

Cosmic ν 's as a Probe of Fundamental Physics

VILLUM FONDEN



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The Elusive Neutrino

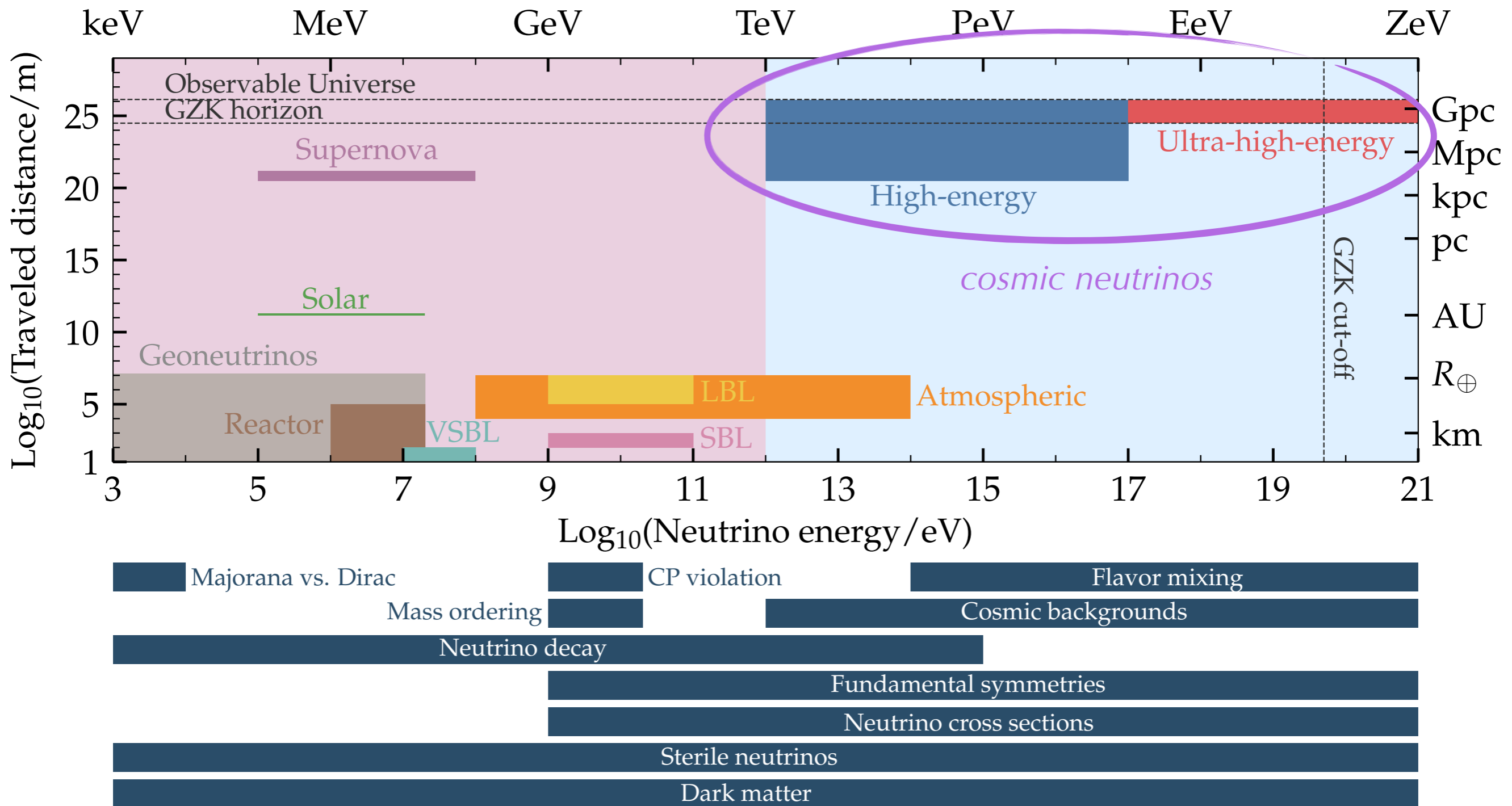
- **small masses** with uncertain origin and scale
- **large mixing** between flavour and mass states
- potential source of **CP violation** (*leptogenesis?*)
- **Dirac or Majorana** fermions
- susceptible to **beyond-the-SM** effects

Standard Model of Particle Physics

1968: SLAC u up quark	1974: Brookhaven & SLAC c charm quark	1995: Fermilab t top quark	1979: DESY g gluon
1968: SLAC d down quark	1947: Manchester University s strange quark	1977: Fermilab b bottom quark	1923: Washington University* γ photon
1956: Savannah River Plant ν_e electron neutrino	1962: Brookhaven ν_μ muon neutrino	2000: Fermilab ν_τ tau neutrino	1983: CERN W W boson
1897: Cavendish Laboratory e electron	1937: Caltech and Harvard μ muon	1976: SLAC τ tau	1983: CERN Z Z boson

(+ Higgs boson)

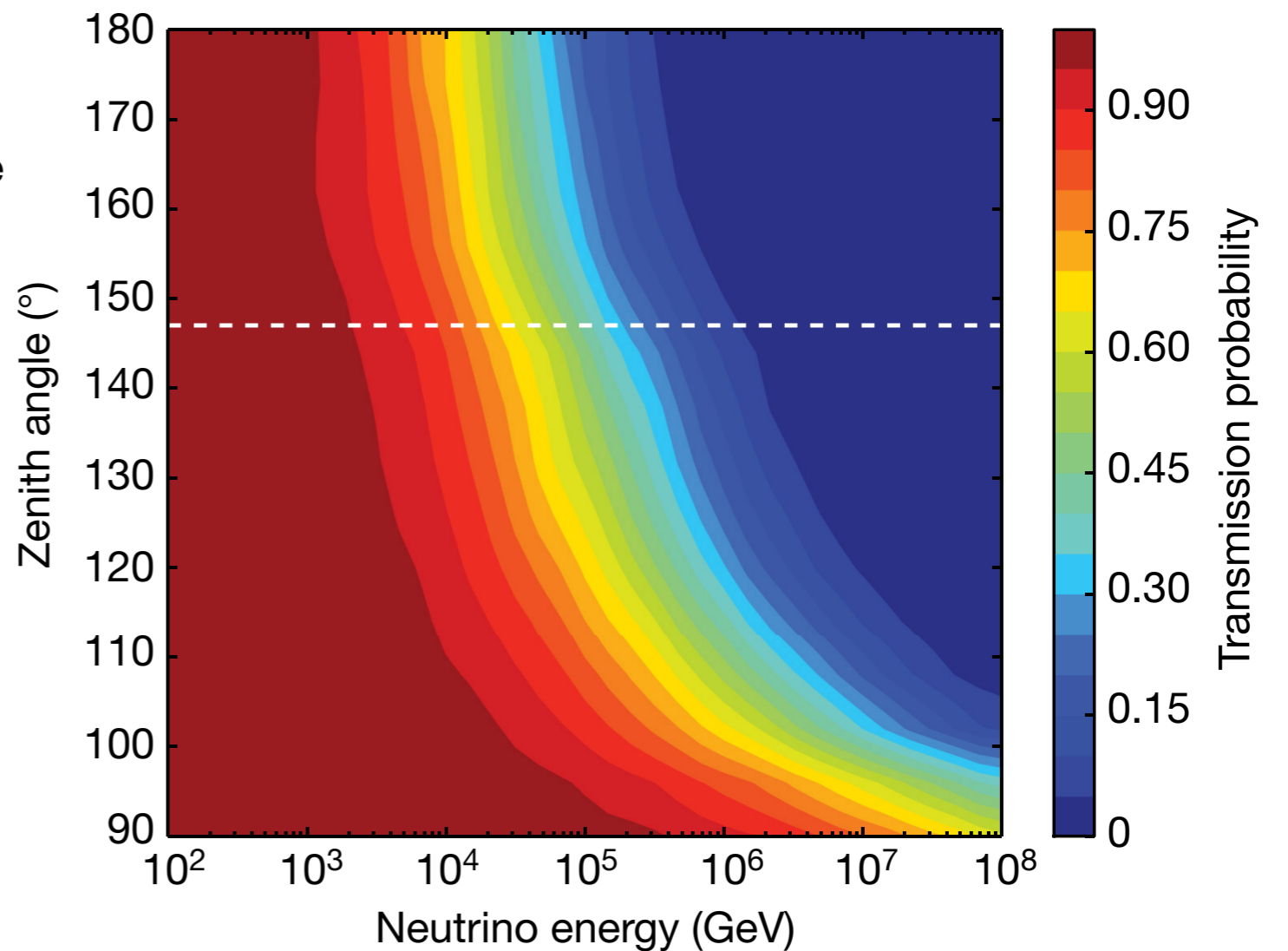
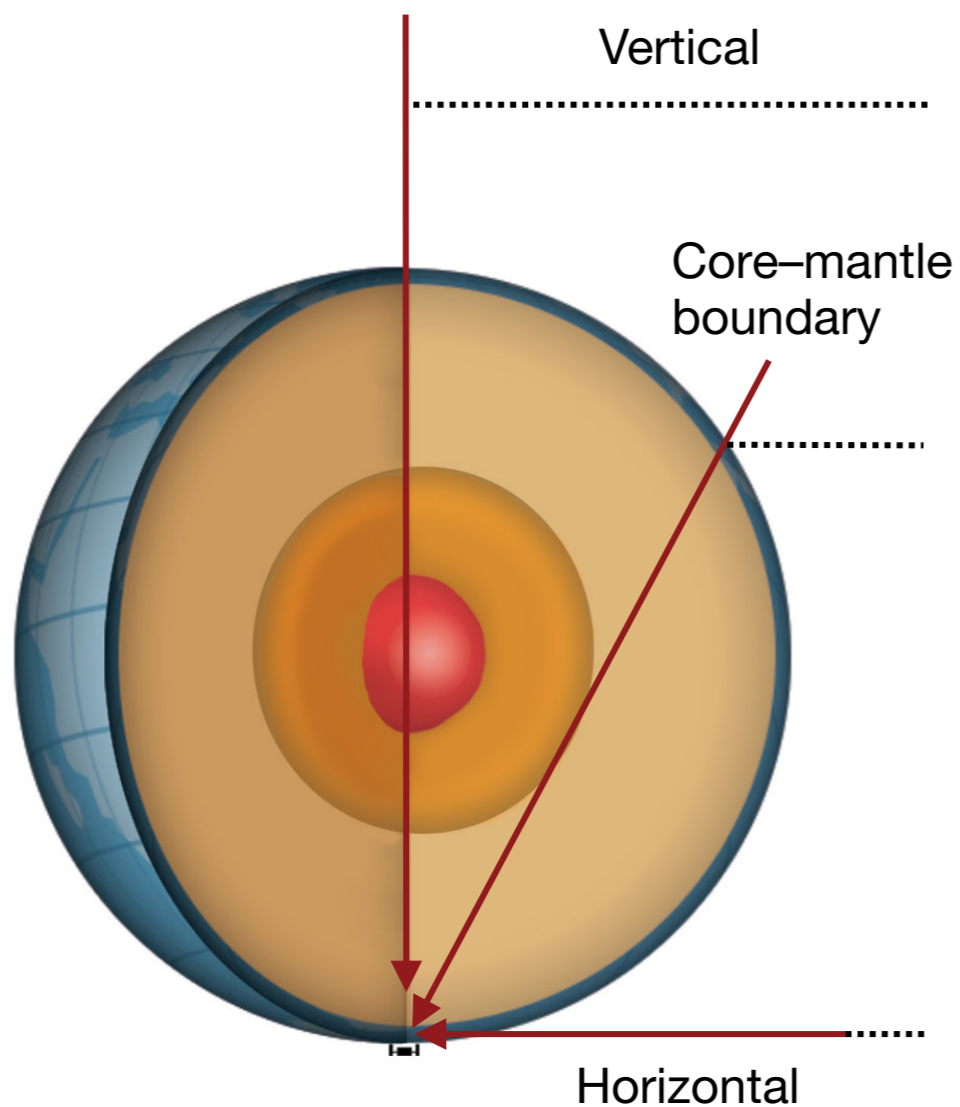
Probe of Fundamental Physics



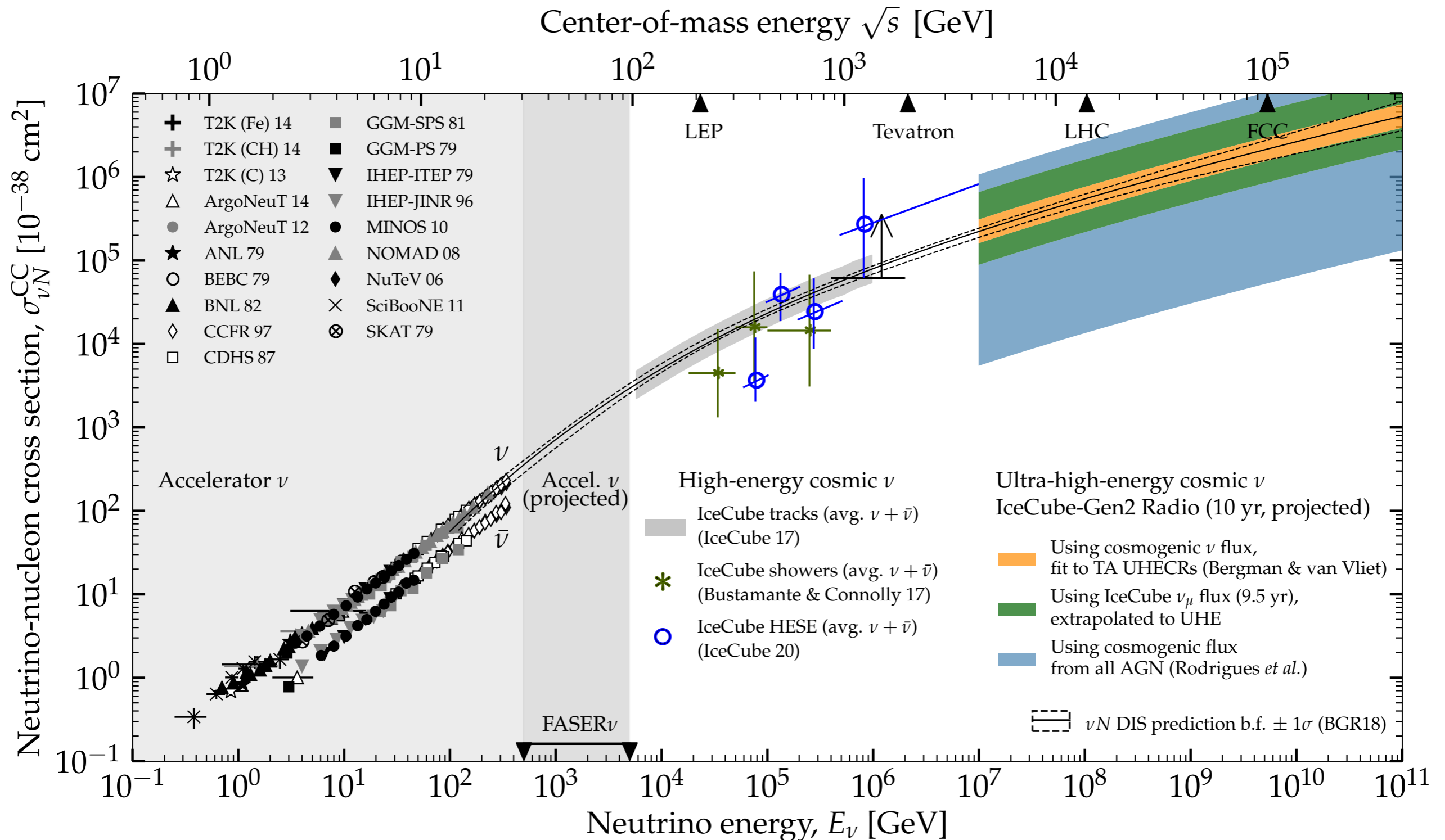
[Ackermann, MA, Anchordoqui, Bustamante+ **Bull.Am.Astron.Soc.** 51 (2019)]

Neutrino Cross Section

$$N_{\text{events}}(\theta, E_\nu) \propto \sigma_{\nu N}(E_\nu) \exp\left(-\frac{\sigma_{\nu N}(E_\nu)}{m_p} \int d\ell \rho_\oplus(r_{\text{IC}} + \ell \hat{\mathbf{n}}(\theta))\right)$$



Neutrino Cross Section



[IceCube-Gen2 Technical Design Report: icecube-gen2.wisc.edu/science/publications/tdr/]

Neutrino Mixing



Superpositions of mass eigenstates!

3 **flavour eigenstates** $|\nu_\alpha\rangle$ with greek index ($\alpha = e, \mu, \tau$)

3 **mass eigenstates** $|\nu_i\rangle$ with roman index ($i = 1, 2, 3$)

Mixing is parametrized by unitary mixing matrix U :

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle$$

Two-Flavour Neutrino Oscillation

- Considering only two flavour oscillations (e.g. $\nu_\mu \leftrightarrow \nu_\tau$)

$$P_{\nu_\beta \rightarrow \nu_\alpha}(\ell) \simeq \sin^2(2\theta) \sin^2\left(\frac{(m_2^2 - m_1^2)\ell}{4E_\nu}\right)$$

- Similarly, the muon neutrino **survival probability** is given as:

$$P_{\nu_\beta \rightarrow \nu_\beta}(\ell) = 1 - P_{\nu_\beta \rightarrow \nu_\alpha}(\ell)$$

- Oscillation phase depends on **mass-squared difference**:

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

- Can be expressed as:

$$\frac{\Delta m_{ij}^2 \ell}{4E_\nu} \simeq 1.27 \left(\frac{\Delta m_{ij}^2}{\text{eV}^2}\right) \left(\frac{\ell}{\text{km}}\right) \left(\frac{E_\nu}{\text{GeV}}\right)^{-1}$$

Oscillation Probes

Oscillation measurement are based on **reactor, solar, accelerator and atmospheric neutrinos** looking for the **appearance and disappearance**.

Source	Type of ν	\bar{E} [MeV]	L [km]	$\min(\Delta m^2)$ [eV ²]
Reactor	$\bar{\nu}_e$	~ 1	1	$\sim 10^{-3}$
Reactor	$\bar{\nu}_e$	~ 1	100	$\sim 10^{-5}$
Accelerator	$\nu_\mu, \bar{\nu}_\mu$	$\sim 10^3$	1	~ 1
Accelerator	$\nu_\mu, \bar{\nu}_\mu$	$\sim 10^3$	1000	$\sim 10^{-3}$
Atmospheric ν 's	$\nu_{\mu,e}, \bar{\nu}_{\mu,e}$	$\sim 10^3$	10^4	$\sim 10^{-4}$
Sun	ν_e	~ 1	1.5×10^8	$\sim 10^{-11}$

(source: pdg.lbl.gov)

In practice, the destructive interference from the limited energy resolution of the detector or size of the neutrino source, require L/\bar{E} to lie within the range of the first few oscillations.

