys}) \pm 0.15(\text{theory}) \text{ pb}$$

$$\text{b-tag : } \sigma_{t\bar{t}} = 7.32 \pm 0.36(\text{stat}) \pm 0.56(\text{sys}) \pm 0.14(\text{theory}) \text{ pb}$$

$M_t = 172.5 \text{ GeV}$

combined:

$$\sigma_{t\bar{t}} = 7.70 \pm 0.52 \text{ pb}$$

$$\Delta \sigma / \sigma \sim 6.8 \%$$



Mass Extraction From the Cross Section

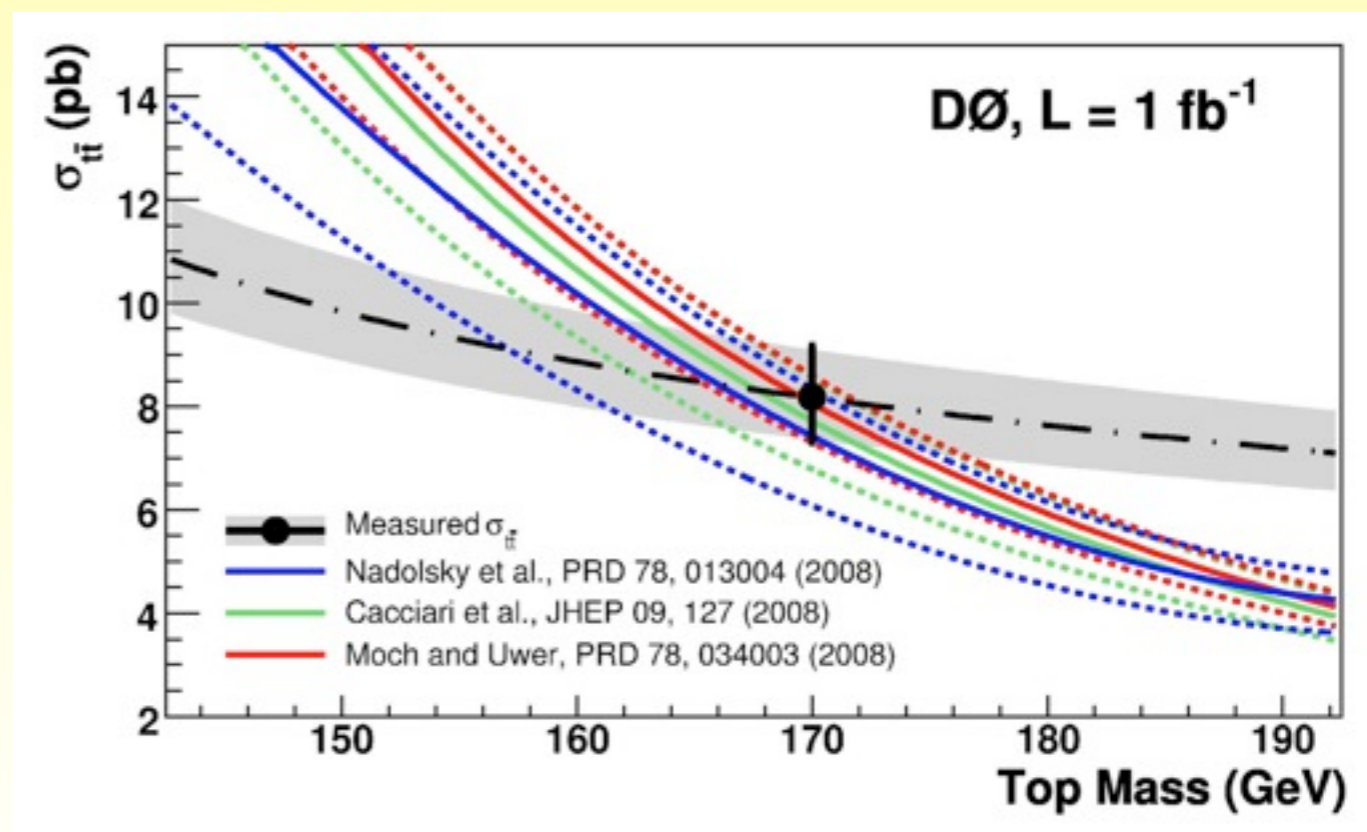
PRD80 071102 (2009)

- indirect mass measurement less sensitive to any difference between pole mass and the mass used in the MC simulation used for direct measurements
- combine experimental and theoretical $t\bar{t}$ cross section vs top mass:
 - experimental dependency due to kinematics cut (selection efficiency)
 - theoretical: use the most accurate QCD computations (\sim NNLO)
- joint normalized likelihood function based on the theoretical and the total experimental uncertainty

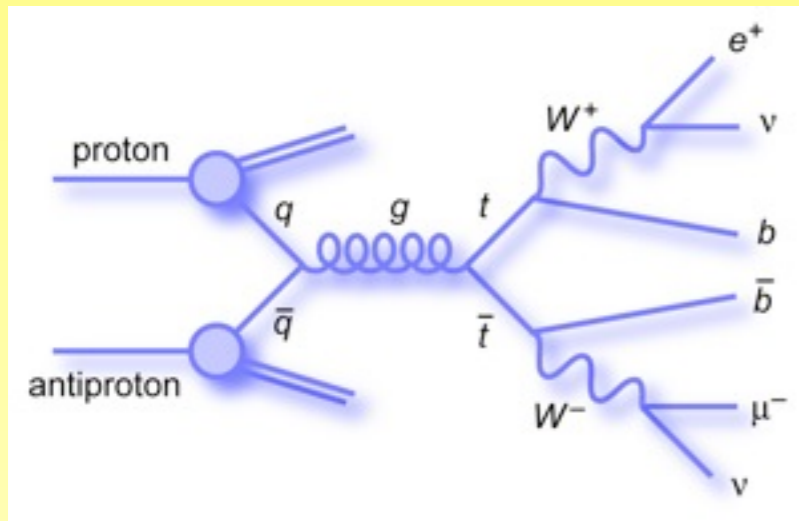


Theoretical prediction	M_t (GeV)
NLO	$165.5^{+6.1}_{-5.9}$
Cacciari <i>et al.</i>	$167.5^{+5.8}_{-5.6}$
Moch and Uwer <i>et al.</i>	$169.1^{+5.9}_{-5.2}$
Kidonakis <i>et al.</i>	$168.2^{+5.9}_{-5.4}$

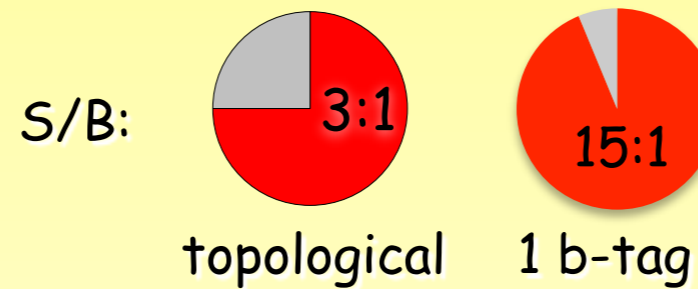
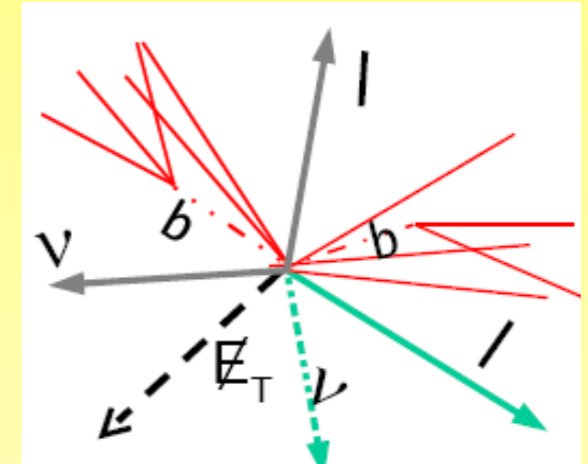
compatible with world average:
 $M_t = 173.1 \pm 1.3 \text{ GeV}$