Neutrino Mixing

Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\frac{\alpha_1}{2}} & 0 & 0 \\ 0 & e^{i\frac{\alpha_2}{2}} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

"atmospheric"
mixing

\mathbb{CP} Dirac phase
 $\propto \sin \theta_{13}$

"solar"
mixing

\mathbb{CP} Majorana
phases

(notation: $c_{ij} \equiv \cos \theta_{ij}$ & $s_{ij} \equiv \sin \theta_{ij}$ & $\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$)

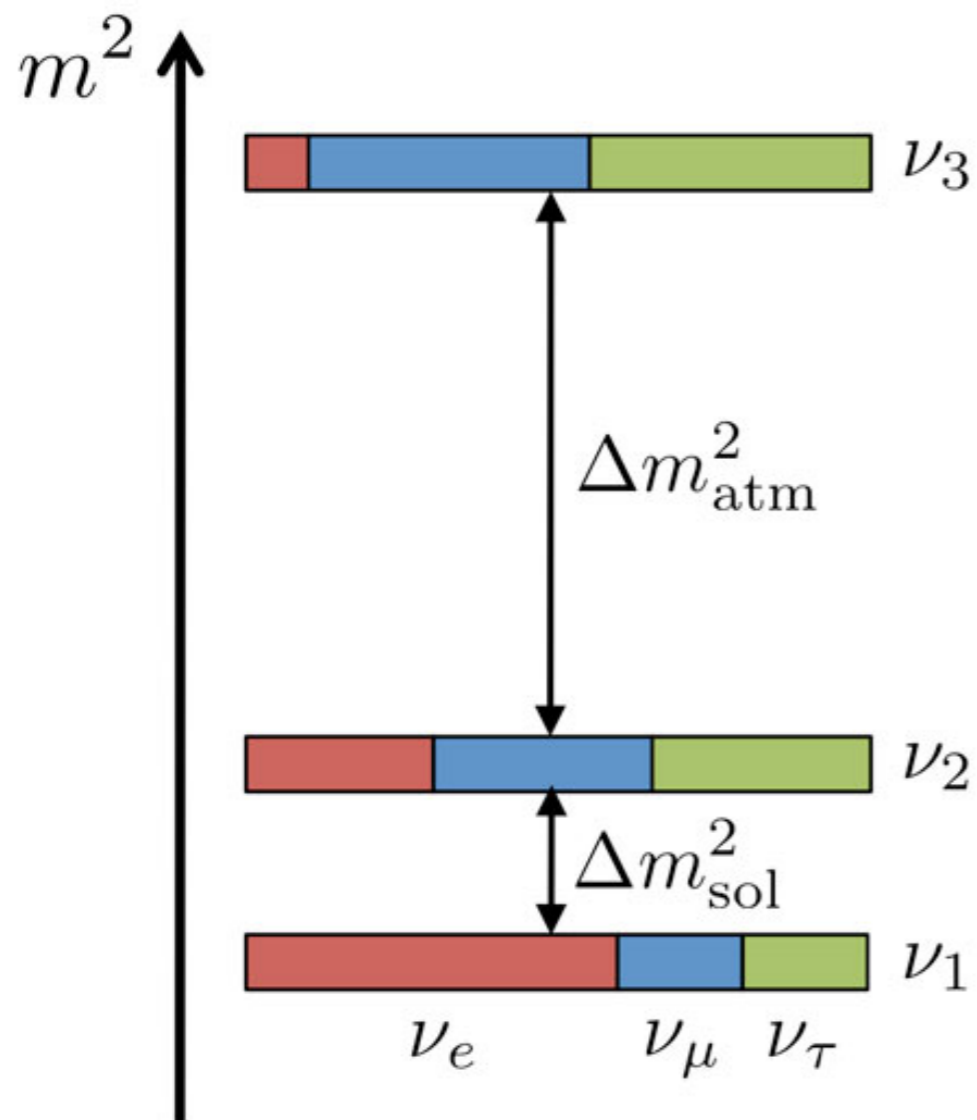
best-fit values (NuFIT 5.2):

$$\sin^2 \theta_{12} \simeq 0.303 \quad \sin^2 \theta_{13} \simeq 0.022 \quad \sin^2 \theta_{23} \simeq 0.57$$

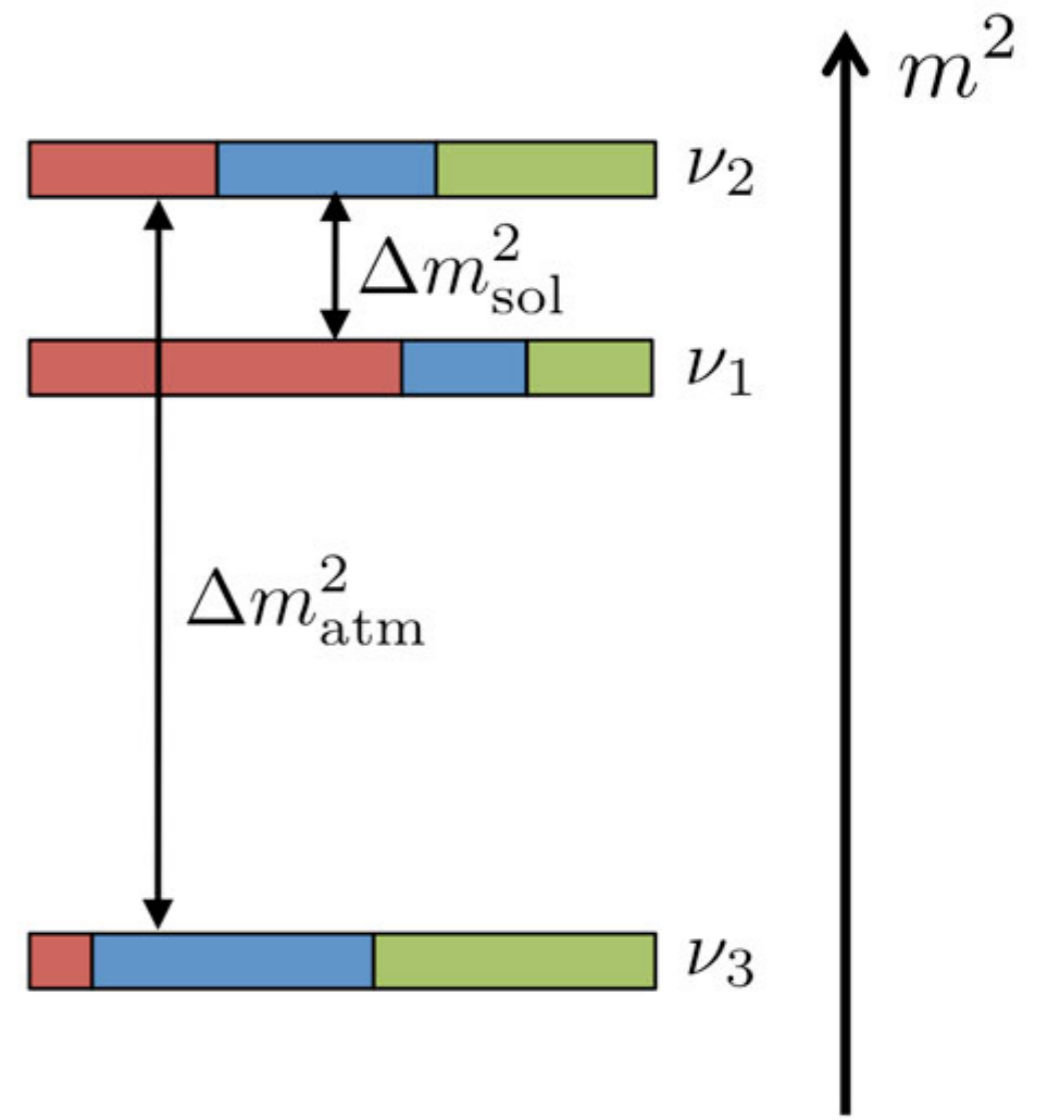
$$\Delta m_{21}^2 \simeq 7.41 \times 10^{-5} \text{eV}^2 \quad \Delta m_{32}^2 \simeq \pm 2.5 \times 10^{-3} \text{eV}^2$$

Neutrino Mass Ordering

normal hierarchy (NH)



inverted hierarchy (IH)

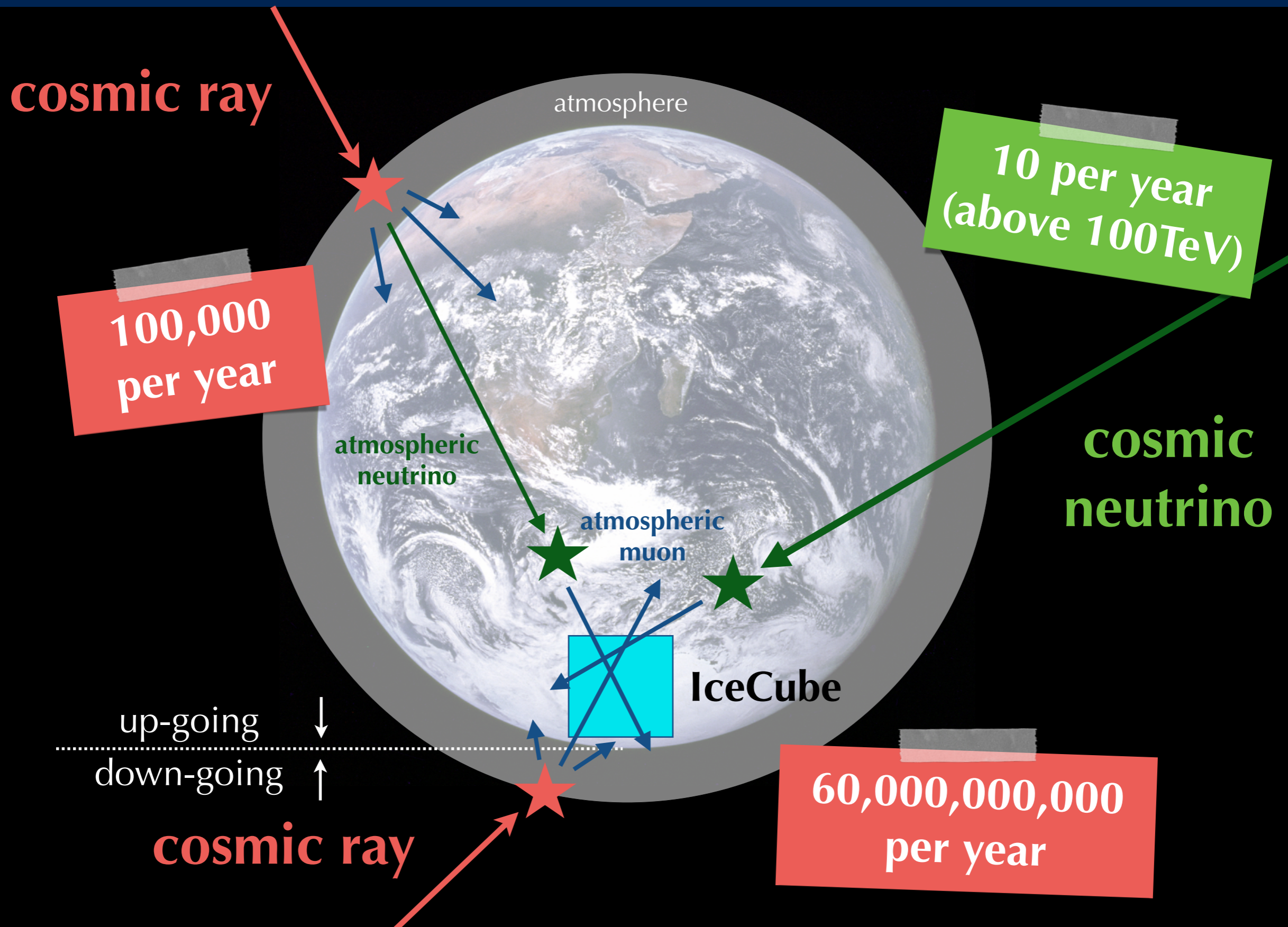


?

(source: neutrinos.fnal.gov)

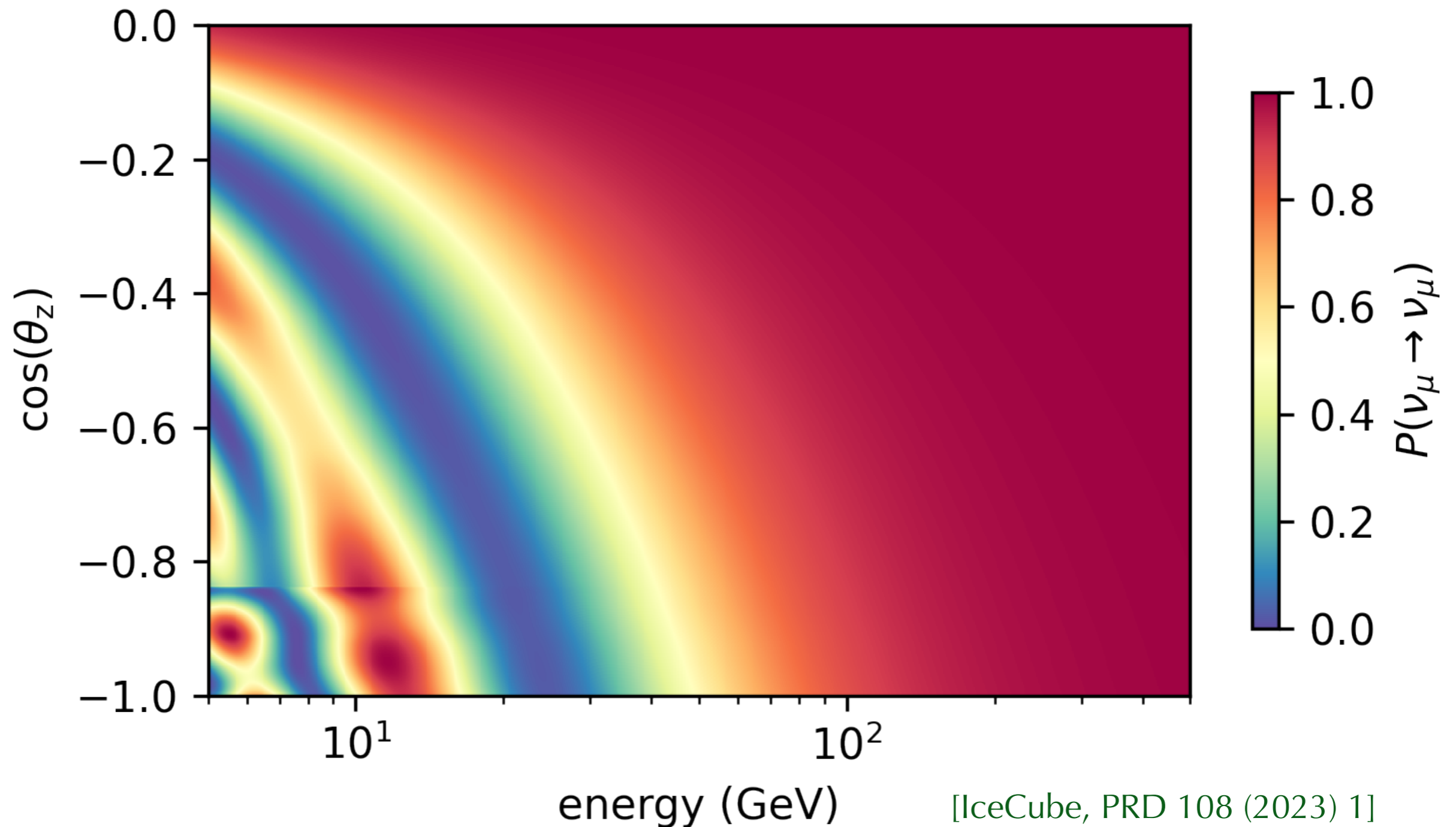
colours show relative contribution of ν_e , ν_μ and ν_τ

Neutrino Selection



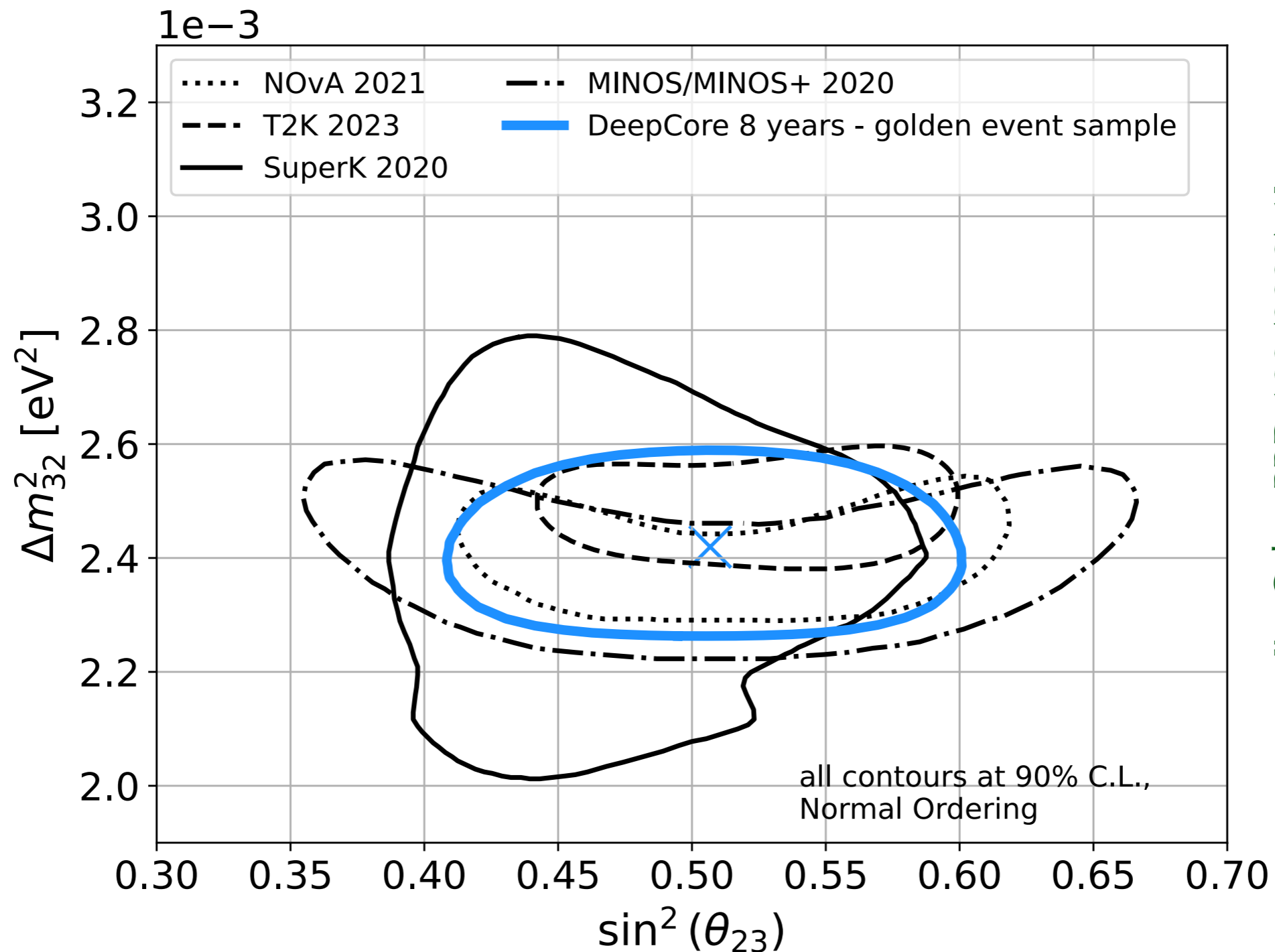
Atmospheric Neutrino Oscillation

Atmospheric **muon neutrino survival probability**
as a function of energy and zenith angle θ_Z



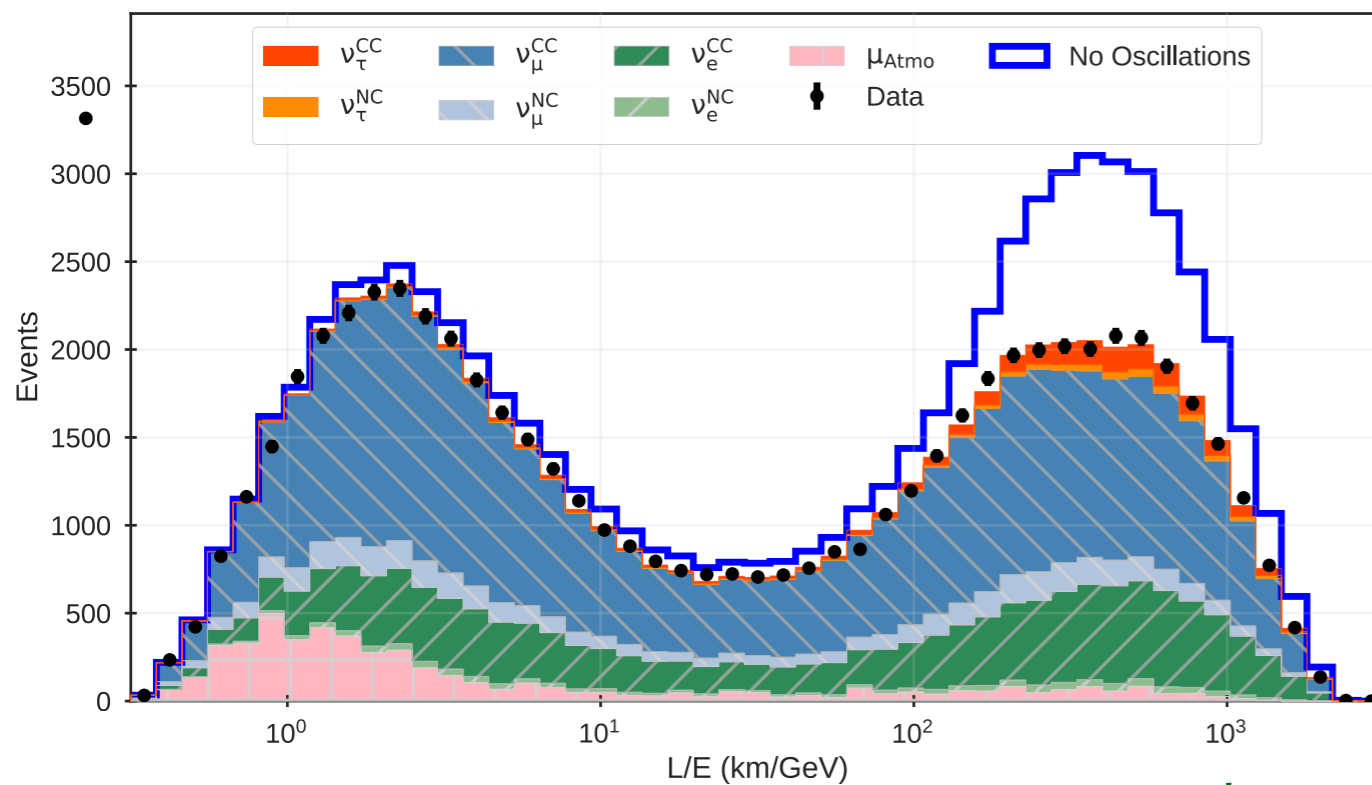
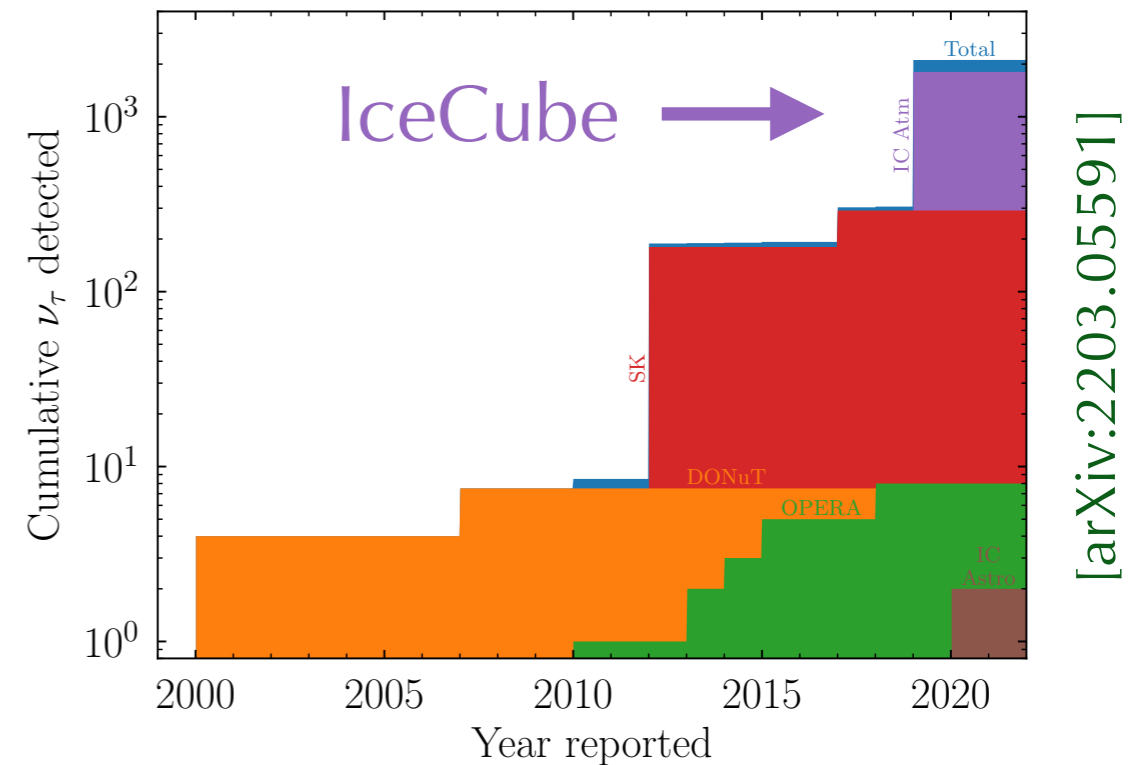
Atmospheric Neutrino Oscillation

90% C.L. allowed region for atmospheric neutrino oscillation parameters

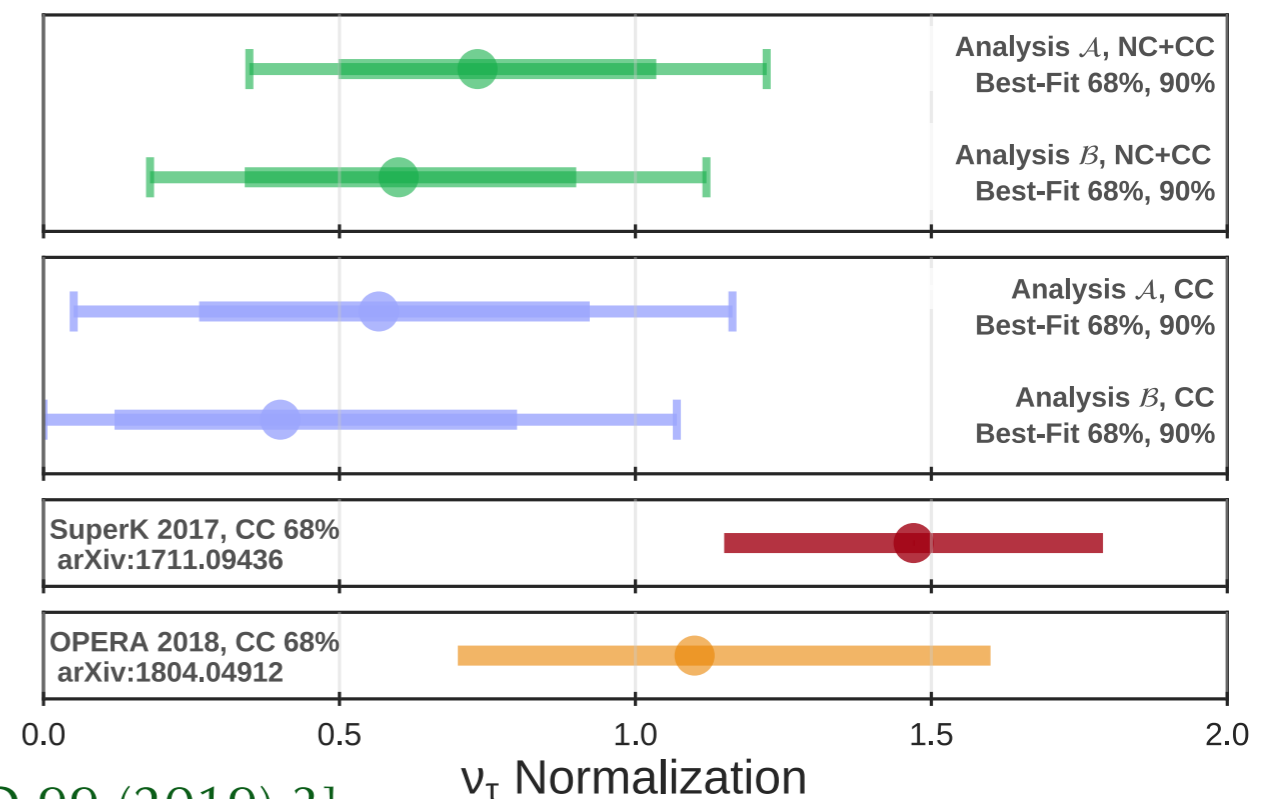


Tau Neutrino Appearance

- 86% of ν_τ global data from IceCube
- High statistics of ν_τ allow to make **precision tests** of the 3-flavour oscillation paradigm.
- Tau neutrino appearance at 3σ level with normalization $0.49 - 1.03$.

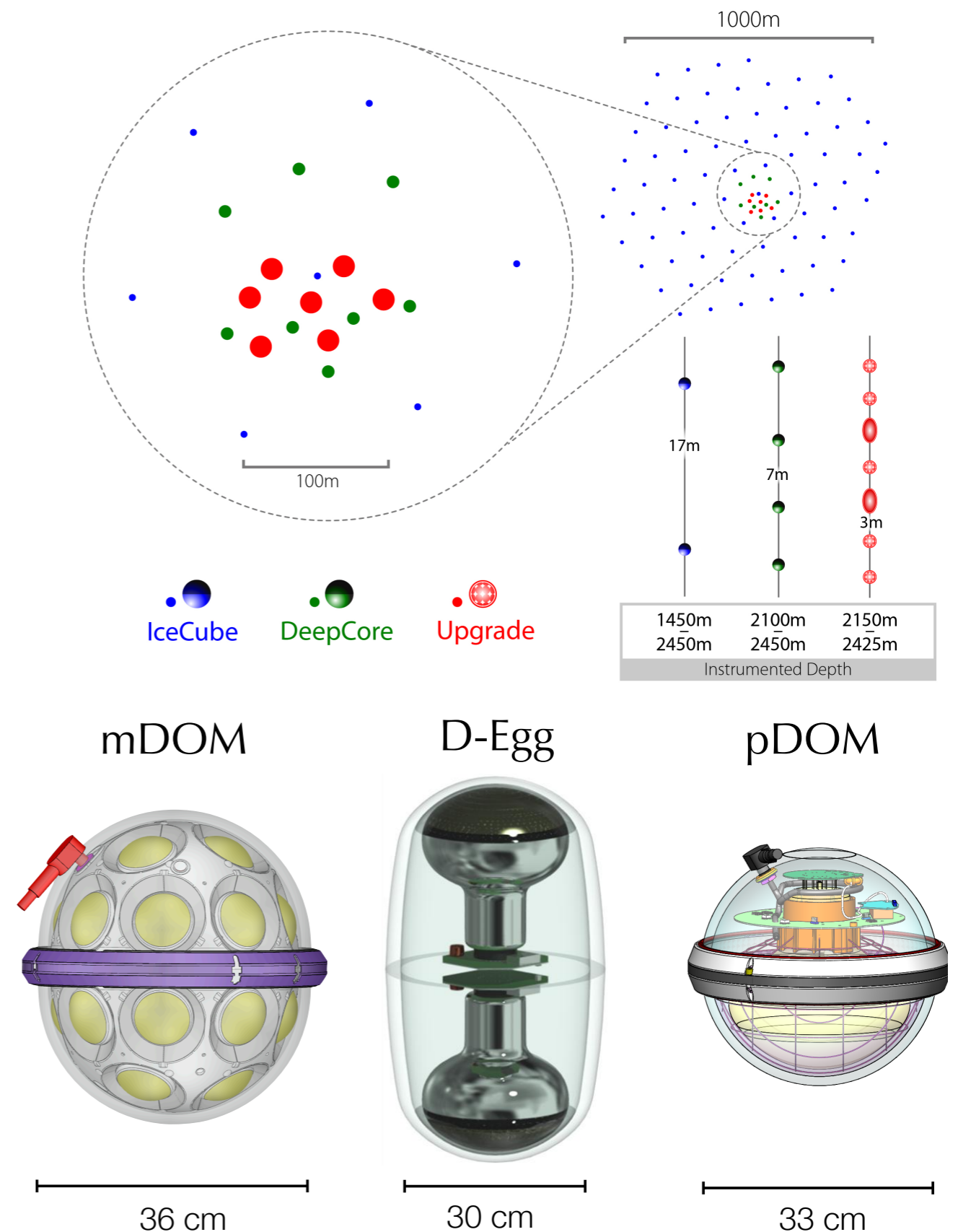


[IceCube, PRD 99 (2019) 3]



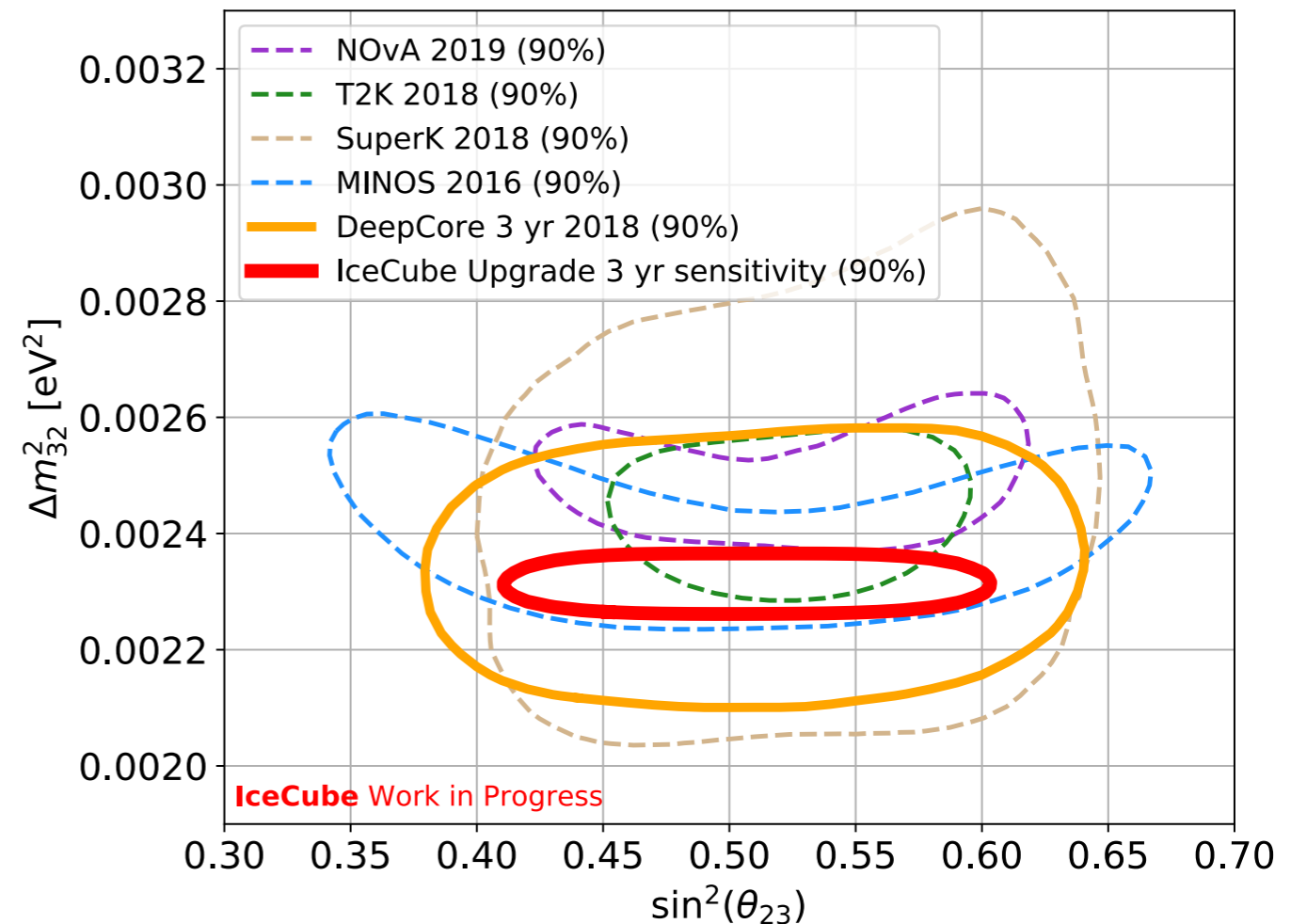
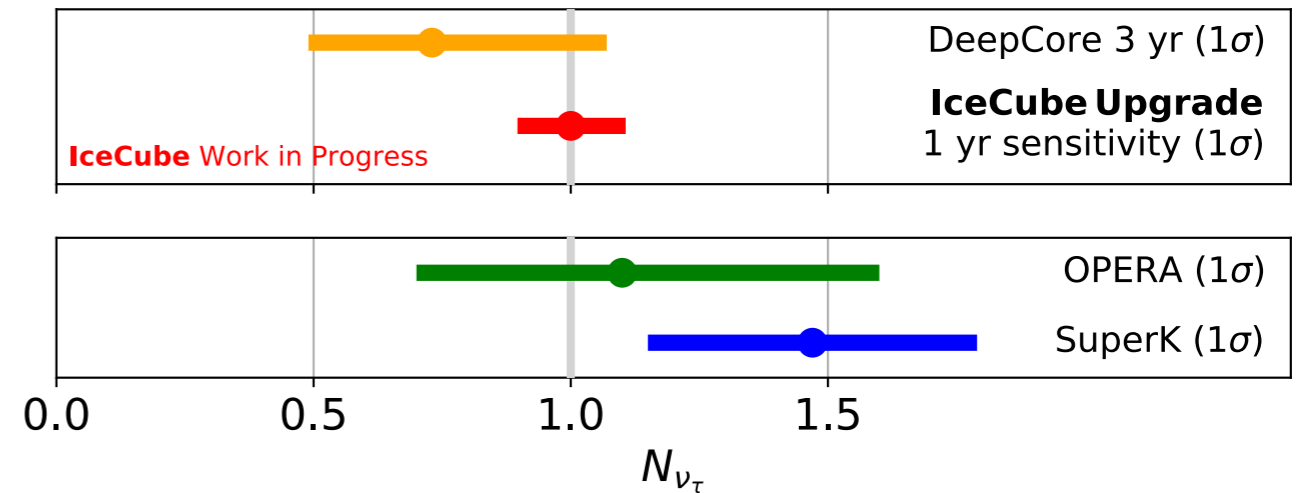
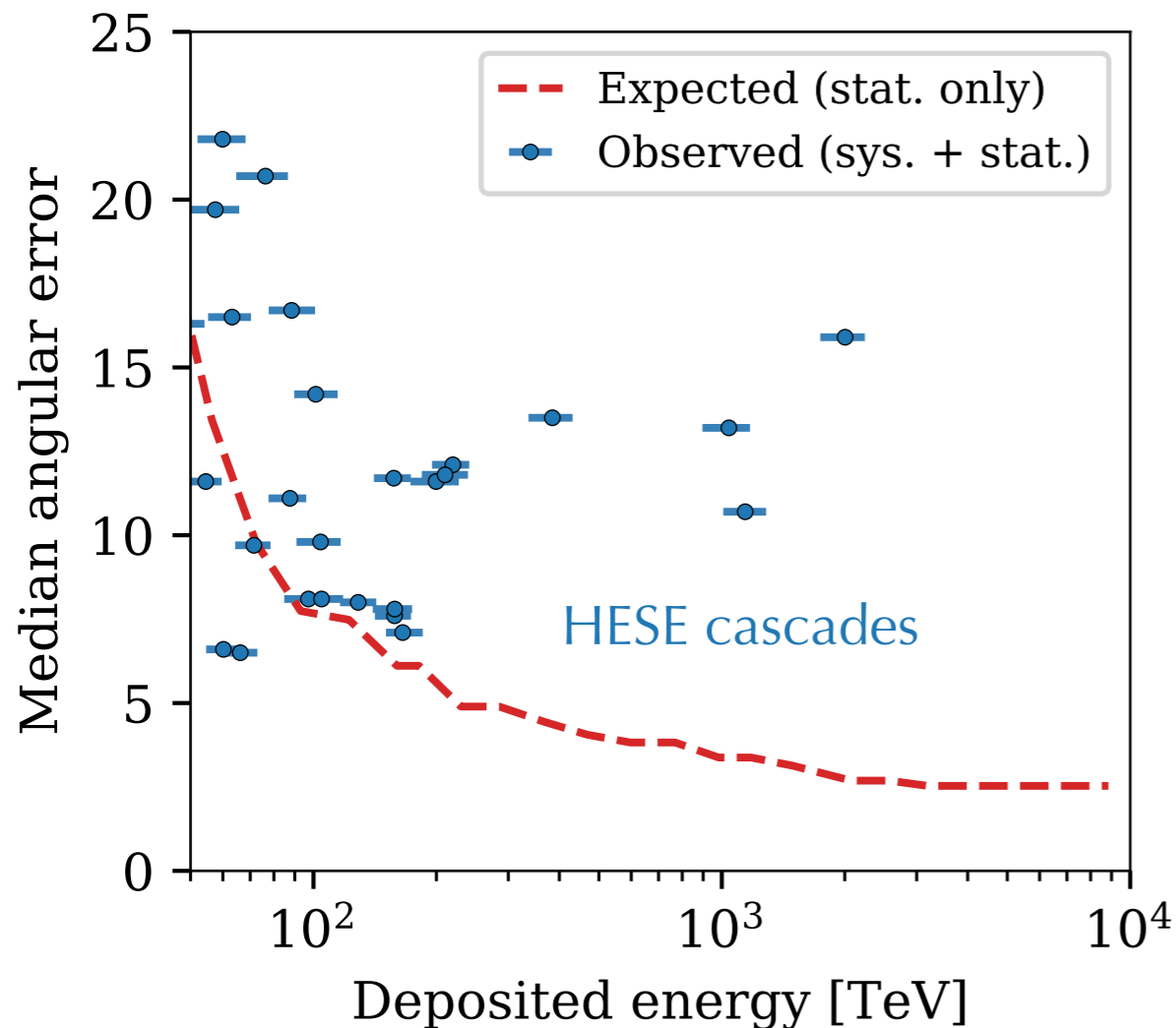
Outlook: IceCube Upgrade

- **7 new strings** in the DeepCore region (~20m inter-string spacing)
- **New sensor designs**, optimized for ease of deployment, light sensitivity & effective area
- **New calibration devices**, incorporating lessons from a decade of IceCube calibration efforts
- In parallel, **IceTop surface enhancements** (scintillators & radio antennas) for CR studies.
- **Aim: deployment in 2025/26**



Outlook: IceCube Upgrade

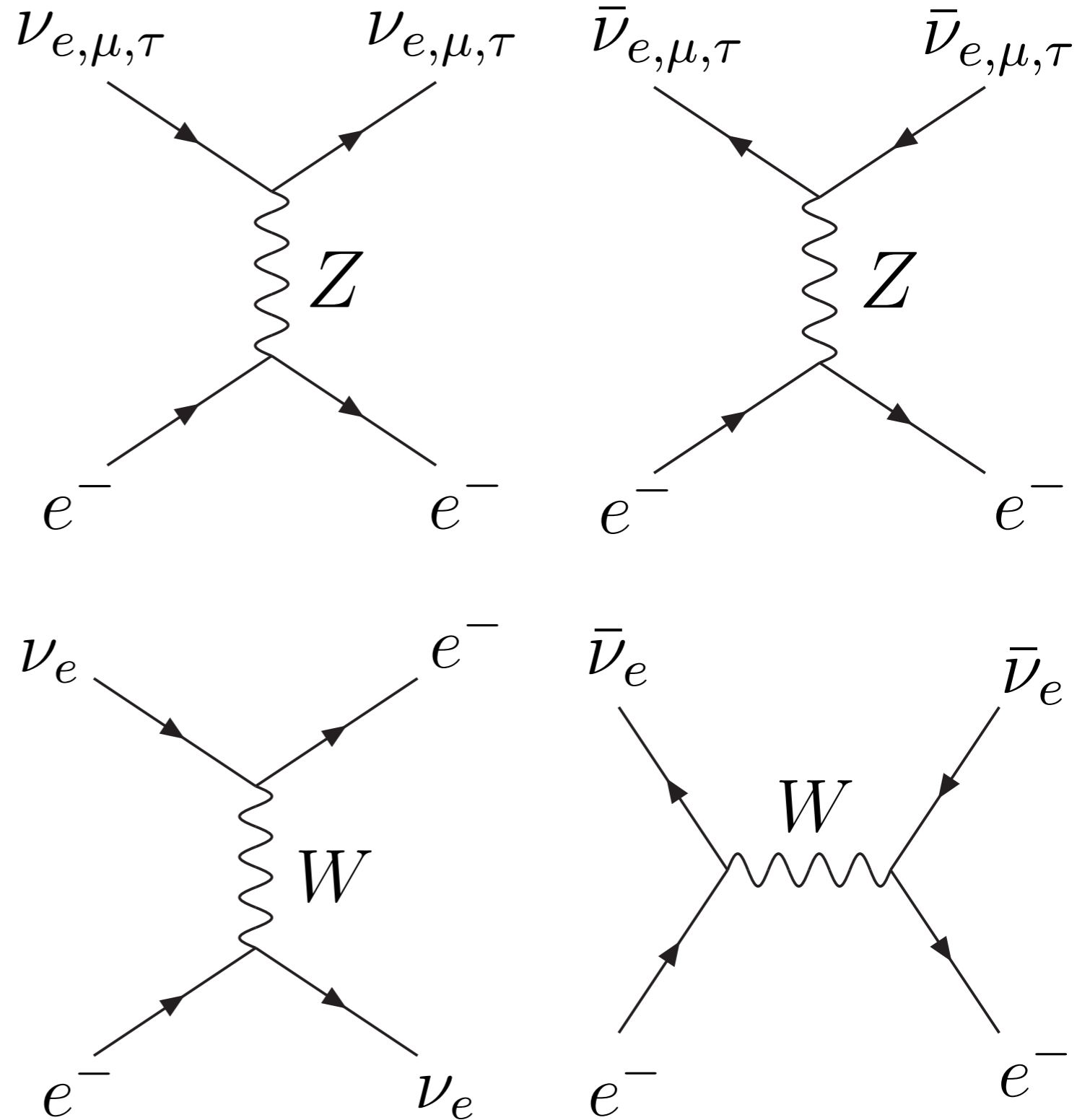
- **Precision measurement** of atmospheric neutrino oscillations and tau neutrino appearance
- **Improved energy and angular reconstructions** of IceCube data