Dilepton Channel



- signature:
 - 2 high pt isolated leptons
 - large Missing Et (MET)
 - 2 b-jets



- main backgrounds:
 - Drell-Yan, diboson
 - Multijets (fake lepton)

using MC (Alpgen or Pythia)
 normalized to the NLO cross sections
 CDF: Z+jets contamination from high MET events in the Z mass range

estimated from data: fake rate using samples with one failing lepton criteria



Dilepton Cross Section



- signal/background discrimination
 - CDF: Ht and MET significance: MET divided by its error ($ee/\mu\mu$) cuts or b-tagging
 - D0: Ht cut and BDT trained against Z and diboson ($ee/\mu\mu$)

	ee	eμ	μμ
$Z \rightarrow \ell\ell$	$8.5^{+3.4}_{-3.4}$	$11.9^{+2.7}_{-2.5}$	$21.7^{+5.6}_{-6.2}$
Dibosons	$2.1^{+0.8}_{-0.8}$	$6.5^{+2.1}_{-2.0}$	$3.3^{+1.1}_{-1.2}$
Instrumental background	$0.1^{+0.2}_{-0.1}$	$10.7^{+4.1}_{-3.9}$	$3.2^{+0.8}_{-0.7}$
$t\bar{t} \rightarrow \ell\ell jj$ ($\sigma = 7.45$ pb)	$36.9^{+3.8}_{-3.8}$	143.4 ± 14.3	$45.1^{+4.4}_{-4.3}$
Total expected events	47.6 ± 6.2	$172.6^{+16.5}_{-16.4}$	$73.3^{+8.1}_{-8.8}$
Data	55	204	72

$t\bar{t}$ Signal Events with the tight SecVtx b-tag				
Source	ee	μμ	eμ	ℓℓ
WW	0.08 ± 0.03	0.09 ± 0.04	0.21 ± 0.06	0.37 ± 0.10
WZ	0.02 ± 0.01	0.03 ± 0.01	0.03 ± 0.01	0.08 ± 0.02
ZZ	0.08 ± 0.06	0.07 ± 0.06	0.02 ± 0.02	0.17 ± 0.14
DY+LF	0.51 ± 0.05	0.60 ± 0.05	0.28 ± 0.03	1.39 ± 0.12
DY+HF	0.51 ± 0.04	1.41 ± 0.11	0.37 ± 0.03	2.28 ± 0.18
Fakes	1.17 ± 0.48	0.90 ± 0.39	3.39 ± 1.12	5.46 ± 1.59
Total background	2.36 ± 0.51	3.10 ± 0.46	4.29 ± 1.13	9.75 ± 1.68
$t\bar{t}$ ($\sigma = 7.4$ pb)	30.22 ± 1.91	29.63 ± 1.87	70.10 ± 4.38	129.96 ± 8.10
Total SM expectation	32.59 ± 2.32	32.73 ± 2.25	74.39 ± 5.42	139.71 ± 9.66
Observed	22	44	71	137

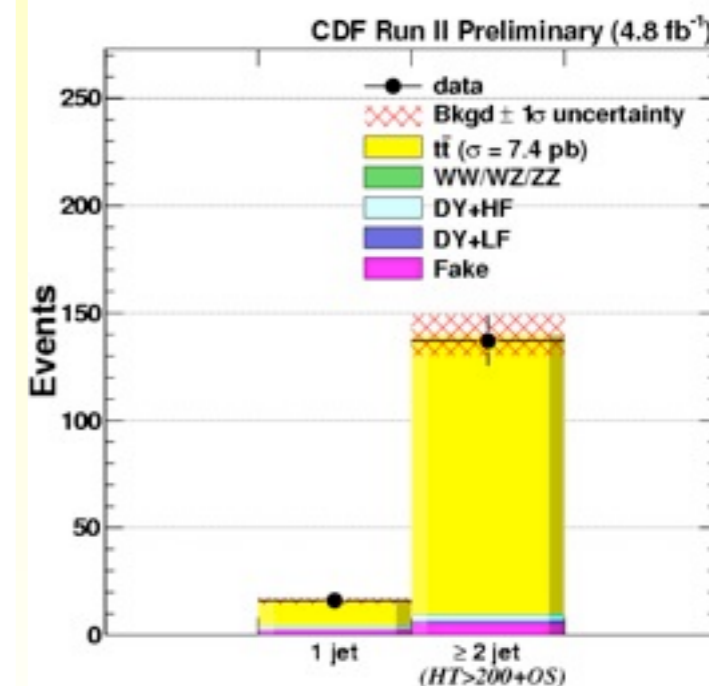
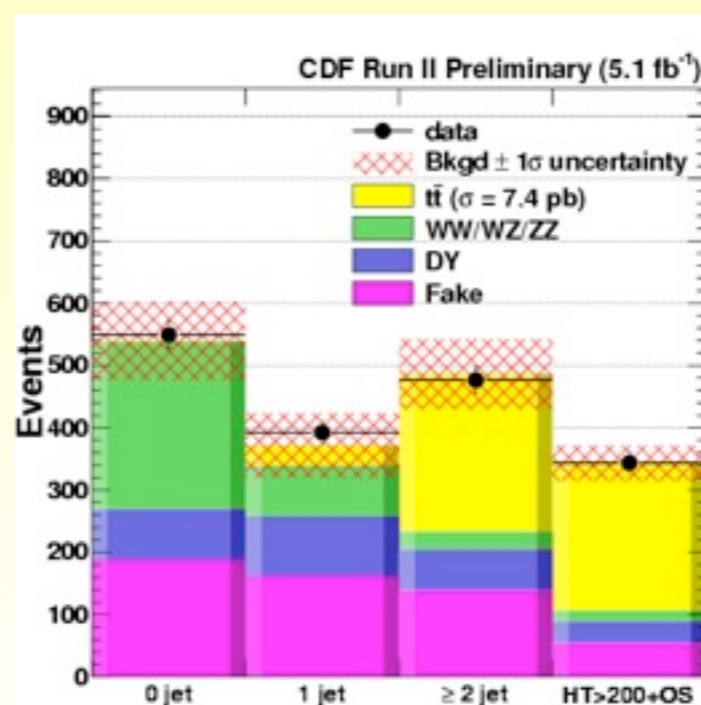
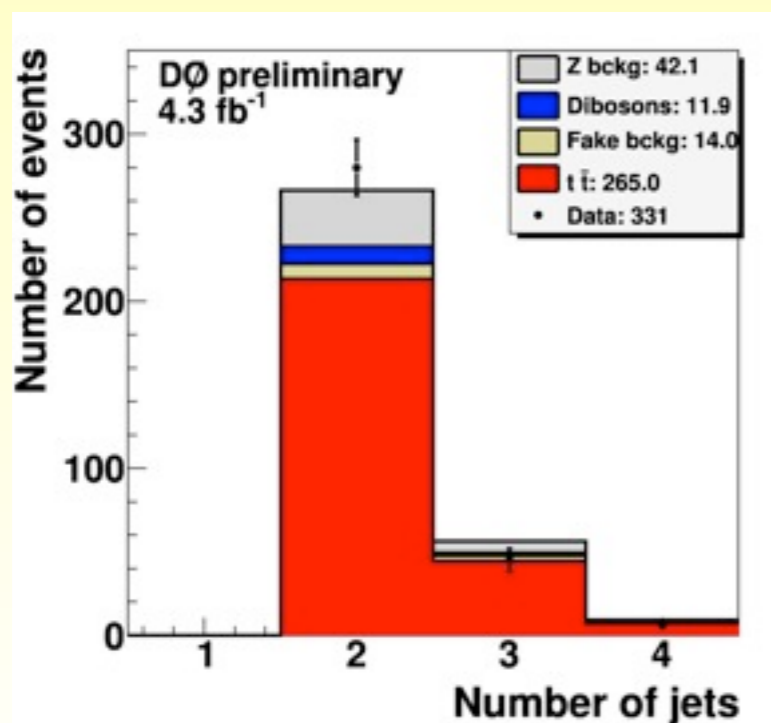
5.3 fb⁻¹

$$\sigma_{t\bar{t}} = 8.4 \pm 0.5 \text{ (stat)} \pm 0.9 \text{ (syst)} \pm 0.7 \text{ (lumi)} \text{ pb.}$$



$$\begin{aligned} \text{topo : } \sigma_{t\bar{t}} &= 7.40 \pm 0.58 \text{ (stat)} \pm 0.63 \text{ (sys)} \pm 0.45 \text{ (lumi)} \text{ pb} \\ \text{b-tag : } \sigma_{t\bar{t}} &= 7.25 \pm 0.66 \text{ (stat)} \pm 0.47 \text{ (sys)} \pm 0.44 \text{ (lumi)} \text{ pb} \end{aligned}$$

Mt = 172.5 GeV

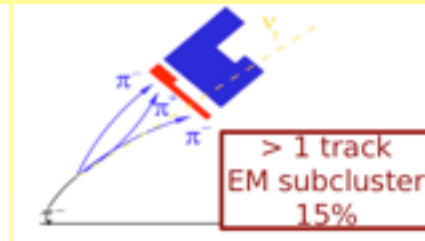
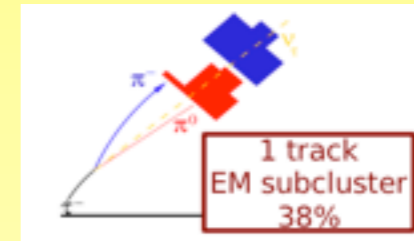




Lepton + τ Cross Section

- τ reconstruction:

- 3 NN depending of the τ decay types to separate from jets faking τ
- 1 additional NN to separate τ type 2 from electron



- main background after b-tagging:

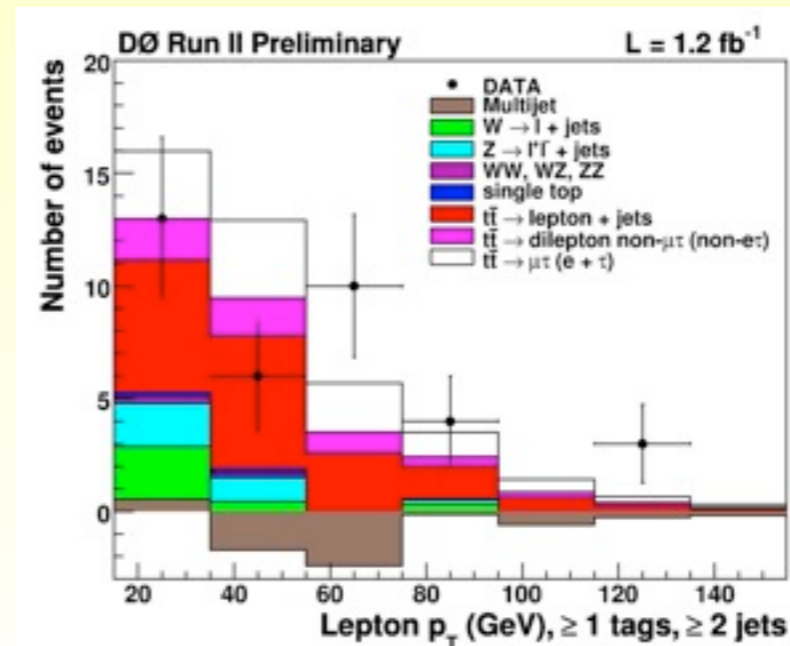
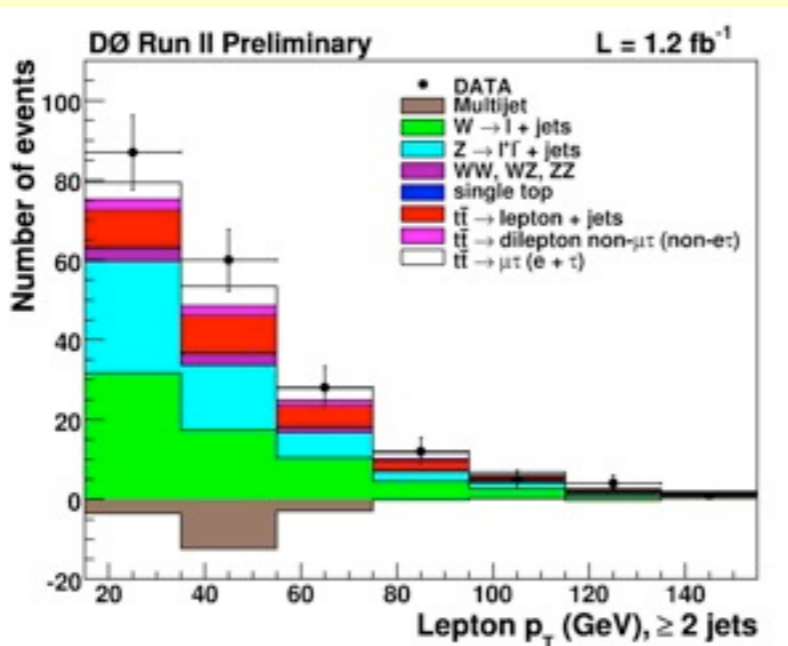
- W+jets (normalized to data), Z+jets, diboson from MC
- Multijets from data (same sign events)

2.2 fb⁻¹

$$\sigma(t\bar{t}) = 7.32_{-1.24}^{+1.34}(\text{stat})_{-1.06}^{+1.20}(\text{syst}) \pm 0.45(\text{lumi}) \text{ pb.}$$

M_t = 175 GeV

	$\mu\tau$ channel		$e\tau$ channel	
	before b-tagging	after b-tagging	before b-tagging	after b-tagging
Multijet	-16.38±6.25	-4.25±1.98	0.05±7.67	0.25±3.19
W → $\ell\nu$ (+jets)	43.07±2.75	3.39±0.23	44.86±3.92	3.08±0.17
Z → $\mu^-\mu^+(e^-e^+)$ (+jets)	19.69±0.73	1.52±0.05	7.51±0.51	0.47±0.03
Z → $\tau^-\tau^+$ (+jets)	10.68±0.60	0.76±0.06	14.81±0.77	0.97±0.04
diboson	4.52±0.48	0.36±0.05	3.70±0.48	0.28±0.04
single top	0.49±0.01	0.25±0.01	0.49±0.01	0.26±0.01
$t\bar{t} \rightarrow \ell$ +jets	11.97±0.18	7.46±0.13	15.61±0.22	9.95±0.16
$t\bar{t} \rightarrow \ell\ell$ +jets non- $\mu\tau_h(e\tau_h)$	6.29±2.39	4.39±0.20	1.52±0.10	1.03±0.09
$t\bar{t} \rightarrow \mu\tau_h(e\tau_h)$ +jets	7.45±0.07	5.24±0.05	7.82±0.07	5.52±0.06
total	87.79±6.91	19.12±2.00	96.28±8.68	21.32±3.20
data	103	19	94	17



MET + Jets Cross Section

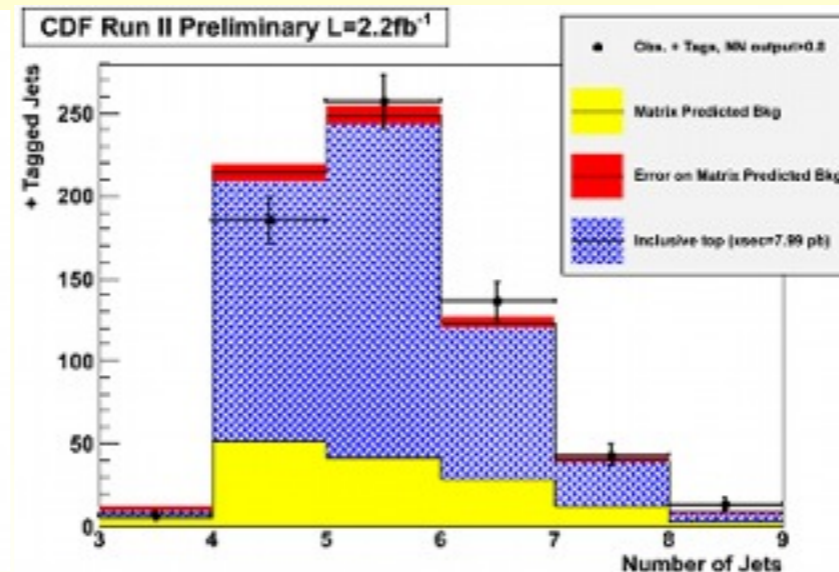
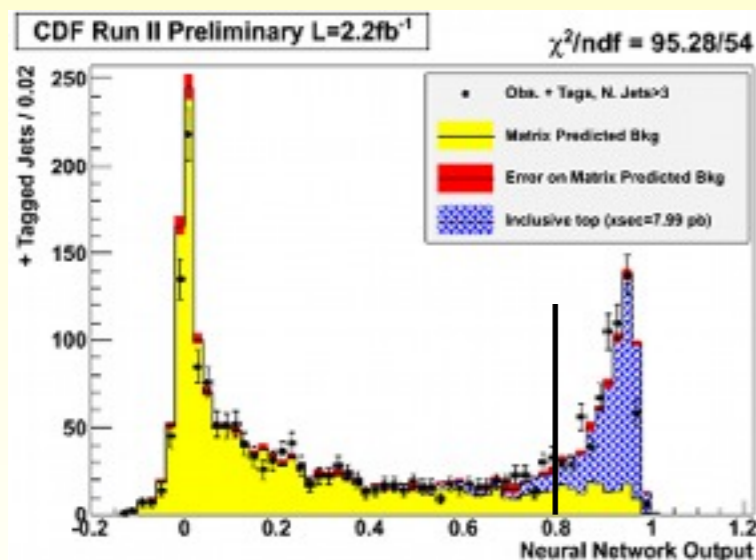
- MET + jets:
 - alternative way to select τ channels: large contribution from $W \rightarrow \tau \nu$
 - complementarity with channels with one identified lepton
- selection:
 - at least 3 strict identified jets
 - at least one b-tagged jet
 - NN trained against background, $NN > 0.8$
- background estimation:
 - b-tag rate/misrate evaluated from data in a 3 jet sample (small signal contamination)

sample composition	Tot.
all hadronic (%)	2.29
e +jets (%)	32.08
μ +jets (%)	22.71
dileptonic (%)	1.45
had. τ +jets (%)	27.73
lep. τ +jets (%)	10.76
$\tau\tau$ (%)	0.77
$e/\mu + \tau$ (%)	2.16



$$\sigma_{t\bar{t}} = 7.99 \pm 0.55 \text{ (stat)} \pm 0.76 \text{ (syst)} \pm 0.46 \text{ (lumi)} \text{ pb}$$