[IceCube, PoS (ICRC2019) 1031]

Matter Effects

Neutrino interactions with matter single out ν_e & $\bar{\nu}_e$ and introduce **non-universal effective potential.**



$$V_{\text{CC}}(\mathbf{r}) = \begin{pmatrix} A(\mathbf{r}) & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A(\mathbf{r}) = \begin{cases} +\sqrt{2}G_F n_e(\mathbf{r}) & \nu_e \\ -\sqrt{2}G_F n_e(\mathbf{r}) & \bar{\nu}_e \end{cases}$$

[Wolfenstein'78; Mikheyev & Smirnov'85]

Matter Effects

Matter effects in atmospheric ν oscillations are **sensitive to mass ordering**:

[Choubey & Roy'06]

$$P(\nu_\mu \rightarrow \nu_e) \simeq \sin^2 \theta_{23} \sin^2 2\Theta_{13} \sin^2 \frac{\Delta M_{31}^2 \ell}{4E_\nu}$$

$$P(\nu_\mu \rightarrow \nu_\mu) \simeq 1 - \sin^2 2\theta_{23} \cos^2 \Theta_{13} \sin^2 \left(\frac{(\Delta m_{31}^2 + \Delta M_{31}^2) \ell}{8E_\nu} + \frac{A\ell}{4} \right)$$

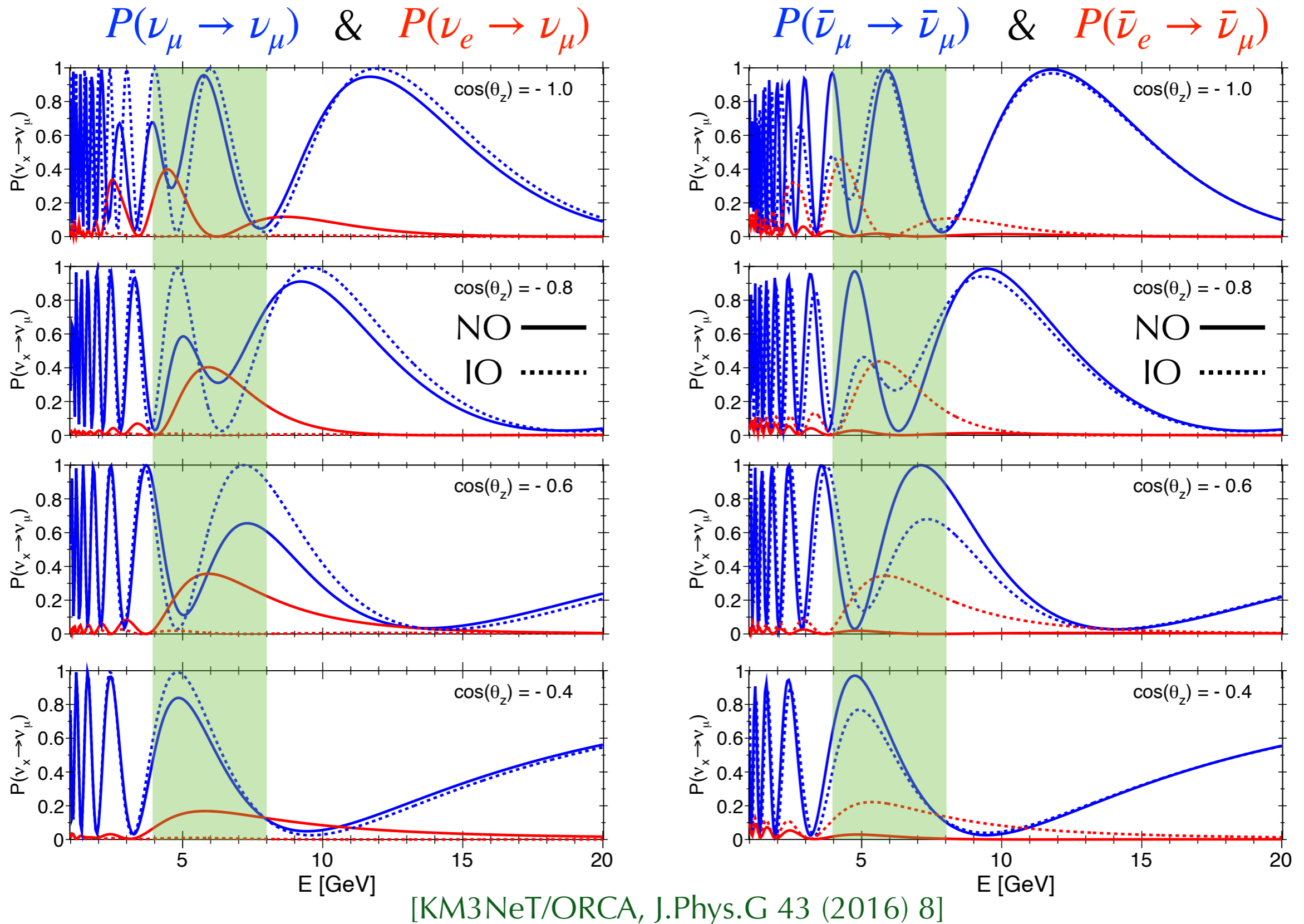
$$- \sin^2 2\theta_{23} \sin^2 \Theta_{13} \sin^2 \left(\frac{(\Delta m_{31}^2 - \Delta M_{31}^2) \ell}{8E_\nu} + \frac{A\ell}{4} \right)$$

$$- \sin^4 \theta_{23} \sin^2 2\Theta_{13} \sin^2 \frac{\Delta M_{31}^2 \ell}{4E_\nu}$$

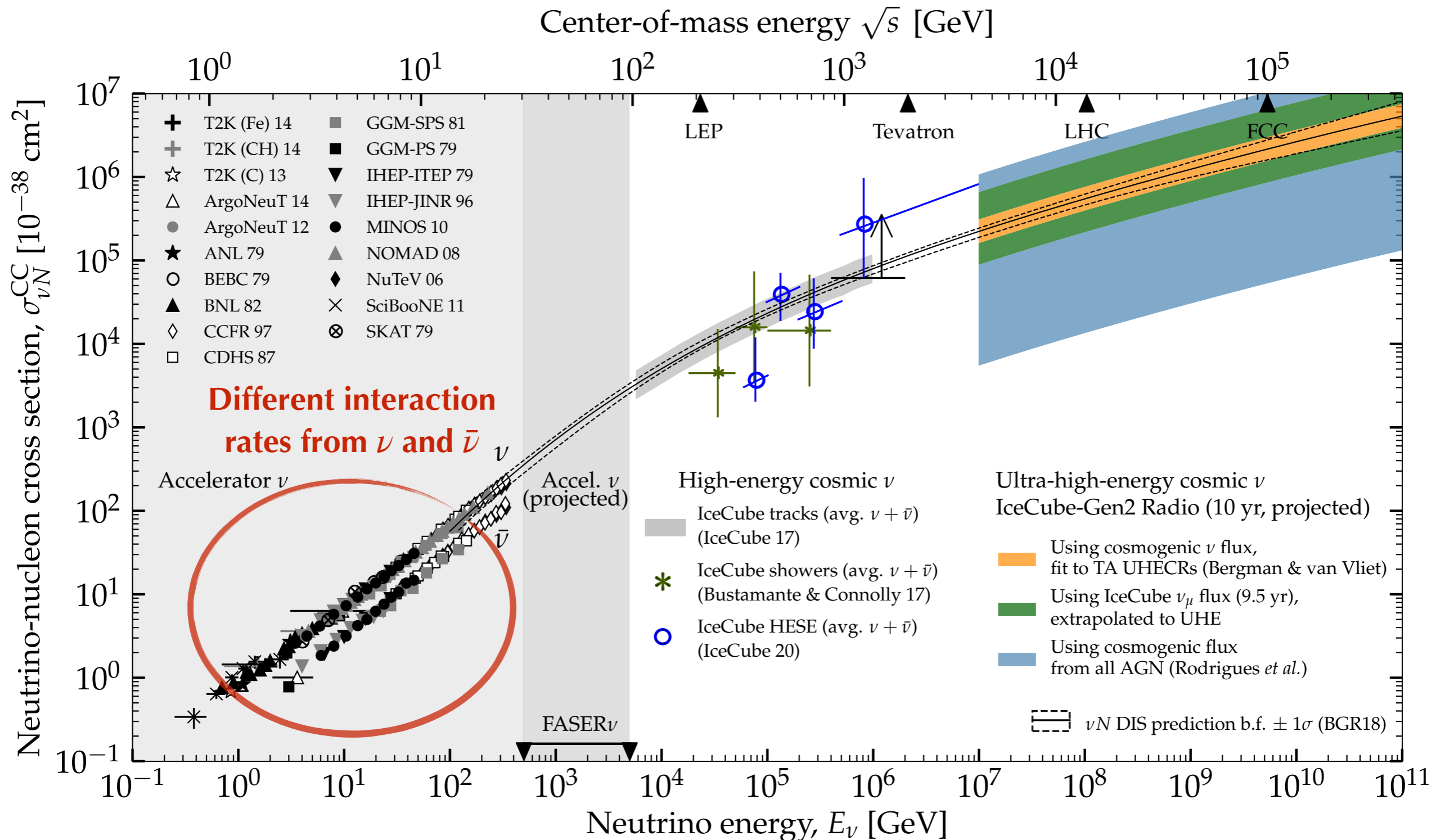
$$\sin^2 2\Theta_{13} \equiv \sin^2 2\theta_{13} \left(\frac{\Delta m_{31}^2}{\Delta M_{31}^2} \right)^2 \quad \Delta M_{31}^2 \equiv \sqrt{(\Delta m_{31}^2 \cos 2\theta_{13} - 2E_\nu A)^2 + (\Delta m_{31}^2 \sin 2\theta_{13})^2}$$

Maximal mixing $\sin^2 2\Theta_{13} \rightarrow 1$ at energies $E_{\text{res}} \simeq (4 - 8) \text{ GeV}$.

Sensitivity to Mass Ordering

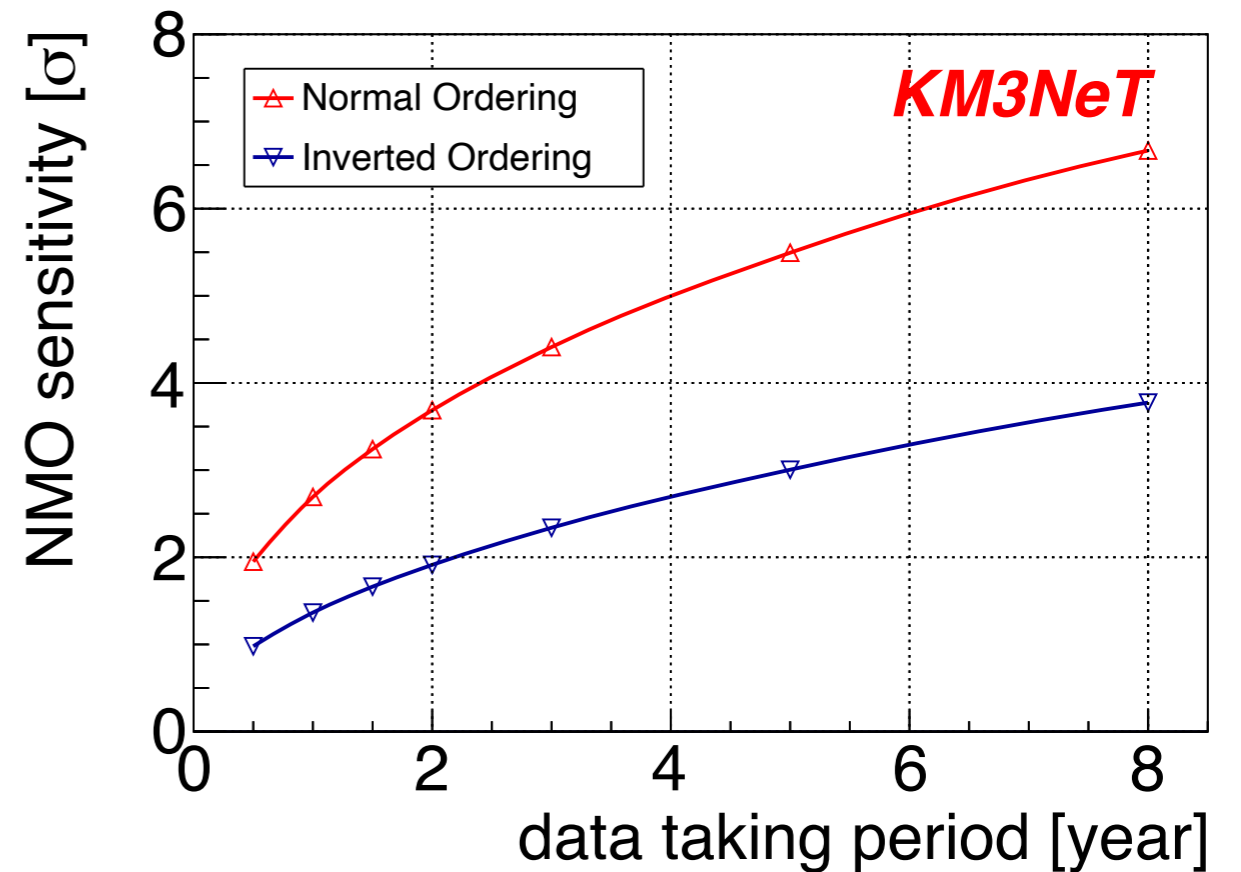
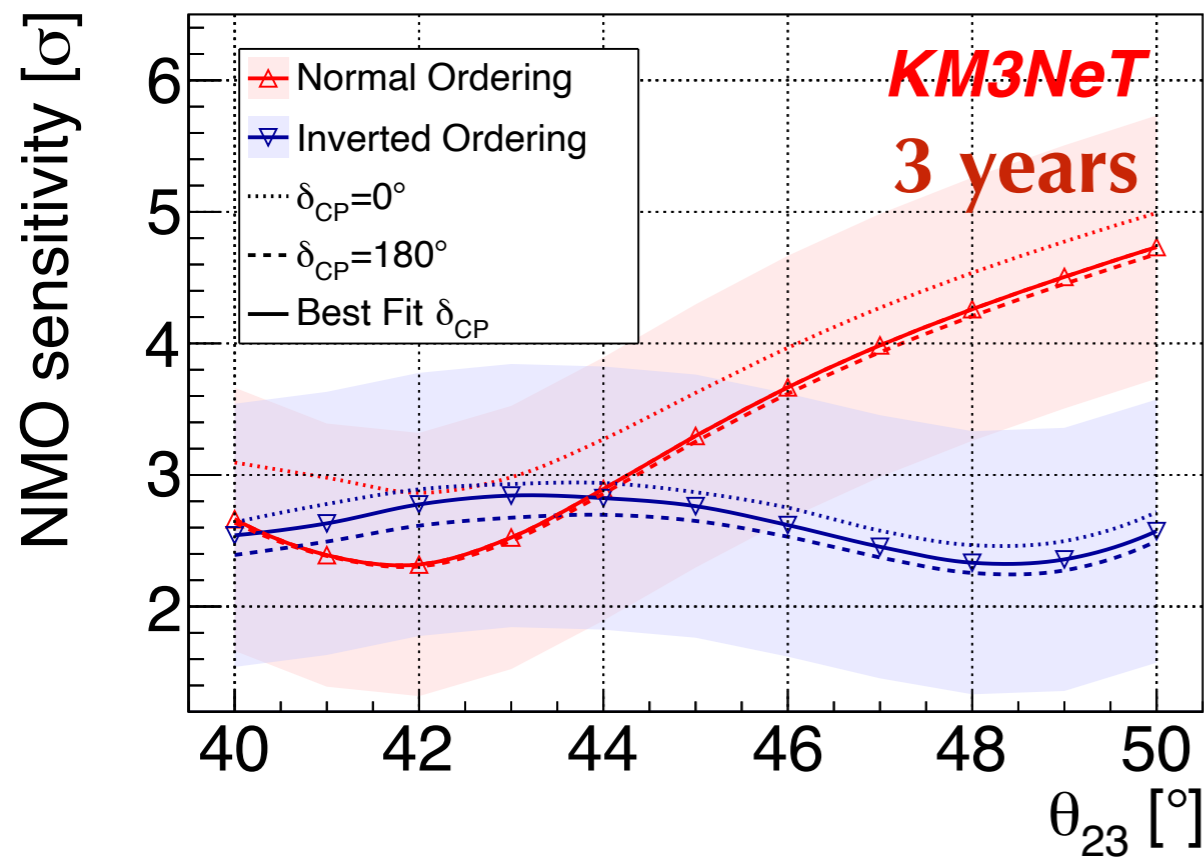
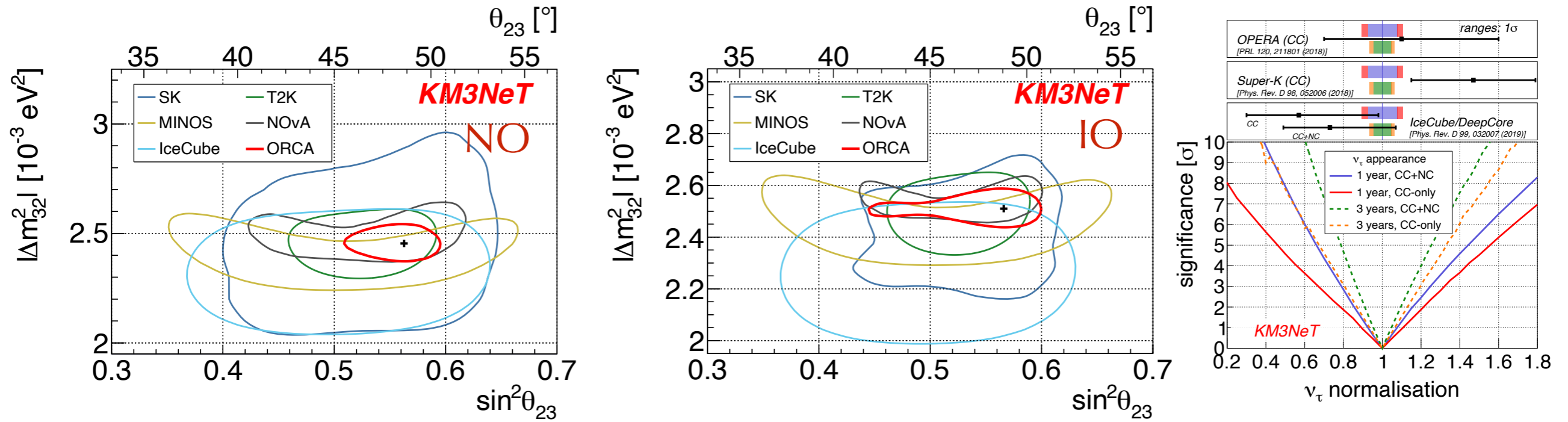


Neutrino Cross Section



[IceCube-Gen2 Technical Design Report: icecube-gen2.wisc.edu/science/publications/tdr/]

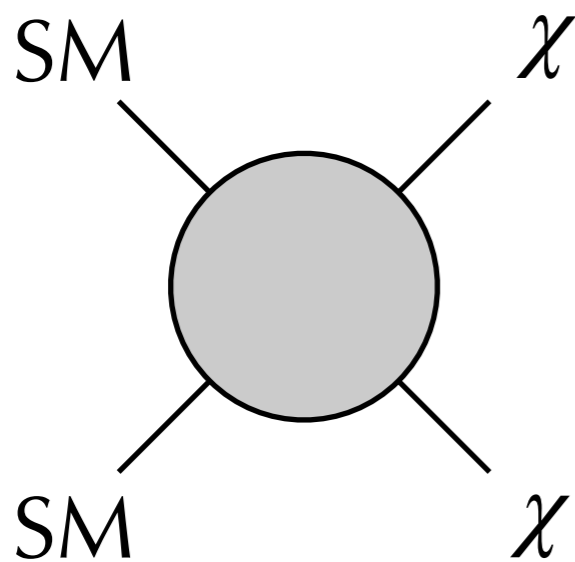
Sensitivity to Mass Ordering



[KM3NeT/ORCA, EPJC 82 (2022) 1]

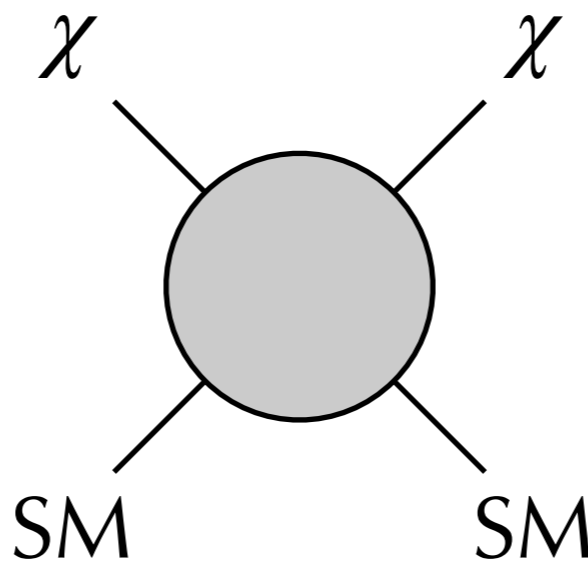
WIMP Dark Matter

Weakly Interacting Massive Particles (WIMPs) are well-motivated DM candidates that appear in extensions of the Standard Model, e.g., by supersymmetry.



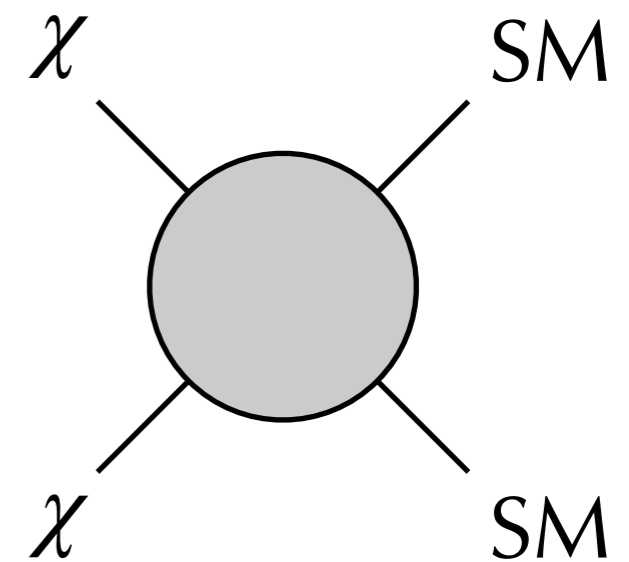
"make it"

thermal production
in the early Universe



"shake it"

direct observation in
scattering
experiments



"break it"

indirect observation
by final stable SM
particles

Annihilation and Decay

- Neutrino emission from DM annihilation ($\rho_\chi = m_\chi n_\chi$) at a rate:

$$Q_{\nu_\alpha}^{\text{ann}}(\mathbf{r}) = \frac{1}{2} \rho_\chi^2(\mathbf{r}) \frac{\langle \sigma_A v \rangle}{m_\chi^2} \frac{dN_{\nu_\alpha}}{dE_\nu} \quad Q_{\nu_\alpha}^{\text{dec}}(\mathbf{r}) = \rho_\chi(\mathbf{r}) \frac{\Gamma_\chi}{m_\chi} \frac{dN_{\nu_\alpha}}{dE_\nu}$$

- Neutrino flux observed per solid angle from Earth's location \mathbf{r}_\oplus :

$$\phi_{\nu_\beta}(E_\nu) = \sum_{\nu_\alpha} P_{\nu_\alpha \rightarrow \nu_\beta} \underbrace{\left[\int_0^\infty d\ell \rho_\chi^2(\mathbf{r}_\oplus + \ell \hat{\mathbf{n}}) \right]}_{\text{"}\mathcal{J}\text{-factor"}}$$

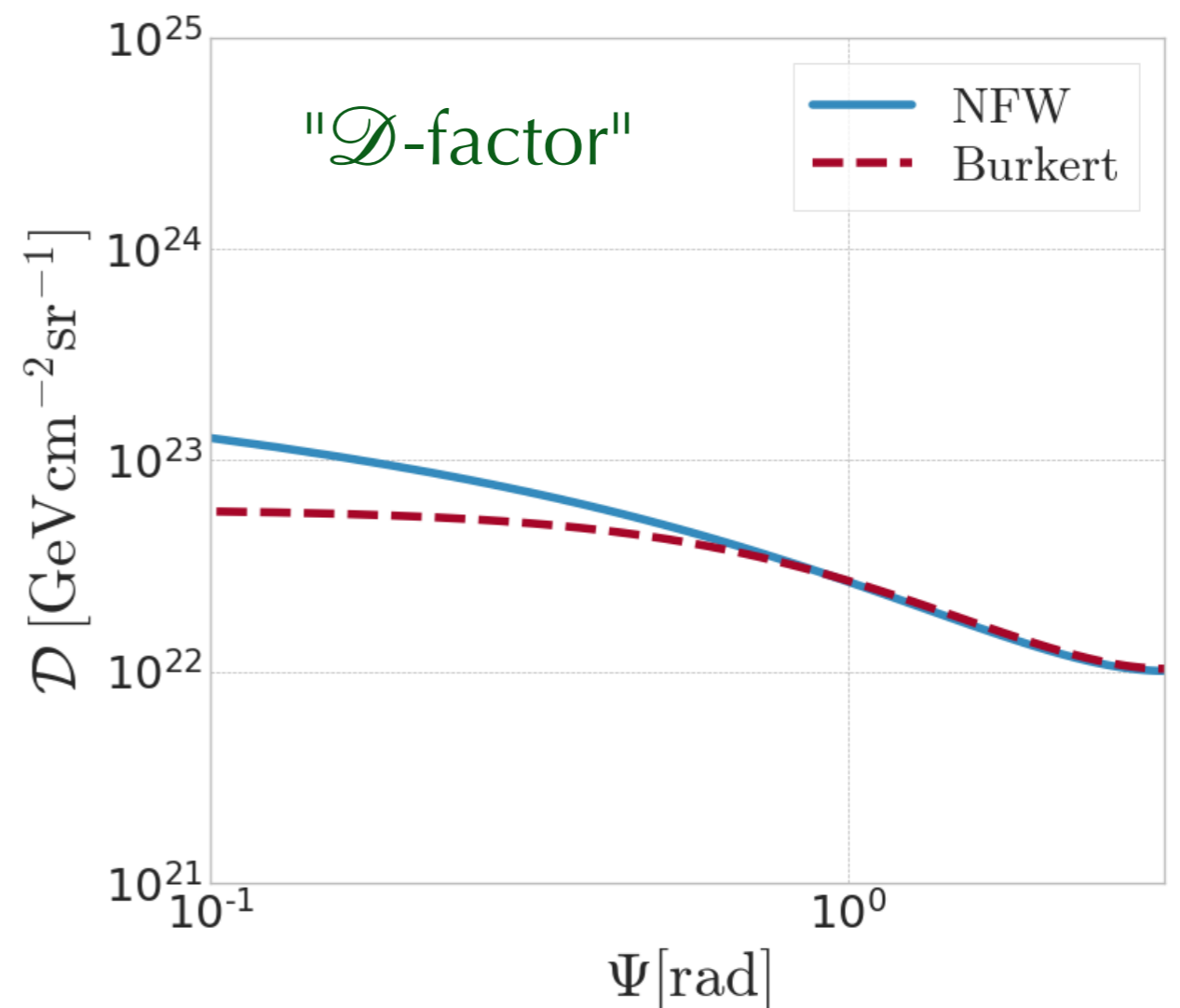
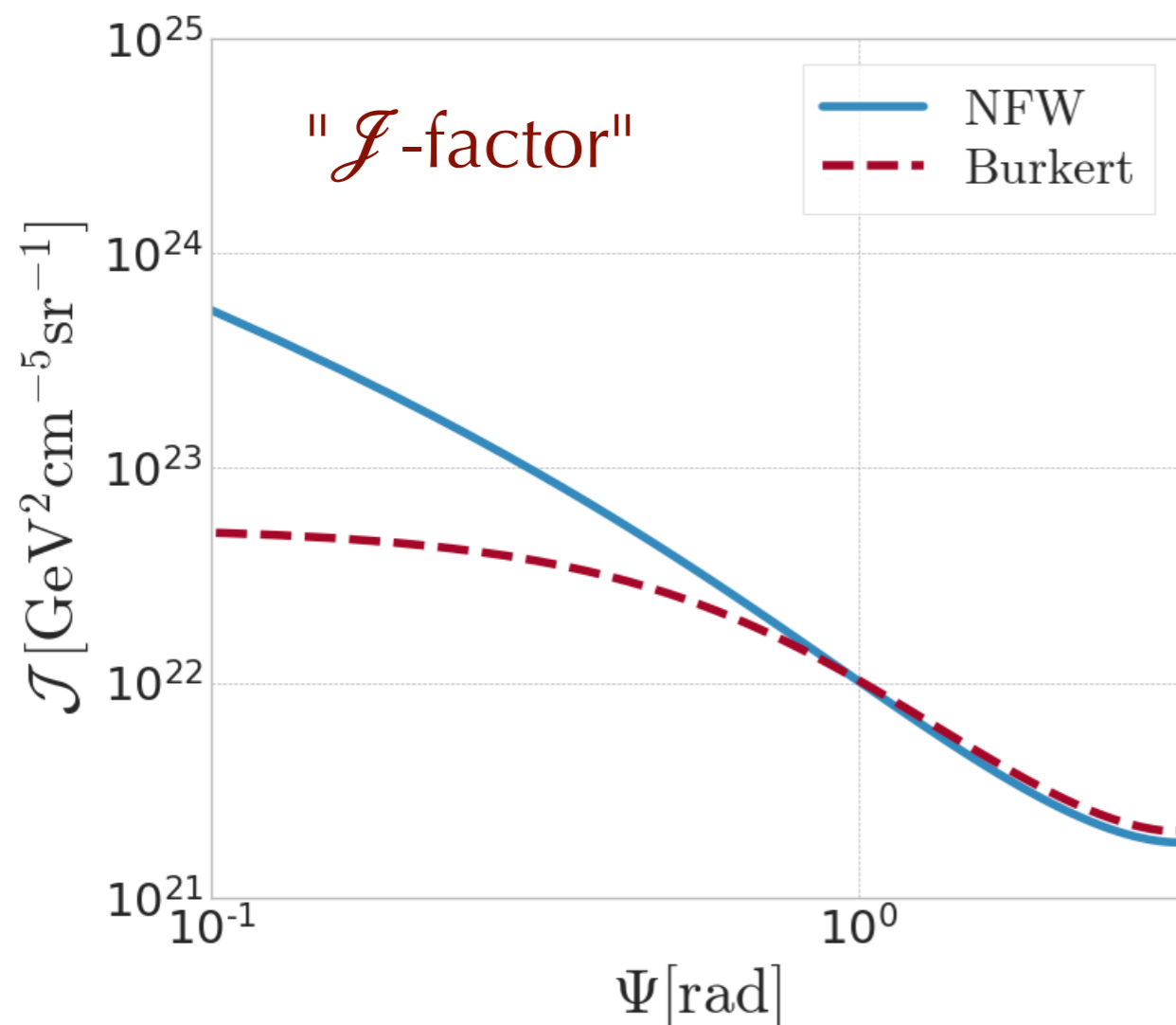
$$\frac{\langle \sigma_A v \rangle}{8\pi m_\chi^2} \frac{dN_{\nu_\alpha}}{dE_\nu}$$

$$\phi_{\nu_\beta}(E_\nu) = \sum_{\nu_\alpha} P_{\nu_\alpha \rightarrow \nu_\beta} \underbrace{\left[\int_0^\infty d\ell \rho_\chi(\mathbf{r}_\oplus + \ell \hat{\mathbf{n}}) \right]}_{\text{"}\mathcal{D}\text{-factor"}}$$

$$\frac{\Gamma_\chi}{4\pi m_\chi} \frac{dN_{\nu_\alpha}}{dE_\nu}$$

Galactic DM Distribution

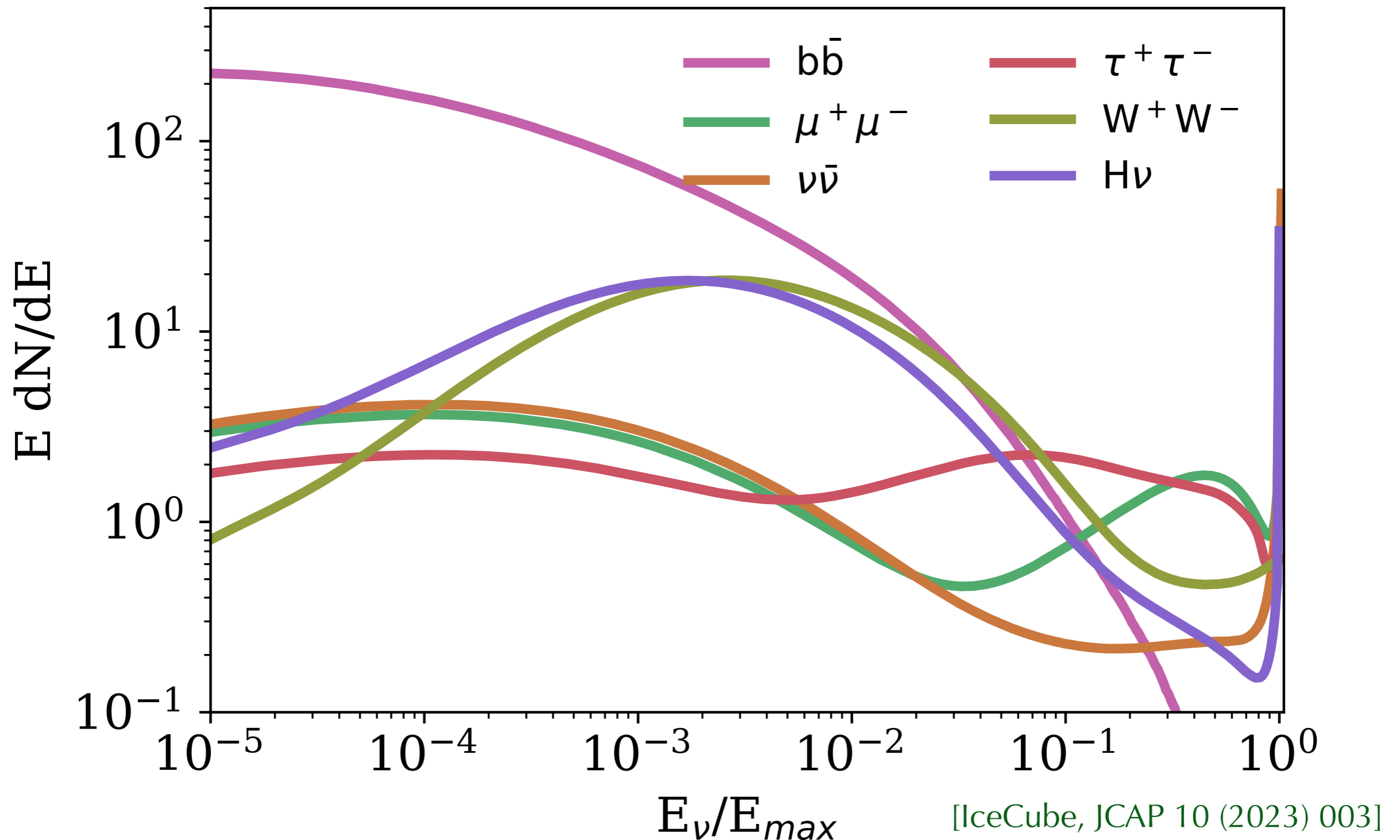
Distribution of neutrino flux depends on the "cuspieness" of the Milky Way dark matter distribution, in particular for the annihilation signal (\mathcal{J} -factor).



[IceCube, PRD 108 (2023) 10]

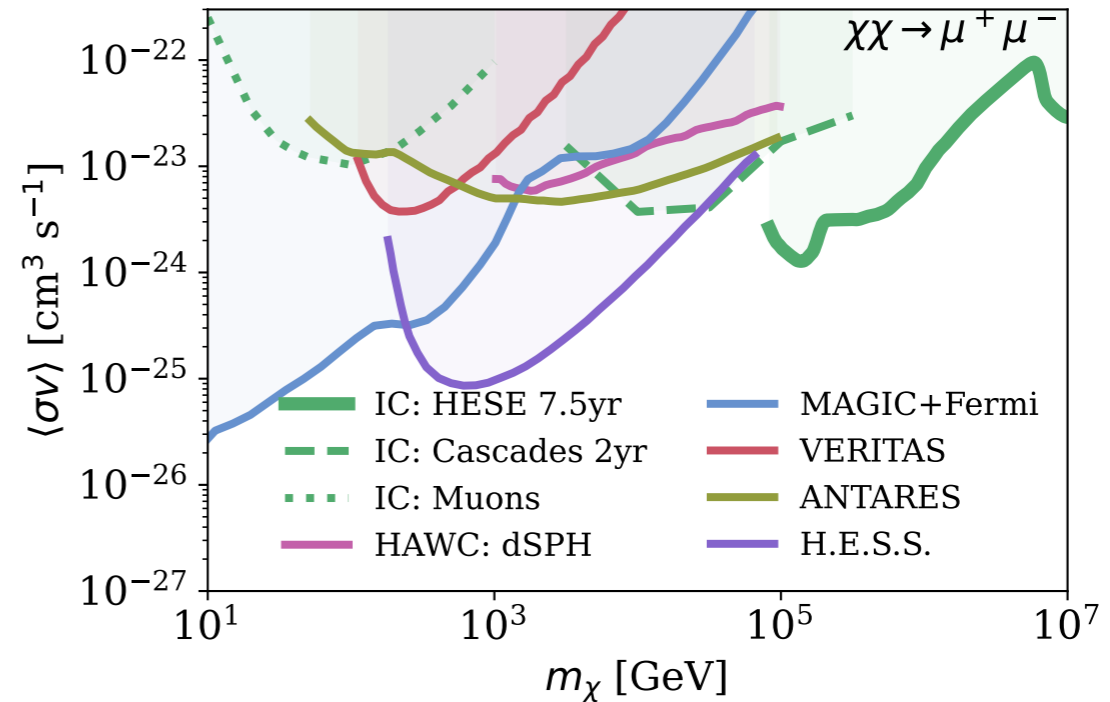
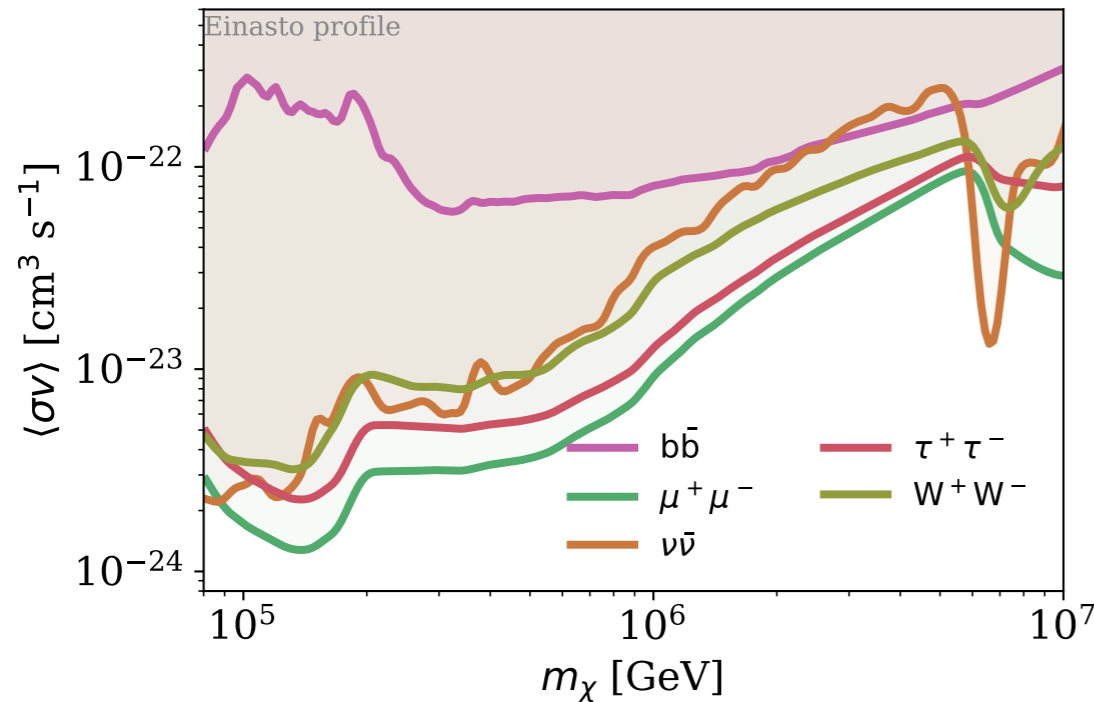
Neutrino Spectra from DM

Neutrino energy distribution from dark matter decay or annihilation.