$M_t = 172.5 \text{ GeV}$





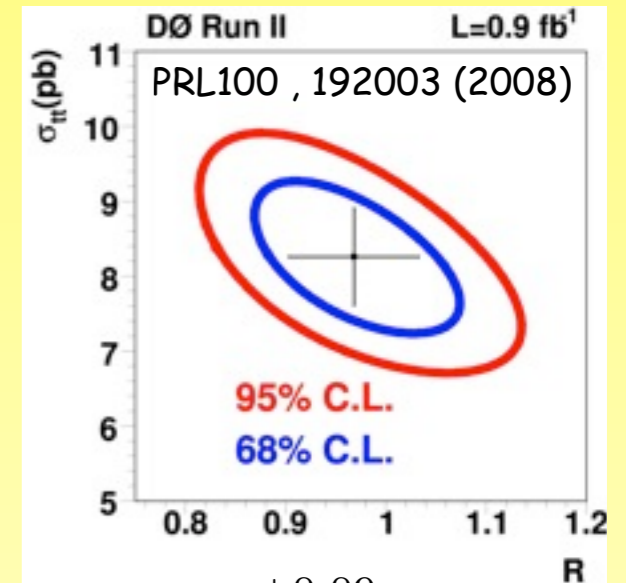
Cross Section Ratio and Charged Higgs Searches

- cross section with different number of b-tag jets:
 - ℓ jets with 0, 1 or 2 b-tag jets: $R = \frac{B(t \rightarrow Wb)}{B(t \rightarrow Wq)}$
- cross section in different channels sensitive to new physics:
 - number of events in ℓ jets, $\ell\ell$ and $\ell\tau$:

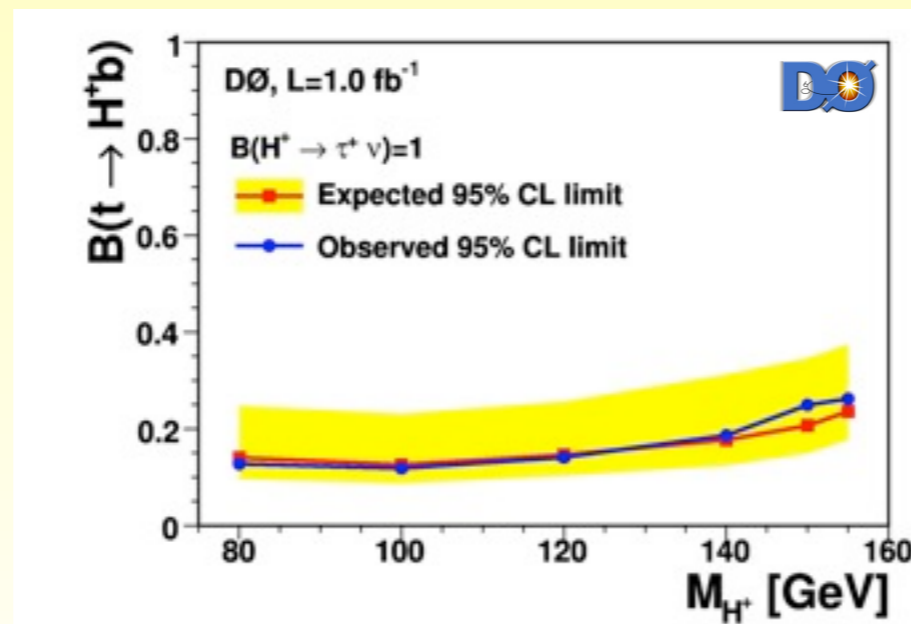
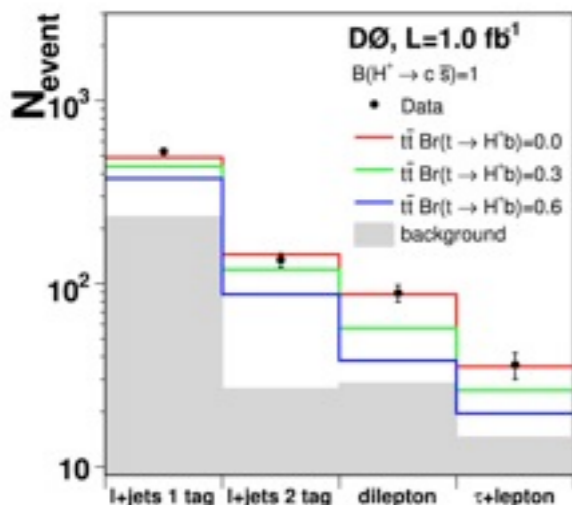
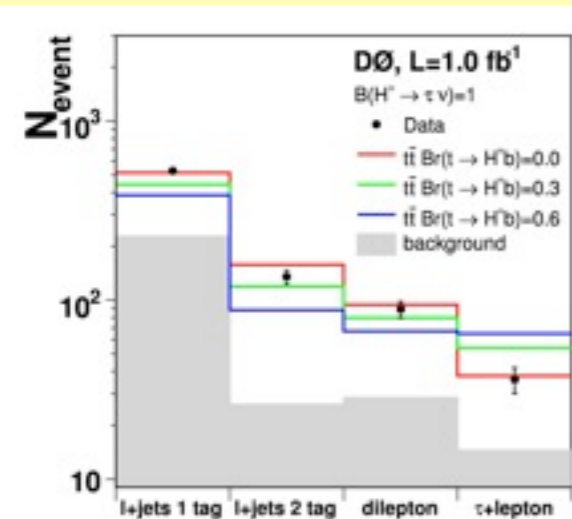
in SM extension with extended Higgs sector

(like MSSM or HDM) $t \rightarrow H^+b$ can compete with $t \rightarrow Wb$

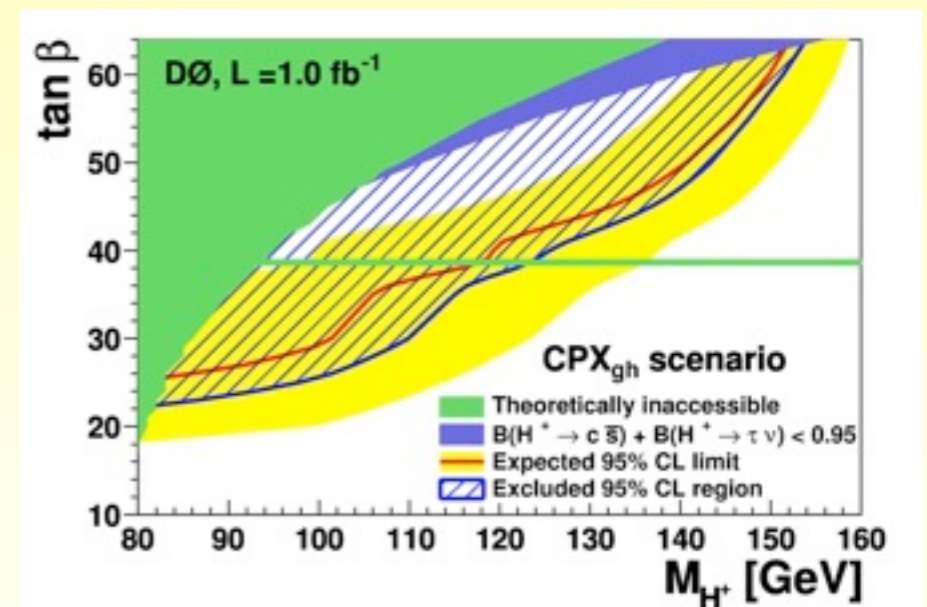
Search here for $H^+ \rightarrow \tau \nu$ or $c\bar{s}$