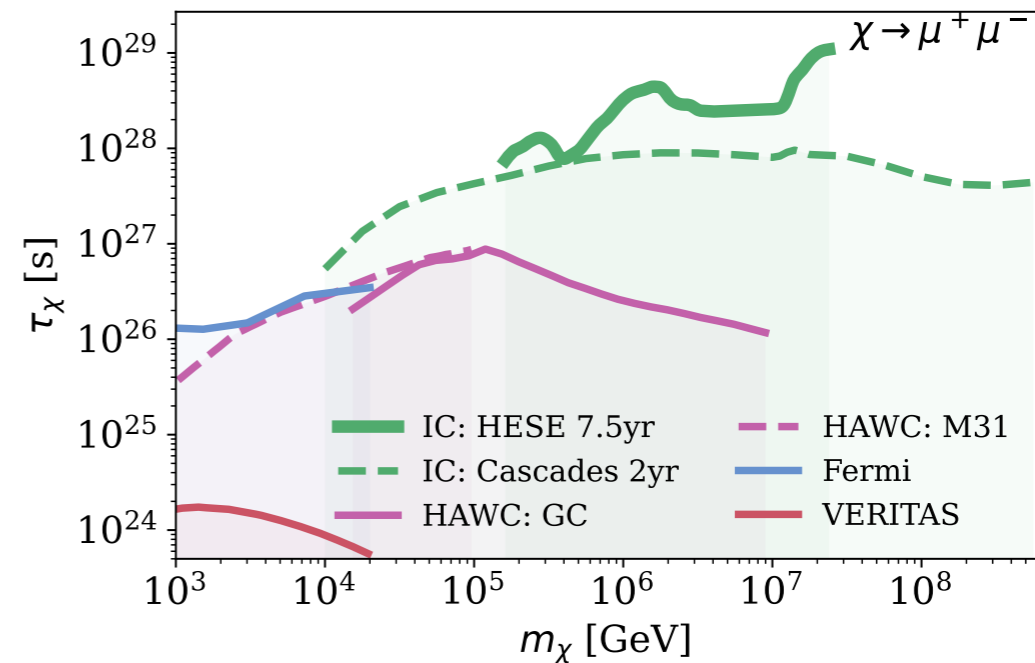
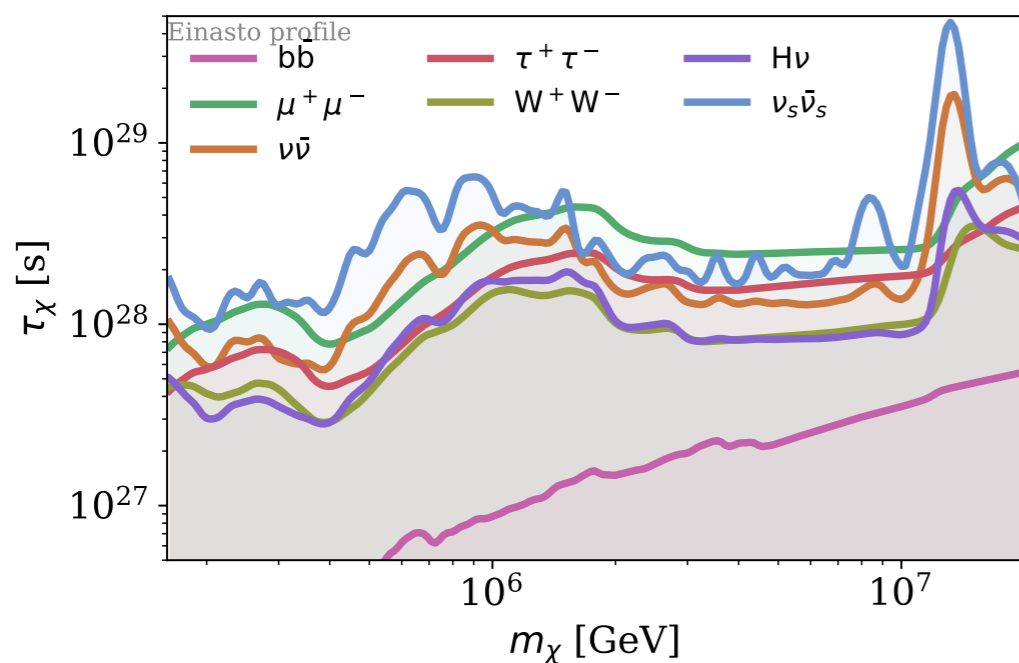


Indirect DM Limits

Upper limits on **velocity-averaged self-annihilation cross-section**.



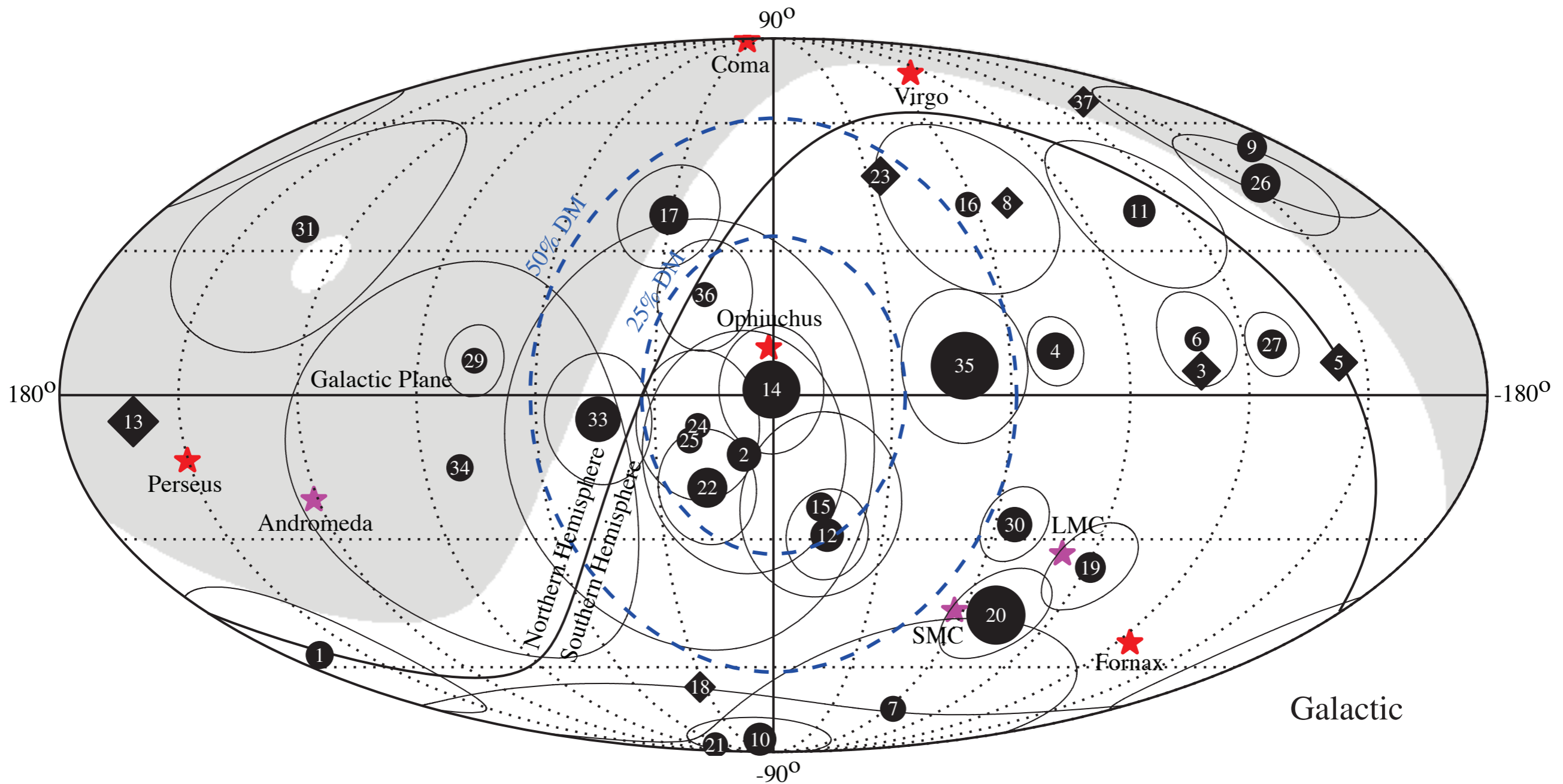
Lower limits on the **dark matter lifetime**.



[IceCube, JCAP 10 (2023) 003]

Cosmic Neutrinos & PeV DM

Distribution of cosmic neutrinos from 2013 HESE analysis.



[Murase, Laha, Ando & MA'15]

[Feldstein, Kusenko, Matsumoto & Yanagida'13; Esmaili & Serpico'13; Zavala'14]

DM Annihilation in the Sun

- Evolution of the DM density in compact celestial objects:

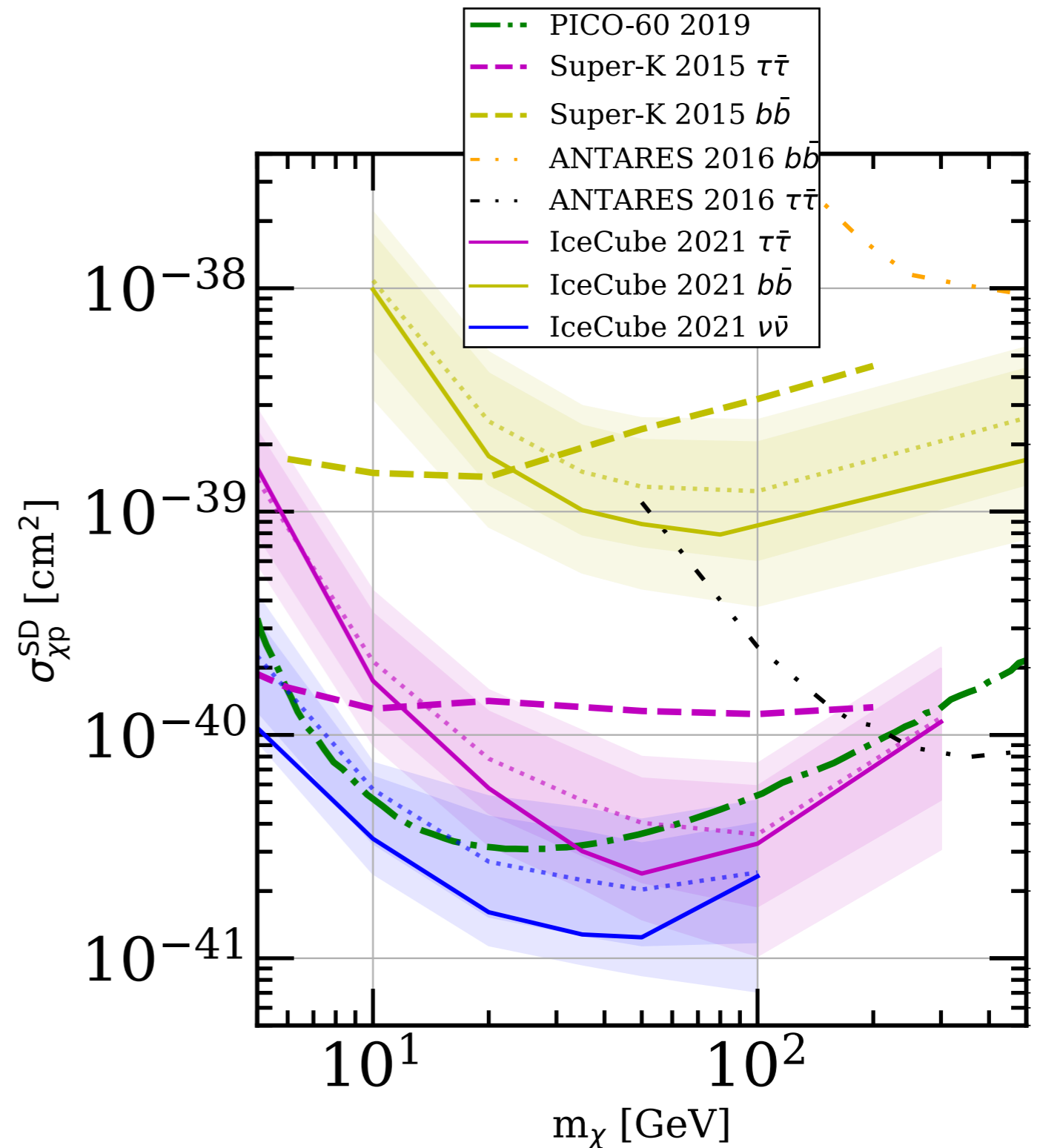
$$\dot{n}_\chi = Q_C - 2\langle\sigma_{AV}\rangle\frac{n_\chi^2}{2}$$

- DM **equilibrium density**:

$$n_{\chi,\text{eq}} = \sqrt{\frac{Q_C}{\langle\sigma_{AV}\rangle}}$$

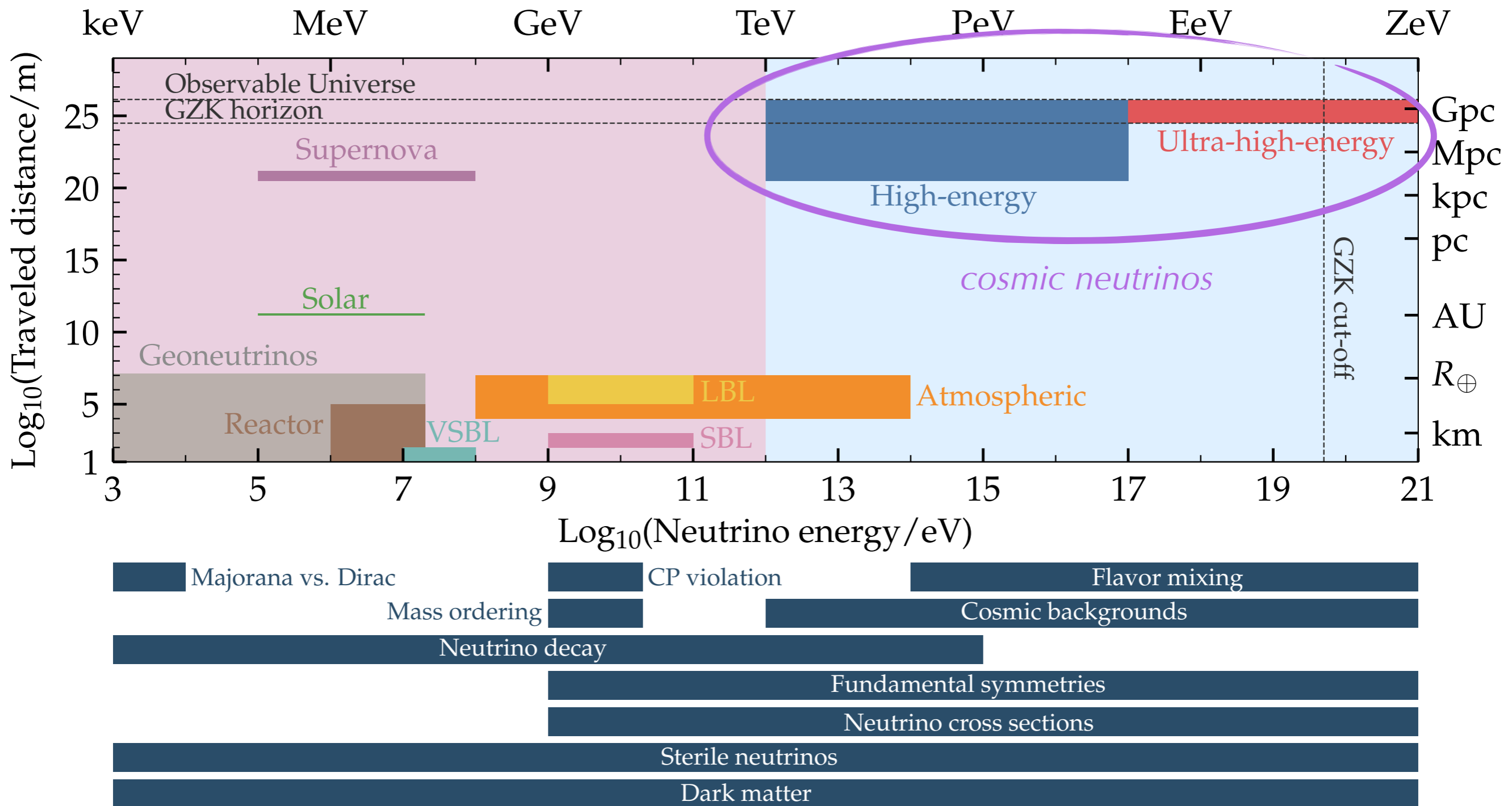
- The neutrino emission proportional to **capture rare**:

$$Q_{\nu_\alpha}^{\text{ann}}(\mathbf{r}) = \frac{Q_C}{2} \frac{dN_{\nu_\alpha}}{dE_\nu} \propto \sigma_{\chi N}$$



[IceCube, PRD 105 (2022) 6]

Probe of Fundamental Physics



[Ackermann, MA, Anchordoqui, Bustamante+ **Bull.Am.Astron.Soc.** 51 (2019)]

Sterile Neutrinos

- Sterile $\mathcal{O}(1)$ eV neutrino motivated by **anomalous data** of accelerator, reactor, and radioactive source experiments:

$$\nu_{\mu} \rightarrow \nu_e \text{ \& } \bar{\nu}_{\mu} \rightarrow \bar{\nu}_e \text{ appearance}$$

(LSND & MiniBooNE)

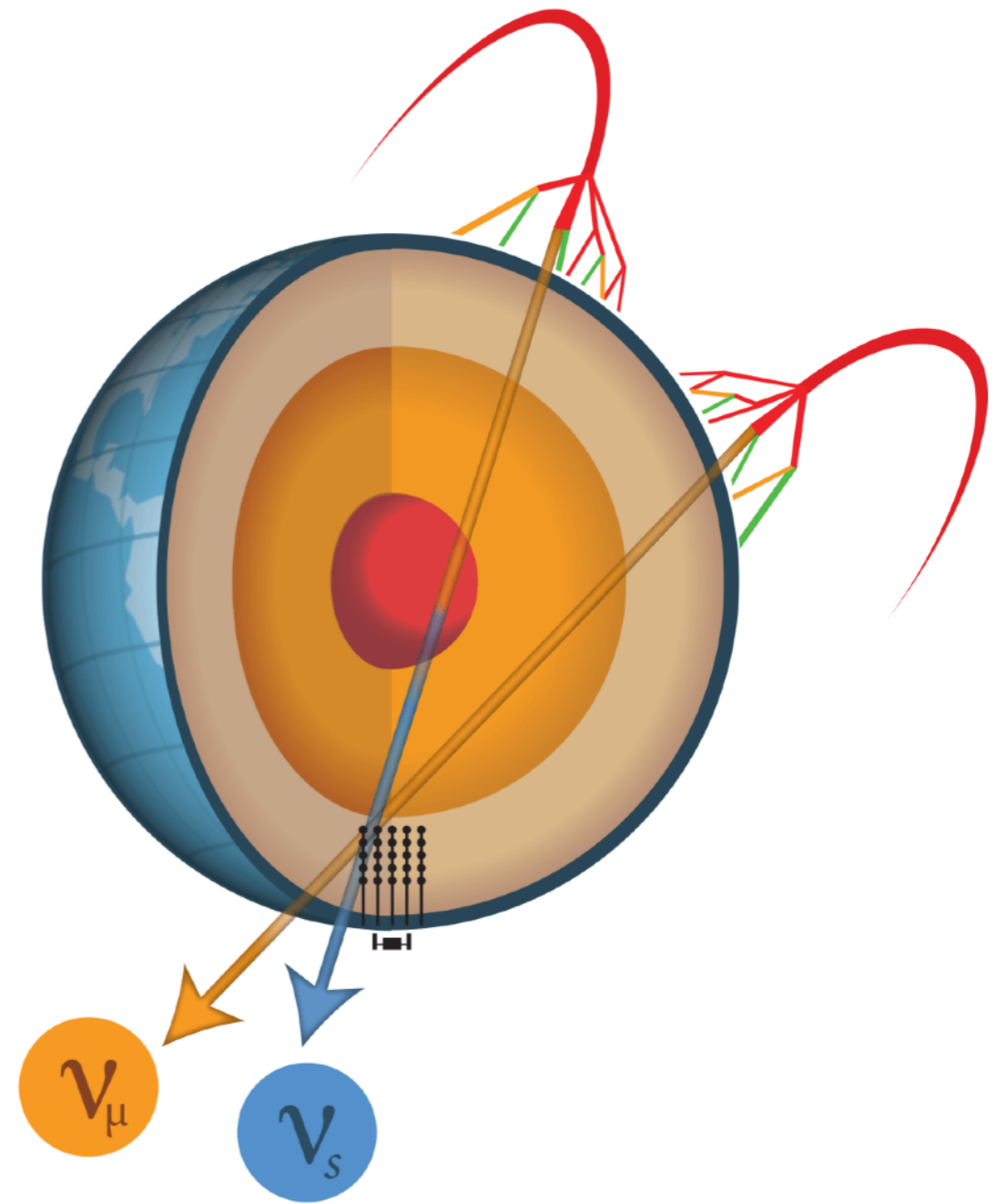
$$\nu_e \text{ \& } \bar{\nu}_e \text{ disappearance}$$

(reactor, GALLEX & SAGE)

- IceCube is sensitive to the "3+1" sterile neutrino model:

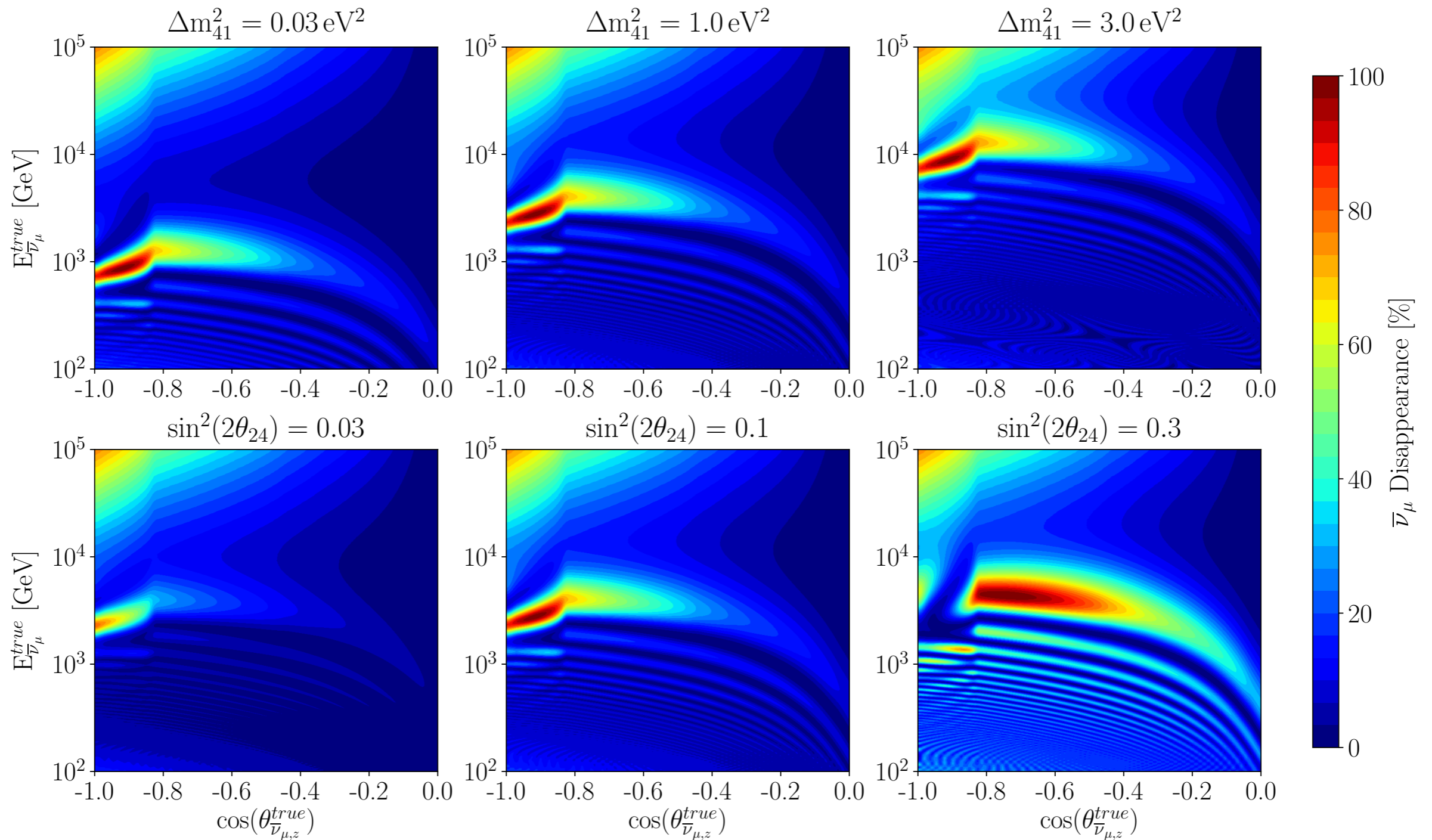
$$U_{4 \times 4} = R_{34} R_{24} R_{14} U_{\text{PMNS}}$$

- Energy-dependent distortions of atmospheric ν_{μ} & $\bar{\nu}_{\mu}$ **disappearance** in **matter-enhanced oscillations**.



Sterile Neutrinos

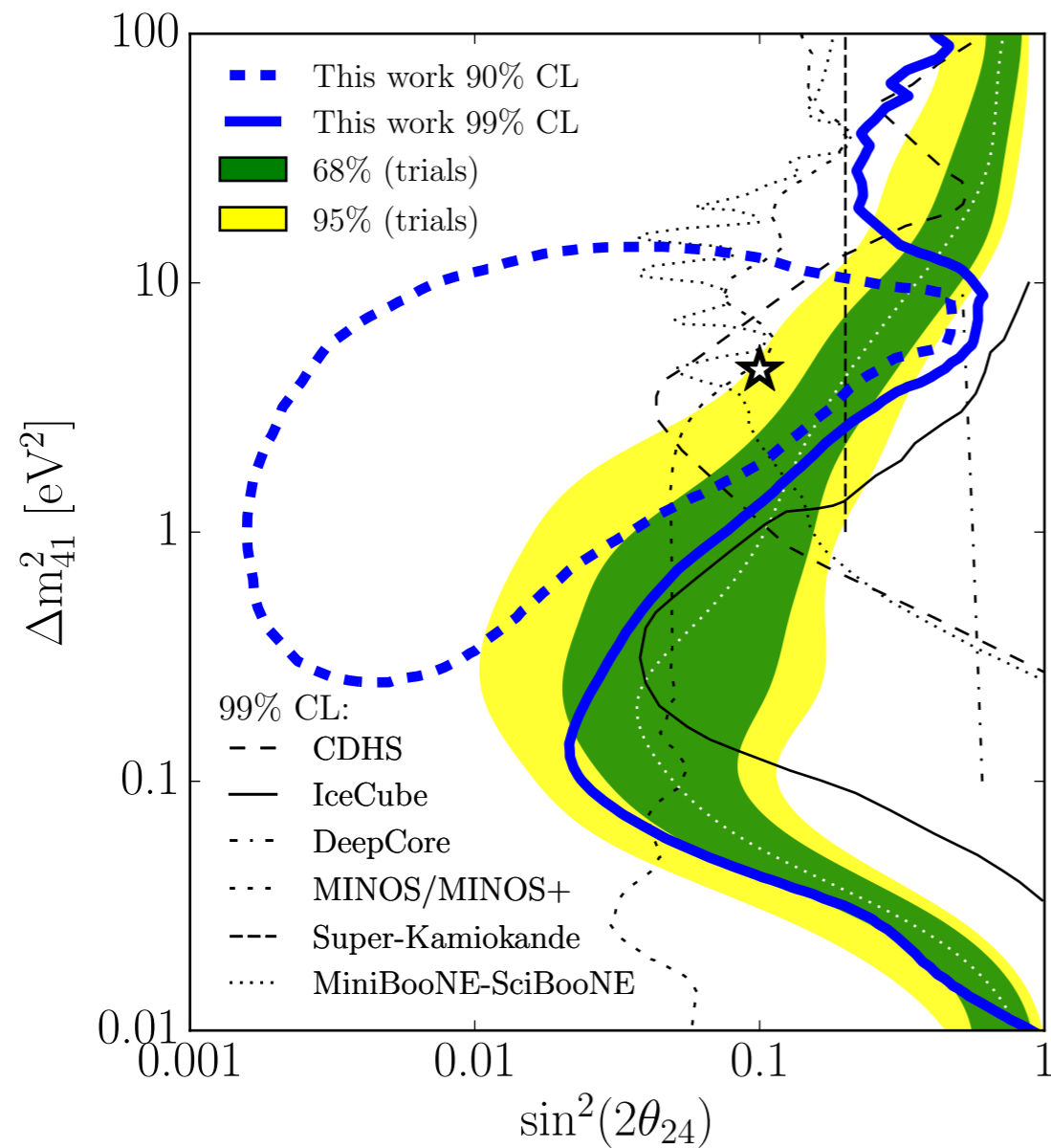
$$|U_{\mu 4}|^2 = \sin^2 \theta_{24} \quad \& \quad |U_{e 4}|^2 = |U_{\tau 4}|^2 = 0$$



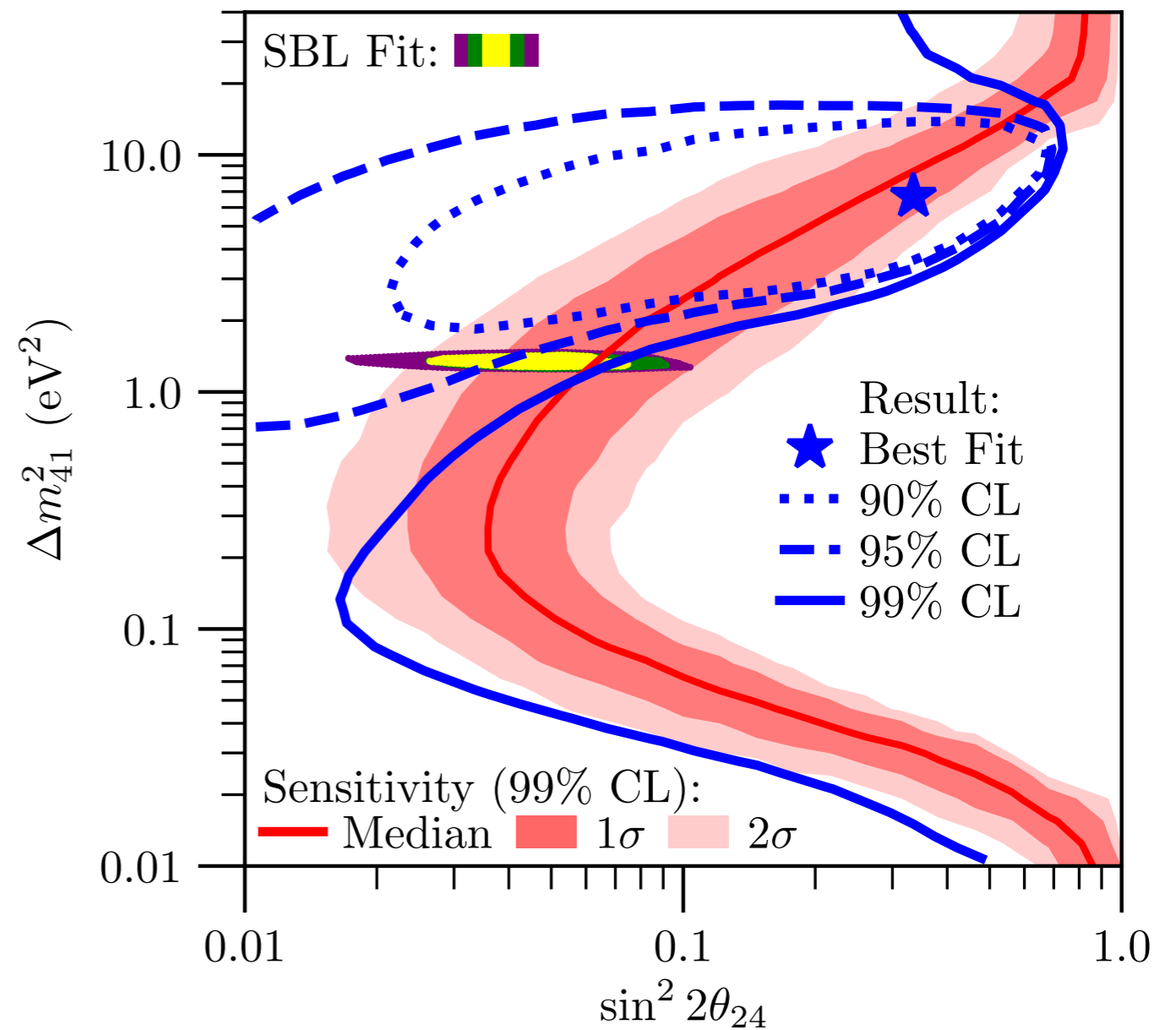
[IceCube, PRL 125 (2020) 14; PRD 102 (2020) 5]

Sterile Neutrino Searches

Best-fit contours in for **stable** (left) and **unstable** (right) sterile neutrinos.



[IceCube, PRL 125 (2020) 14; PRD 102 (2020) 5]

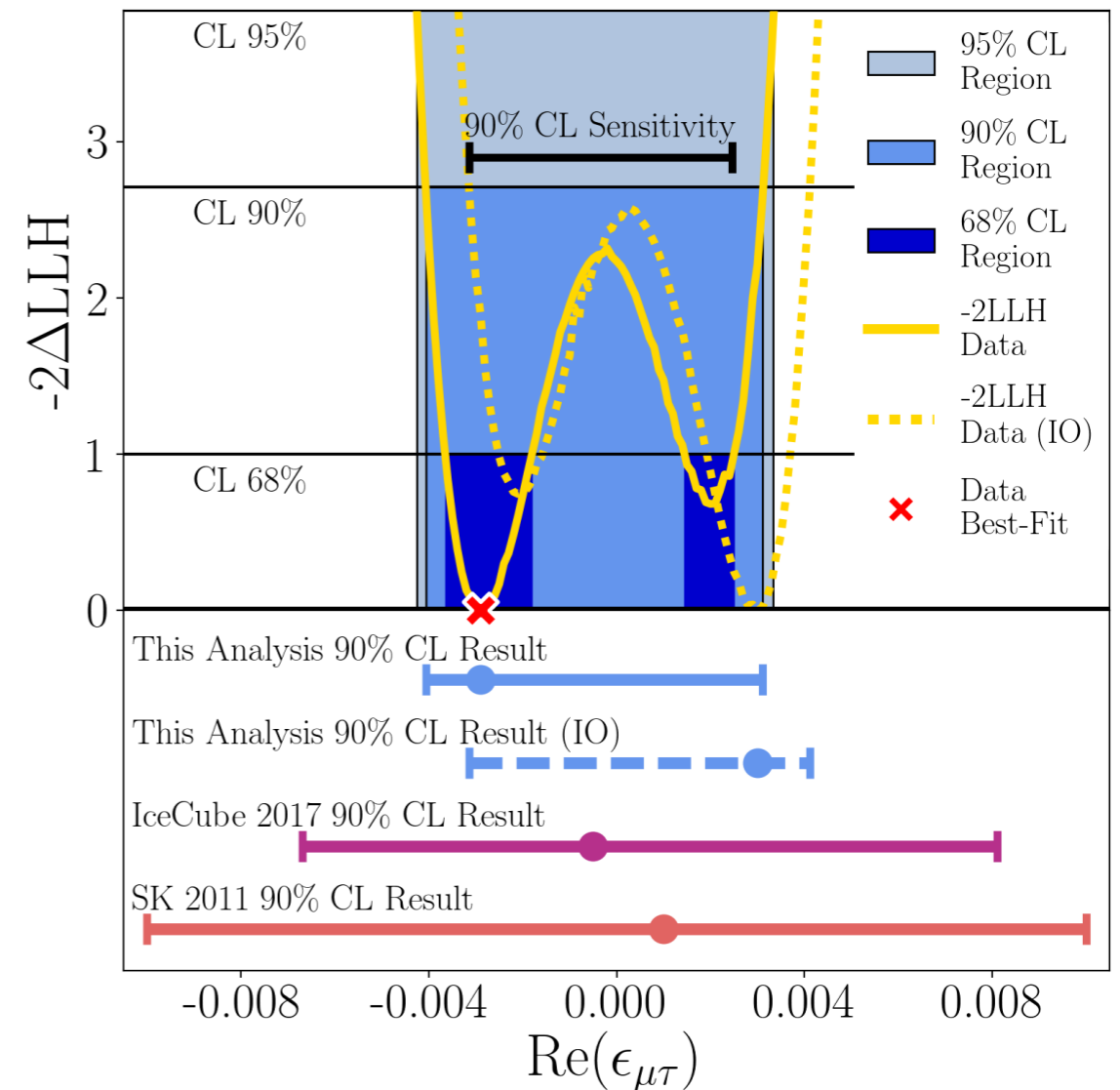
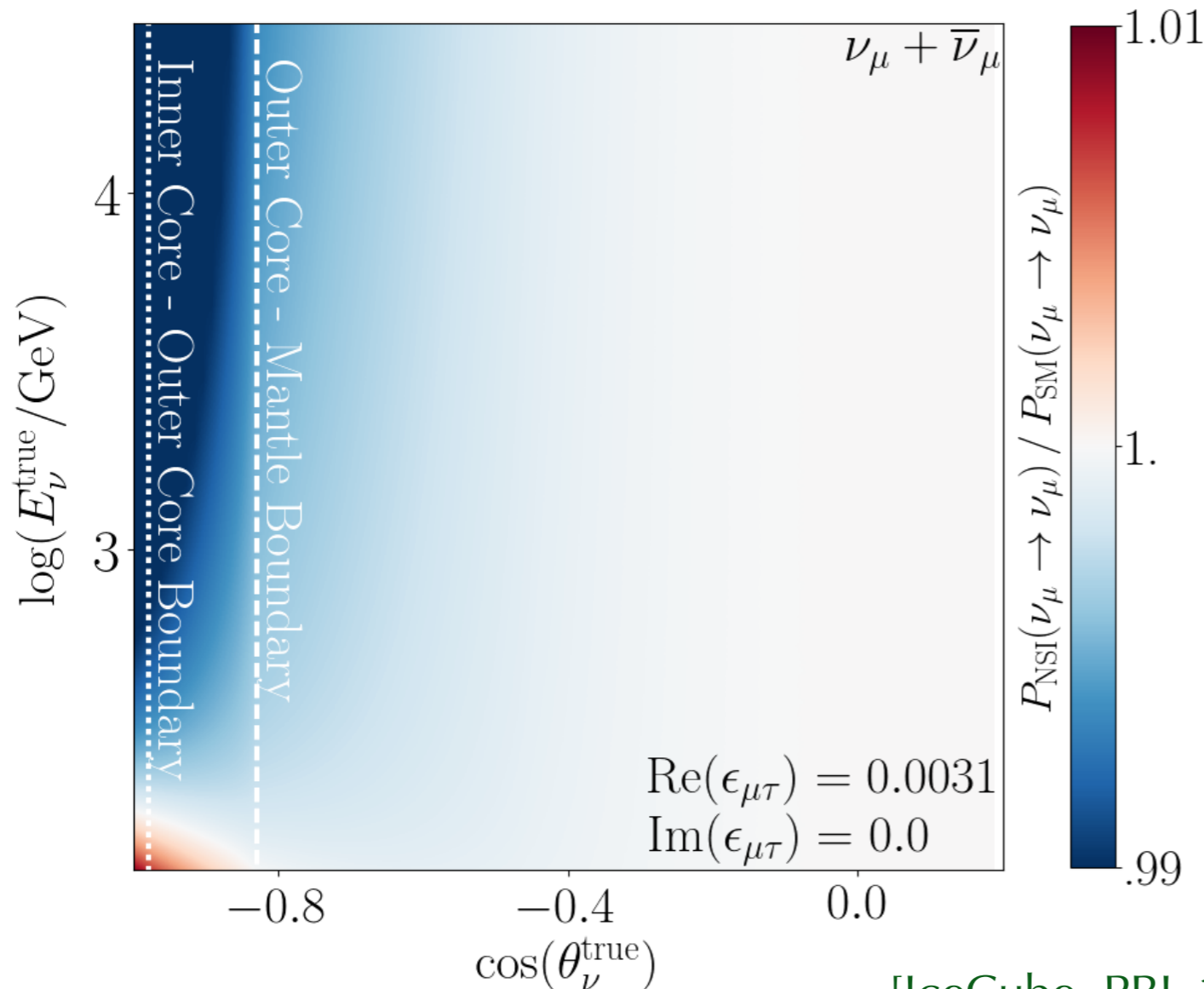


[IceCube, PRL 129 (2022) 1]

Nonstandard Neutrino Interactions

Hamiltonian including nonstandard interactions with matter:

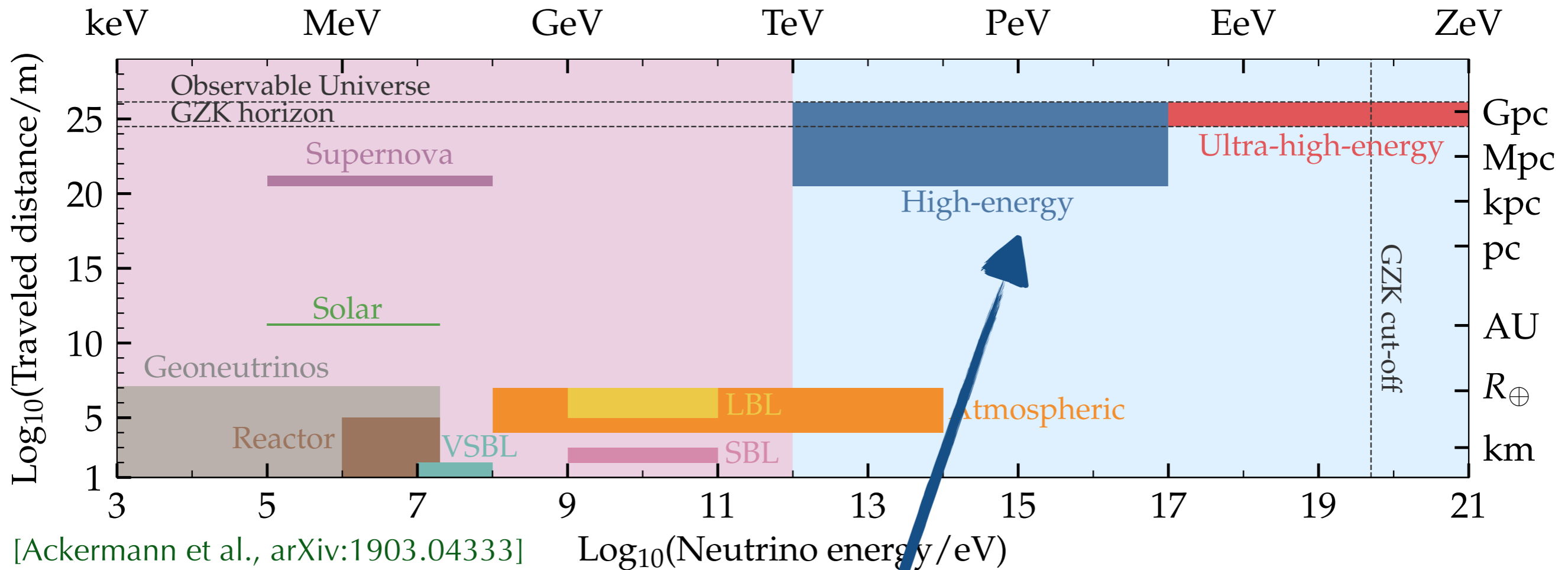
$$H_{\text{mat}}(x) = V_{\text{CC}}(x) \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\mu\tau}^* & \epsilon_{\tau\tau} \end{pmatrix}$$



[IceCube, PRL 129 (2022) 1]

Probe of Fundamental Physics

IceCube neutrinos test new energy and distance regime.



$$H \simeq \sum_i \frac{m_i^2}{2E_\nu} (|\nu_i\rangle\langle\nu_i| + |\bar{\nu}_i\rangle\langle\bar{\nu}_i|) + \left(\frac{E_\nu^n}{\Lambda^n} \right) \sum_a (\epsilon_a |\nu_a\rangle\langle\nu_a| + \bar{\epsilon}_a |\bar{\nu}_a\rangle\langle\bar{\nu}_a|)$$

standard Hamiltonian

"exotic" contributions?