$$R = 0.96_{-0.08}^{+0.09} (\text{stat} + \text{sys})$$

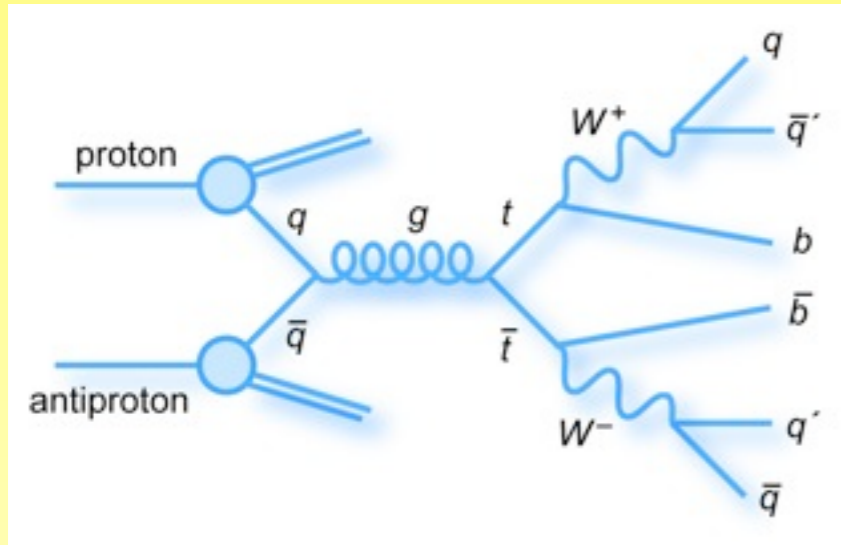


interpretation in the CPX scenario
(strangephilic MSSM Higgs)
Eur.Phys.J C66 261-269,2010

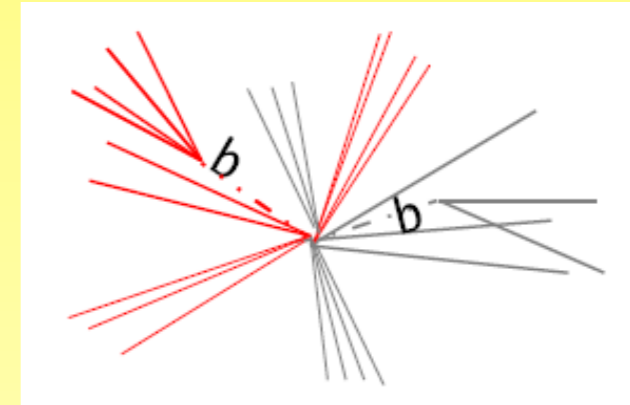
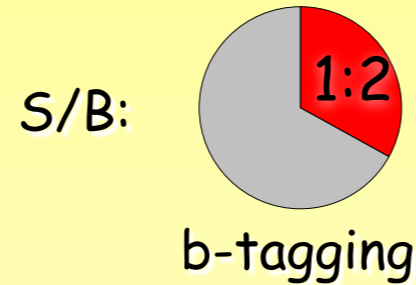


PLB 682, 278 (2009)

All Hadronic Channel



- signature:
 - 6 jets (2 b-jets)



- main background:

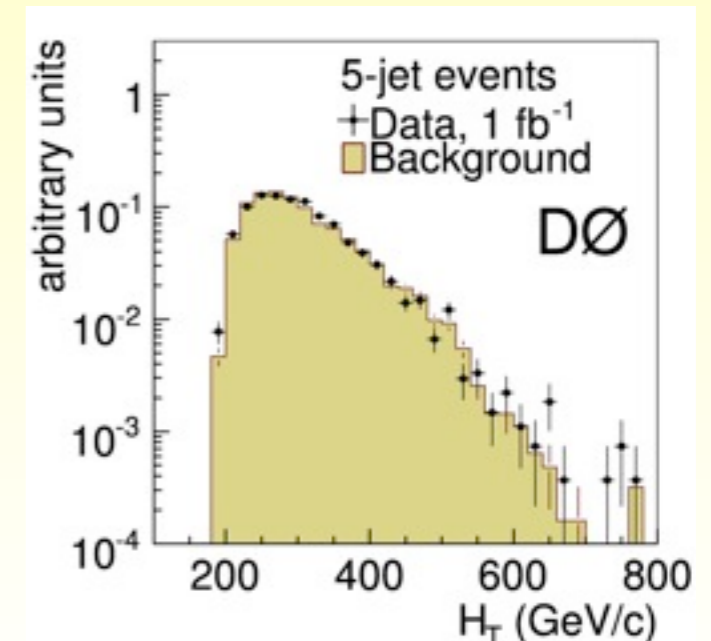
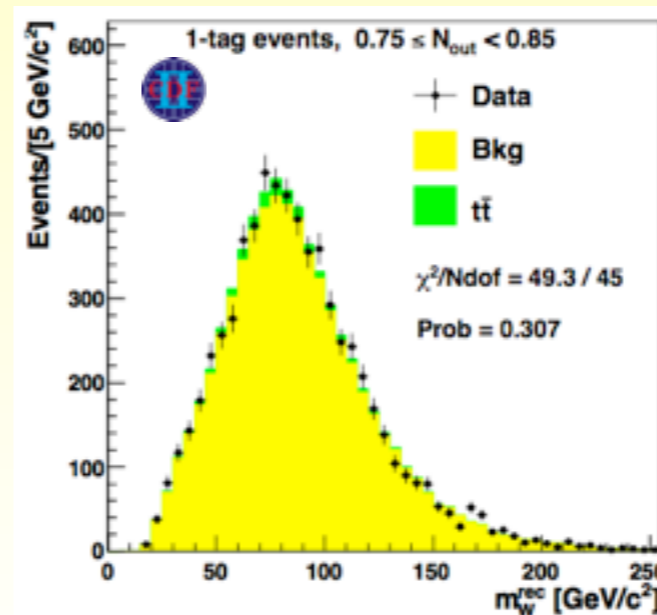
- Multijets: ~ cross section 3 orders of magnitude
 - estimated from data
 - b-tagging essential

CDF: tag rate per jet evaluated using 4 jets events
 D0: adding 1 jet to 5 jets events after 2 b-tags

signal sample:

CDF: $6 \leq N_{\text{jets}} \leq 8$

D0: $6 \leq N_{\text{jets}}$





All Hadronic Cross Section



- built a discriminant:
 - CDF: NN, DØ: Likelihood
 - input variables: H_t , invariant masses, centrality, ...

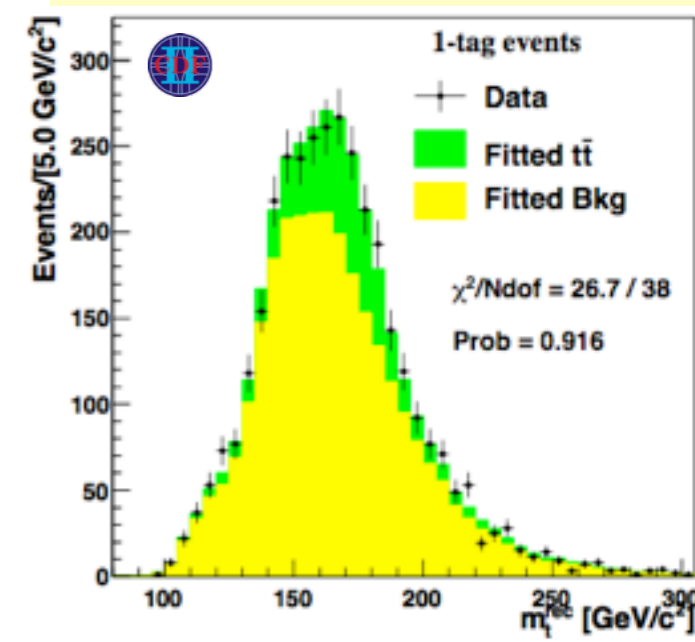
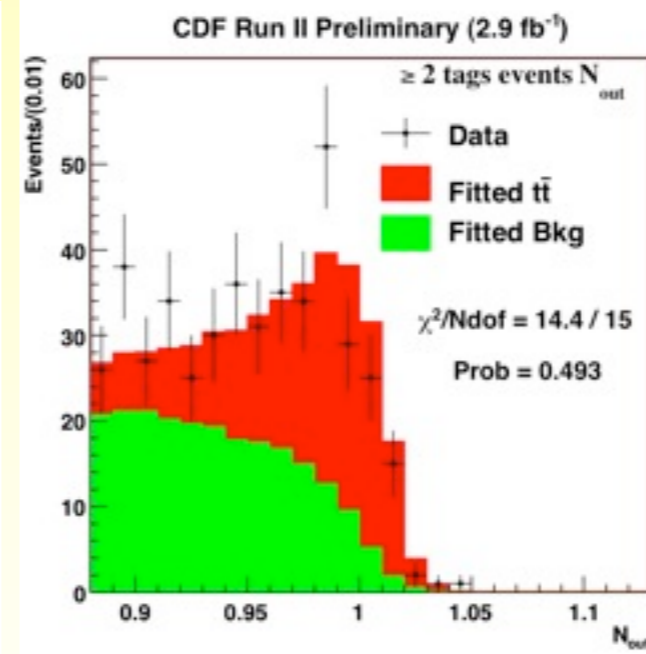
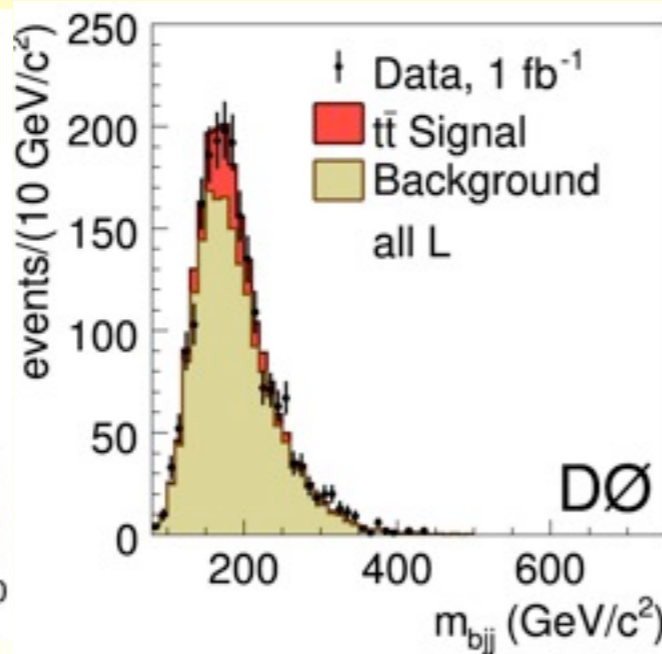
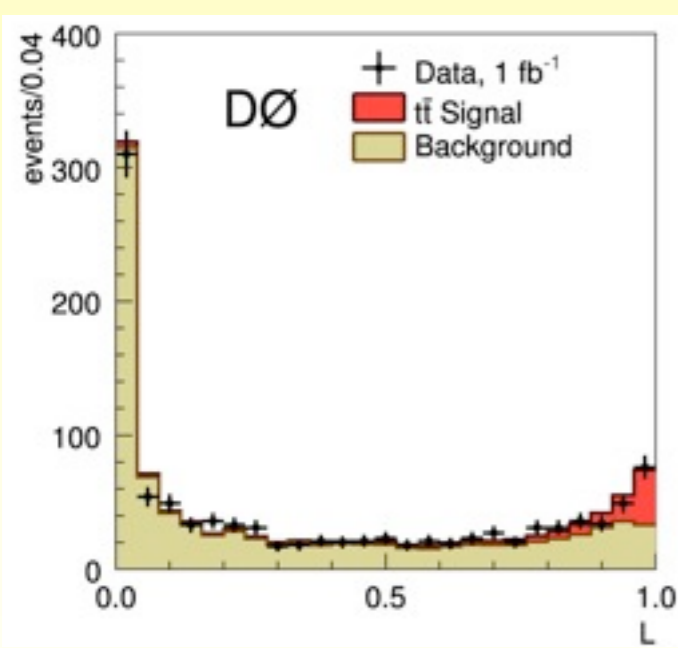
submitted to PRD

$$\sigma_{t\bar{t}}^{175 \text{ GeV}/c^2} = 6.9 \pm 1.3 \text{ (stat)} \pm 1.4 \text{ (sys)} \pm 0.4 \text{ (lum)} \text{ pb}$$

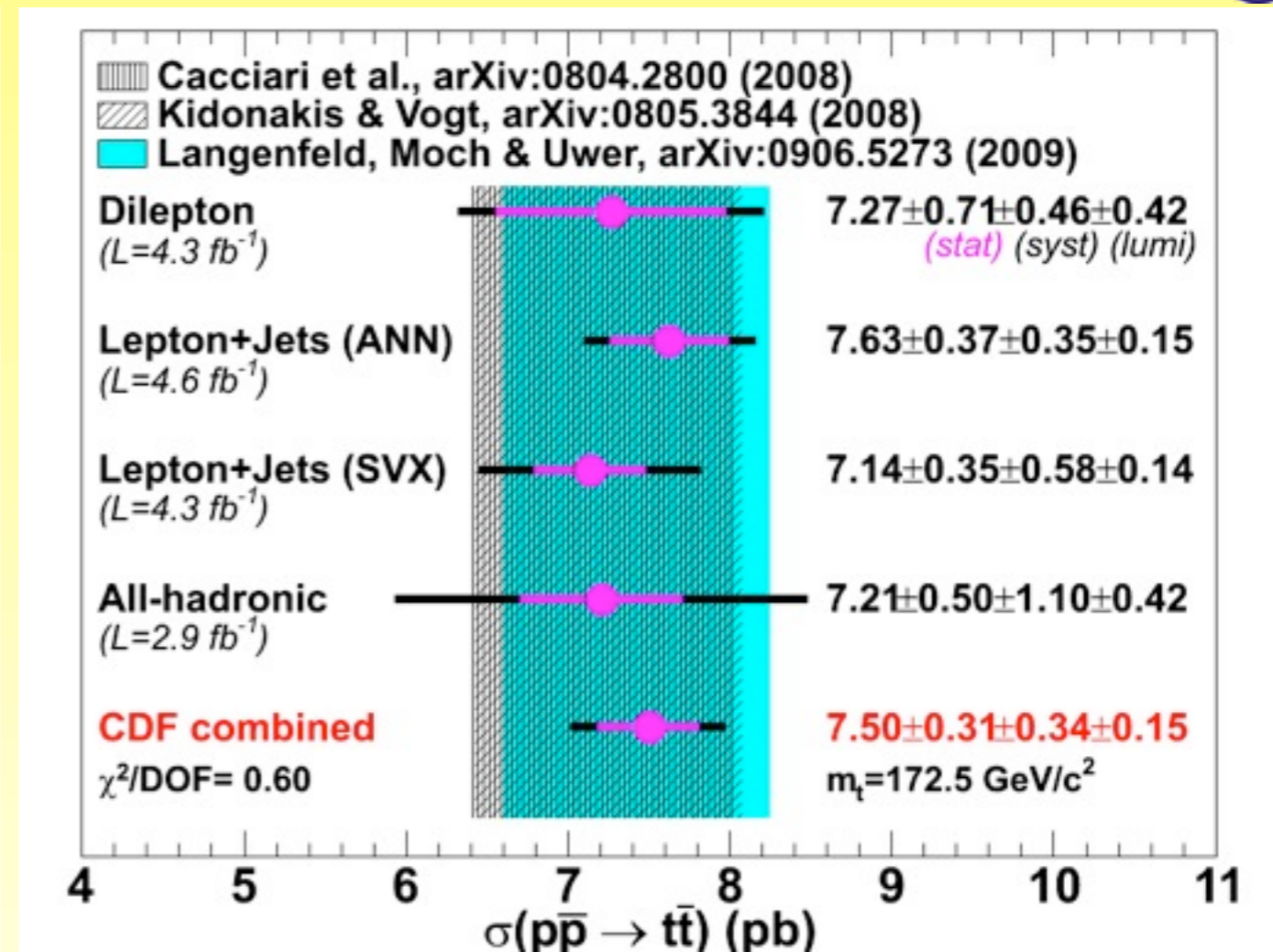
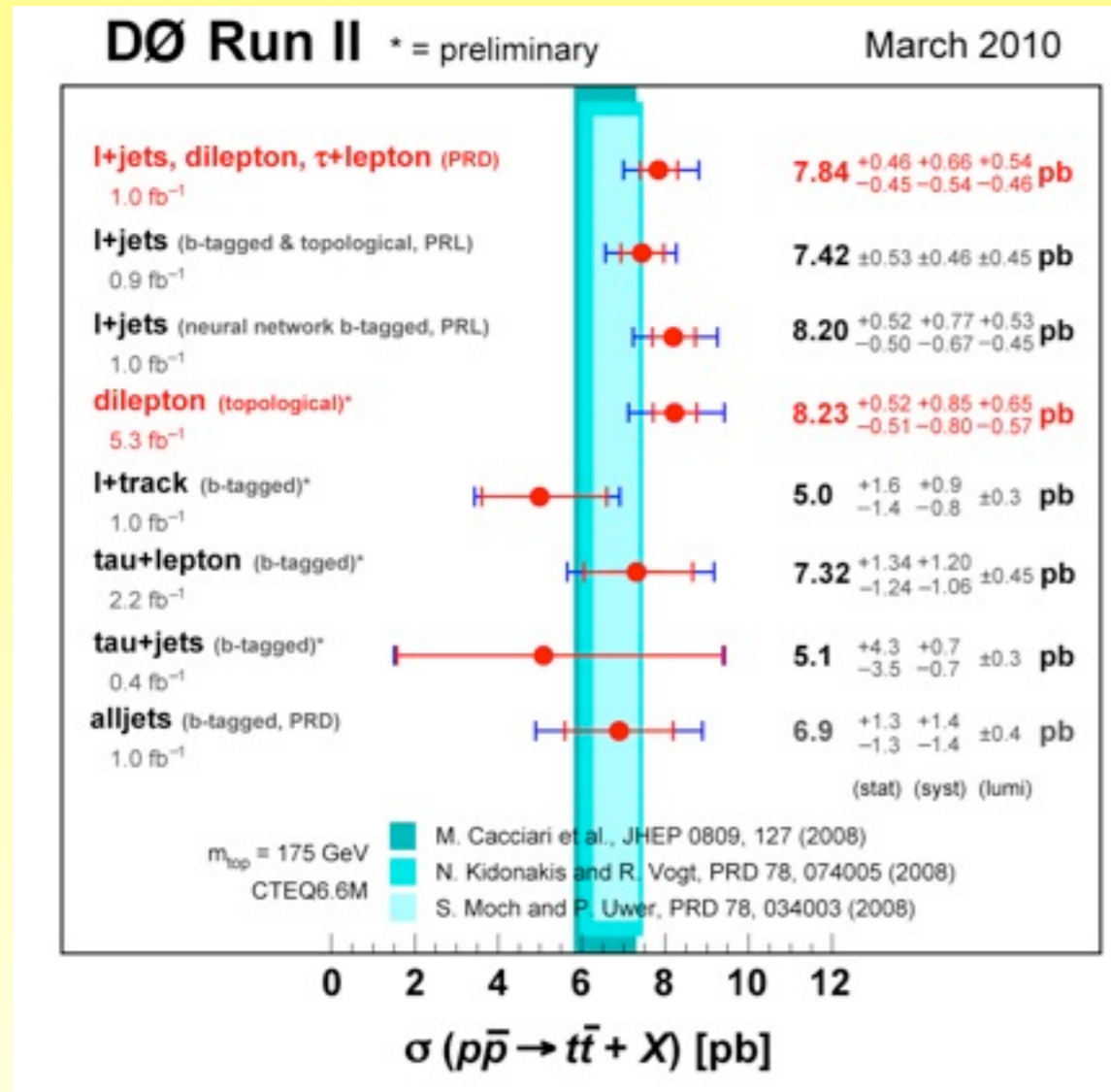
PRD 81, 052011 (2010)

$$\sigma_{t\bar{t}} = 7.2 \pm 0.5 \text{ (stat)} \pm 1.0 \text{ (syst)} \pm 0.4 \text{ (lum)} \text{ pb}$$

$M_t = 175 \text{ GeV}$



Summary of the Tevatron $t\bar{t}$ Cross Section



- measurements in all the possible channels
- consistent with SM expectation
- CDF/DØ Combination:
 - work in progress based on the example of the mass combination



$t\bar{t}$ + jets Cross Section

- test of QCD prediction, sensitive to NLO effects, different FB asymmetry than inclusive $t\bar{t}$
- lepton + jets selection:
 - W+jets: normalized to data before tagging
 - Multijets: estimated by a fit at the low MET
- simultaneous fit of $t\bar{t}+0j$ and $t\bar{t}+1j$



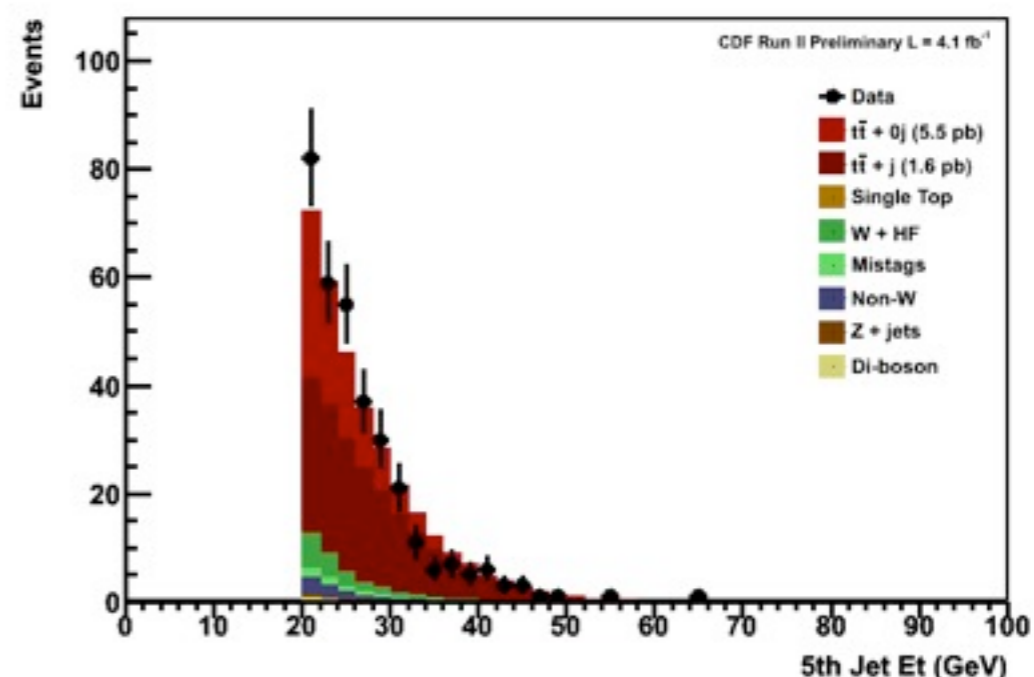
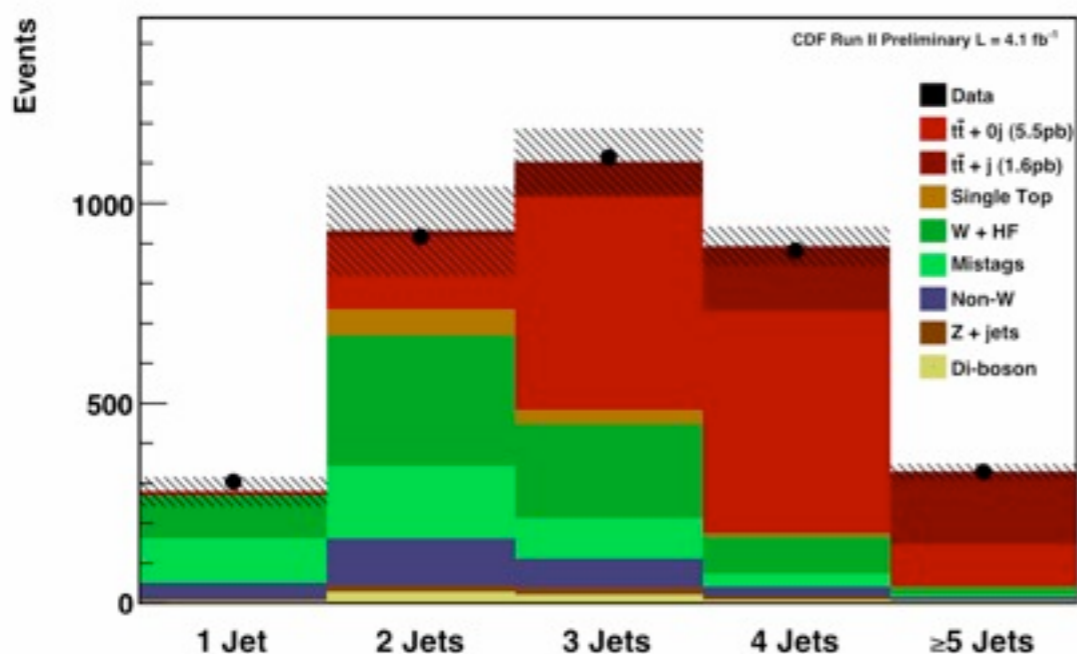
$$\sigma_{t\bar{t}jets} = 1.6 \pm 0.2(\text{stat}) \pm 0.5(\text{sys}) \text{ pb}$$

$M_t = 175 \text{ GeV}$

$$\text{SM} : \sigma_{t\bar{t}jets} = 1.79^{+0.16}_{-0.31} \text{ pb}$$

$M_t = 174 \text{ GeV}$, EPJ C59 625 (2009)

Systematic	$\Delta\sigma_{0j}$ pb	$\Delta\sigma_{0j}/\sigma_{0j}$ %	$\Delta\sigma_{+j}$	$\Delta\sigma_{+j}/\sigma_{+j}$ %
JES	0.27	4.9	0.48 pb	30.2
BTag SF	0.25	4.6	0.07	4.6
C Tag SF	0.01	0.2	0.01	0.4
Mistag Matrix	0.01	0.2	0.01	0.6
Heavy Flavor Correction	0.36	6.7	0.06	3.4
Luminosity	0.32	5.6	0.10	6.1
QCD Fraction	0.01	0.2	0.01	0.4
ISF/FSR	0.11	2.1	0.07	3.3
MC Generator	0.19	3.5	0.04	2.3
Trigger Eff	0.03	0.6	0.01	0.6
PDF	0.06	1.0	0.01	1.0
Total	0.65 pb	11.8 %	0.47 pb	36.5 %







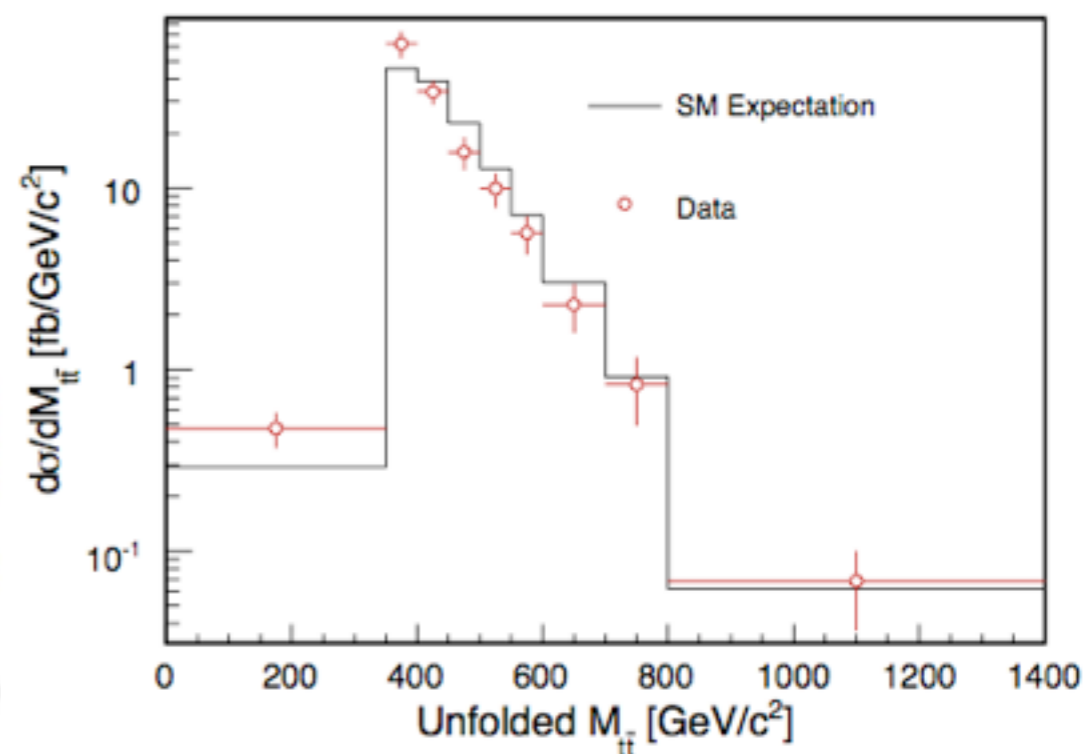
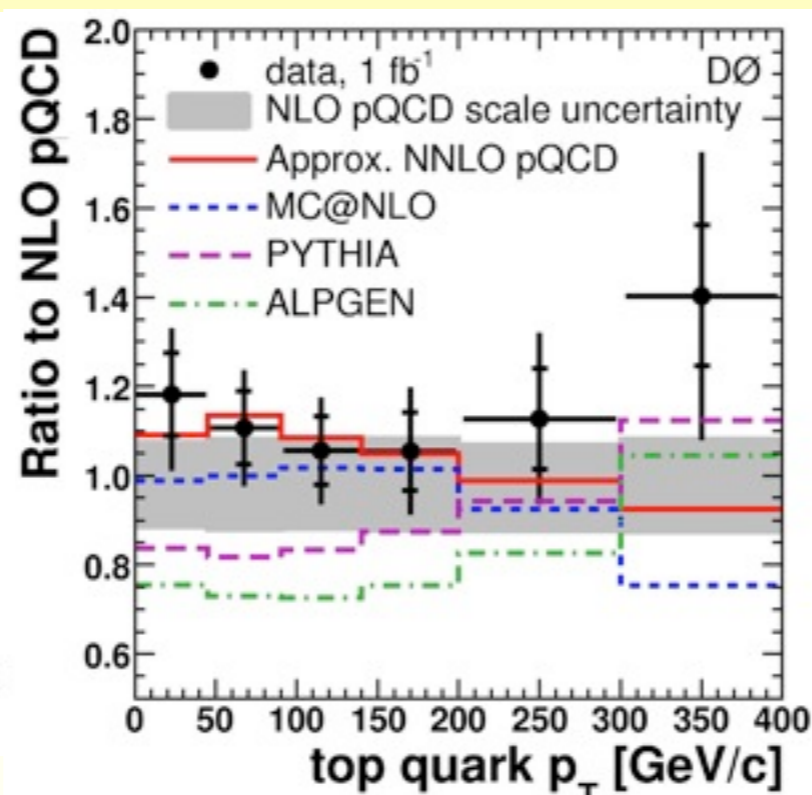
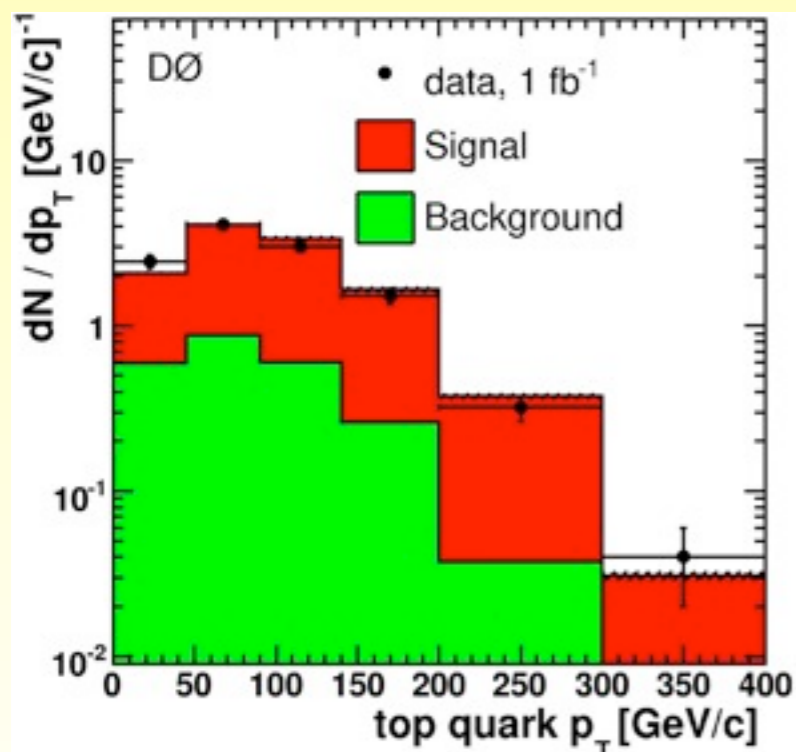
Differential Top p_T and $M_{t\bar{t}}$ Cross Sections



- New physics can distort differential top spectra:
 - deeper investigation than inclusive cross sections
- lepton + jets selection
 - full reconstruction of the $t\bar{t}$ events
 - subtract background contribution
 - unfold distributions from detector effects
- no deviation from SM expectation observed in data

submitted to PLB 

PRL 102, 222003 (2009) 





Conclusion

- the Tevatron experiments have measured the $t\bar{t}$ cross sections in all possible top decay channels
 - well understood $t\bar{t}$ samples
 - a lot of the measurements are now systematics limited
 - precision $\sim 6.5\%$ using $t\bar{t}/Z$ cross section ratio
 - allow to search for many deviations from SM expectations
- expect soon a Tevatron $t\bar{t}$ cross section combination
- will continue to scrutinize the top sector with more than 7 fb^{-1} on tape
 - decay channels with low statistics
 - cross section ratio, differential cross sections

See following talks for other Tevatron top properties results