Lorentz Invariance Violation

- Quantum gravity could modify dispersion relations of neutrinos (or photons, CRs, *etc.*) inducing **Lorentz Invariance Violation (LIV)**:

[e.g. Alves Batista et al.'23]

$$E^2 = \mathbf{p}^2 \left[1 \pm \left(\frac{E}{\Lambda} \right)^n \right]$$

- Modification of the **neutrino velocity**:

$$v(E) = \frac{\partial E}{\partial p} \simeq 1 \pm \frac{n+1}{2} \left(\frac{E}{\Lambda} \right)^n$$

- This causes **energy-dependent time delays** of cosmic neutrinos:

$$\Delta t = \pm \frac{n+1}{2} \frac{E_0^n - E_1^n}{\Lambda^n} \int_0^z dz' \frac{(1+z')^n}{H(z')}$$

- TXS 0506+056 ν - γ coincidence constrains $\Lambda \gtrsim 3 \times 10^{16}$ GeV ($n = 1$).

[Ellis, Mavromatos, Sakharov & Sarkisyan-Grinbaum'18; Laha'18]

Lorentz Invariance Violation

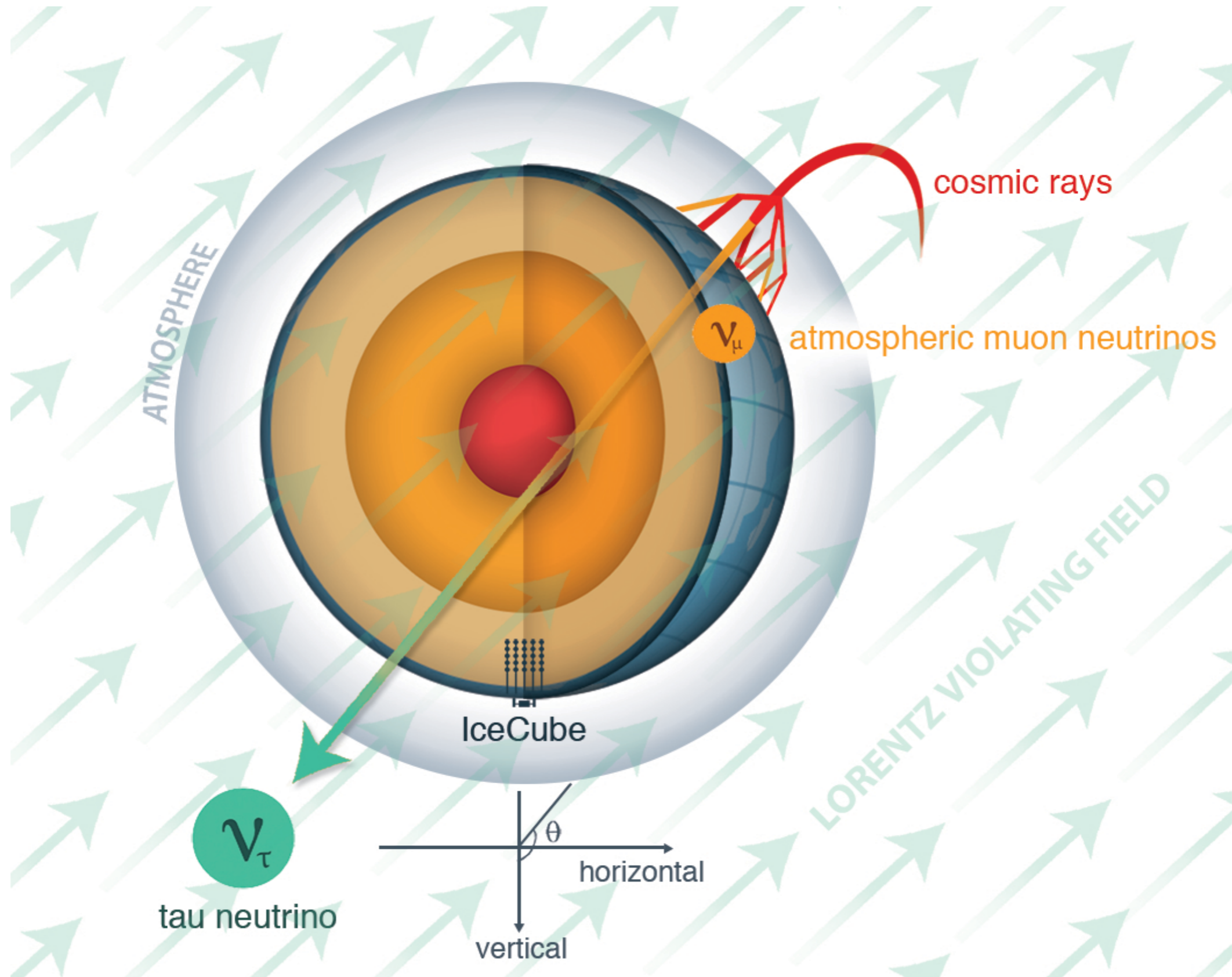
- LIV can also modify neutrino oscillations via an anomalous energy dependence of the effective Hamiltonian.
- For **isotropic LIV effects** we can make the ansatz for the effective Hamiltonian of flavour states: [Kostelecky & Mewes'12]

$$H \simeq \frac{m^2}{2E_\nu} + \hat{a}^{(3)} - E\hat{c}^{(4)} + E^2\hat{a}^{(5)} - E^3\hat{c}^{(6)} + \dots$$

- The LIV 3×3 matrices $a^{(d)}$ are CPT odd and $c^{(d)}$ are CPT even with mass dimension $4 - d$.
- The flavour eigenstates can now be expressed as superpositions of **LIV Hamiltonian eigenstates** $|\nu_\alpha\rangle$:

$$|\nu_\alpha\rangle = \sum_{\mathbf{a}} U_{\alpha\mathbf{a}}^*(E_\nu) |\nu_{\mathbf{a}}\rangle$$

Atmospheric Neutrinos & LIV



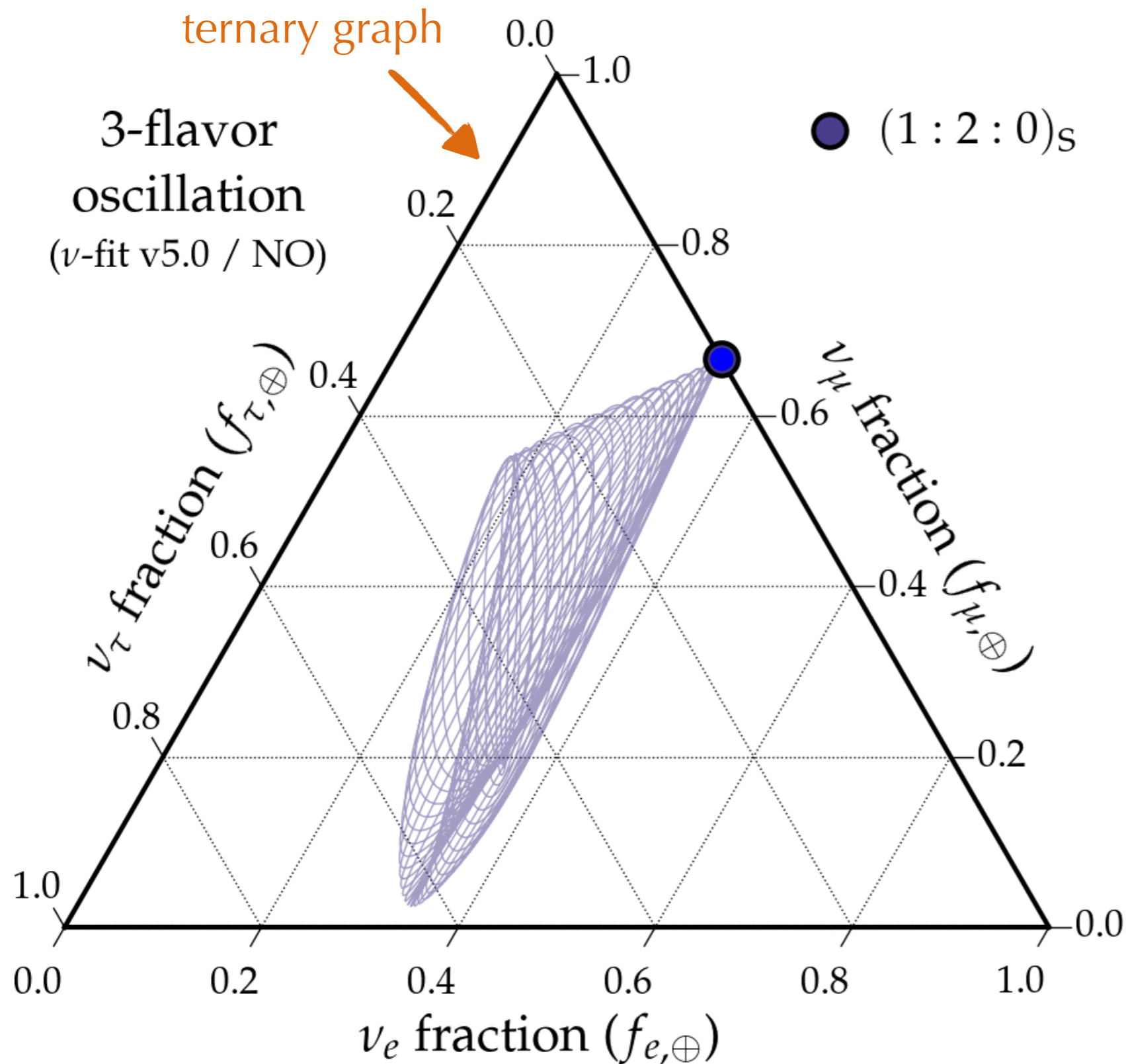
Atmospheric Neutrinos & LIV

Limits on LIV operators using atmospheric neutrinos

dim.	method	type	sector	limits	ref.
3	CMB polarization	astrophysical	photon	$\sim 10^{-43}$ GeV	[5]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}$ GeV	[10]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}$ GeV	[12]
	muon g-2	accelerator	muon	$\sim 10^{-24}$ GeV	[13]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(3)}) , \text{Im}(\hat{a}_{\mu\tau}^{(3)}) $ $< 2.9 \times 10^{-24}$ GeV (99% C.L.) $< 2.0 \times 10^{-24}$ GeV (90% C.L.)	this work
4	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[6]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[7]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[8]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[11]
	trapped Ca^+ ion	tabletop	electron	$\sim 10^{-19}$	[14]
neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(4)}) , \text{Im}(\hat{c}_{\mu\tau}^{(4)}) $ $< 3.9 \times 10^{-28}$ (99% C.L.) $< 2.7 \times 10^{-28}$ (90% C.L.)	this work	
5	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}$ GeV $^{-1}$	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV $^{-1}$	[9]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(5)}) , \text{Im}(\hat{a}_{\mu\tau}^{(5)}) $ $< 2.3 \times 10^{-32}$ GeV $^{-1}$ (99% C.L.) $< 1.5 \times 10^{-32}$ GeV $^{-1}$ (90% C.L.)	this work
6	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-31}$ GeV $^{-2}$	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV $^{-2}$	[9]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31}$ GeV $^{-2}$	[15]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(6)}) , \text{Im}(\hat{c}_{\mu\tau}^{(6)}) $ $< 1.5 \times 10^{-36}$ GeV $^{-2}$ (99% C.L.) $< 9.1 \times 10^{-37}$ GeV $^{-2}$ (90% C.L.)	this work
7	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-28}$ GeV $^{-3}$	[6]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(7)}) , \text{Im}(\hat{a}_{\mu\tau}^{(7)}) $ $< 8.3 \times 10^{-41}$ GeV $^{-3}$ (99% C.L.) $< 3.6 \times 10^{-41}$ GeV $^{-3}$ (90% C.L.)	this work
8	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-46}$ GeV $^{-4}$	[15]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(8)}) , \text{Im}(\hat{c}_{\mu\tau}^{(8)}) $ $< 5.2 \times 10^{-45}$ GeV $^{-4}$ (99% C.L.) $< 1.4 \times 10^{-45}$ GeV $^{-4}$ (90% C.L.)	this work

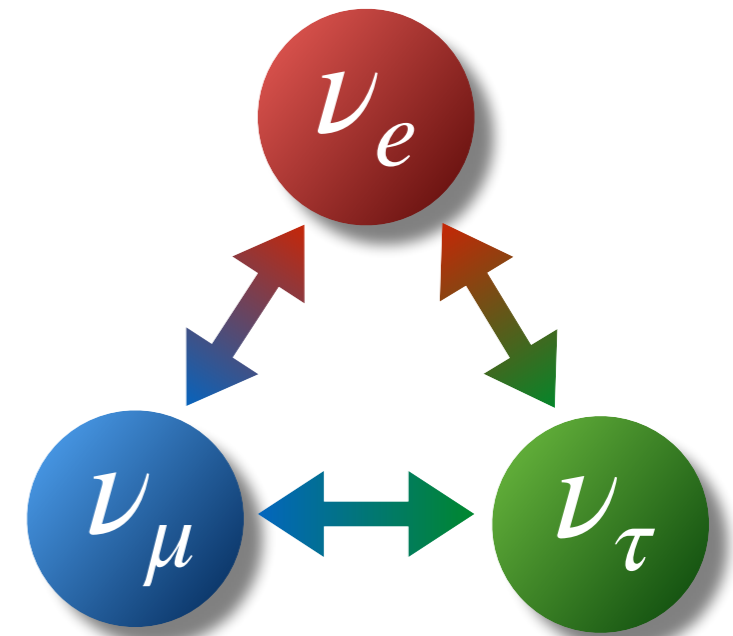
[IceCube, Nature Phys. 14 (2018) 9]

Cosmic Neutrinos & LIV



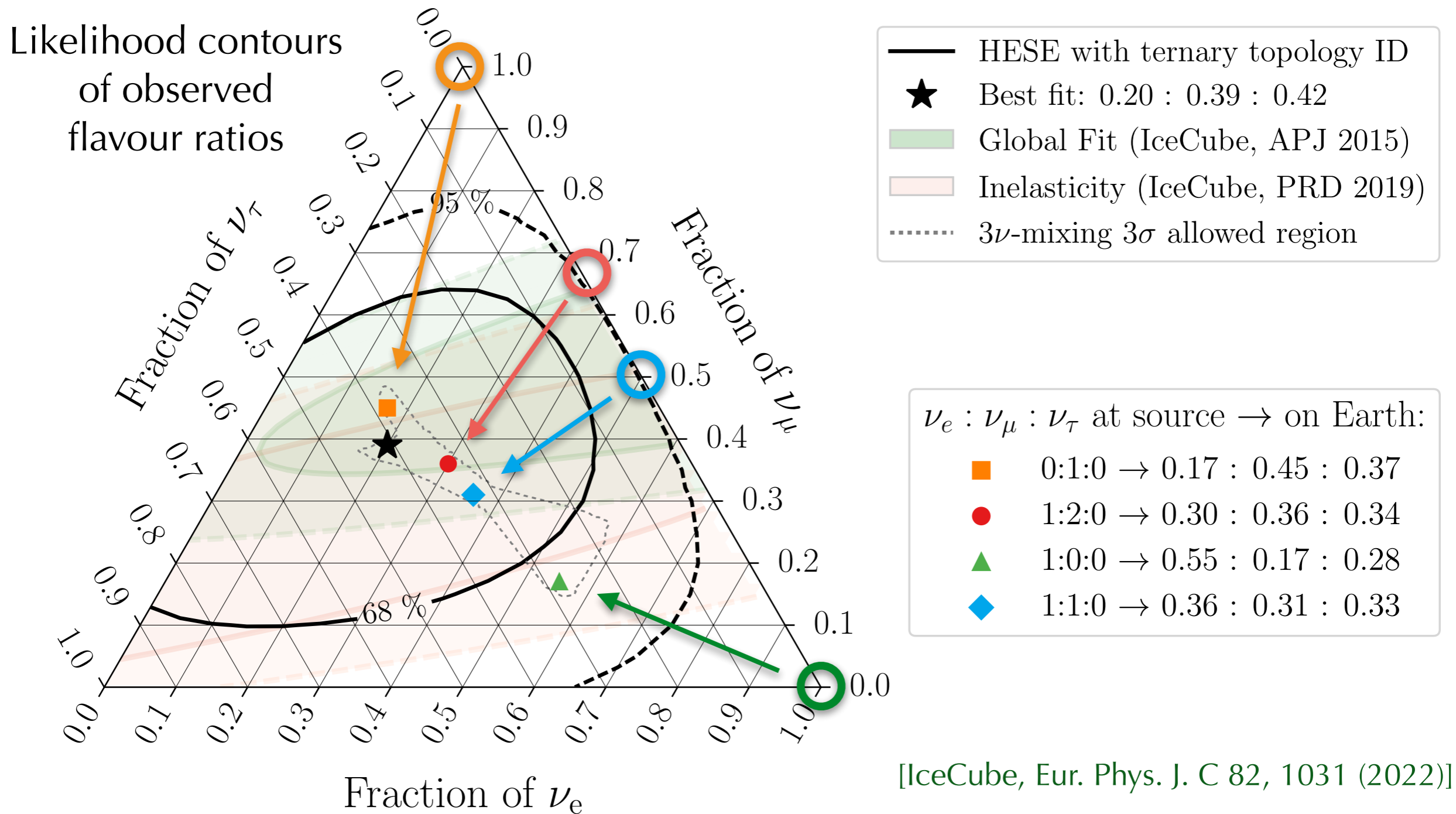
flavour ratios
on production

Superposition of
flavour and mass states
induce oscillations.

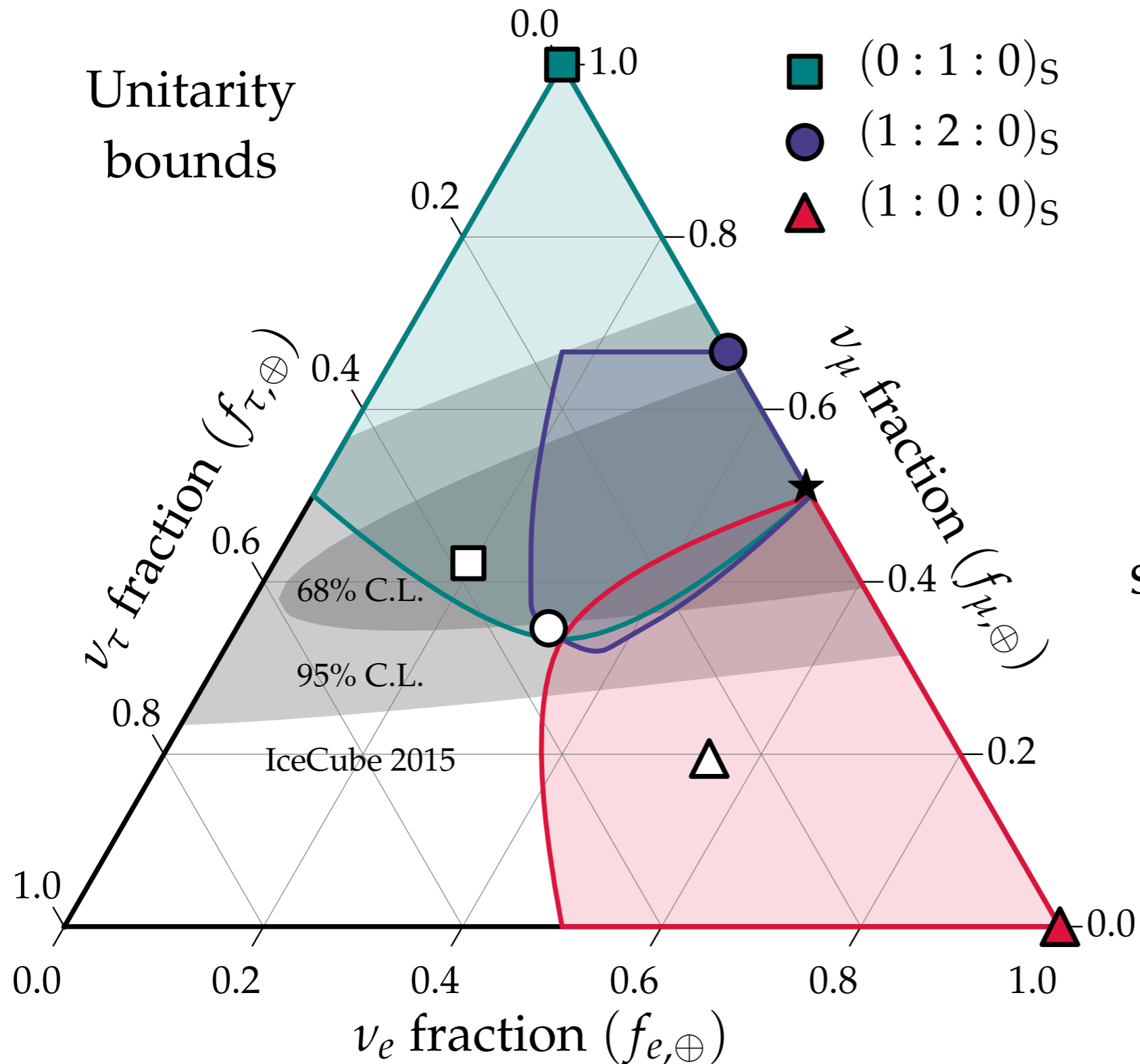


Cosmic Neutrinos & LIV

Cosmic neutrinos visible via their oscillation-averaged flavour.



Cosmic Neutrinos & LIV



unitary mixing matrix

$$U^\dagger U = 1$$

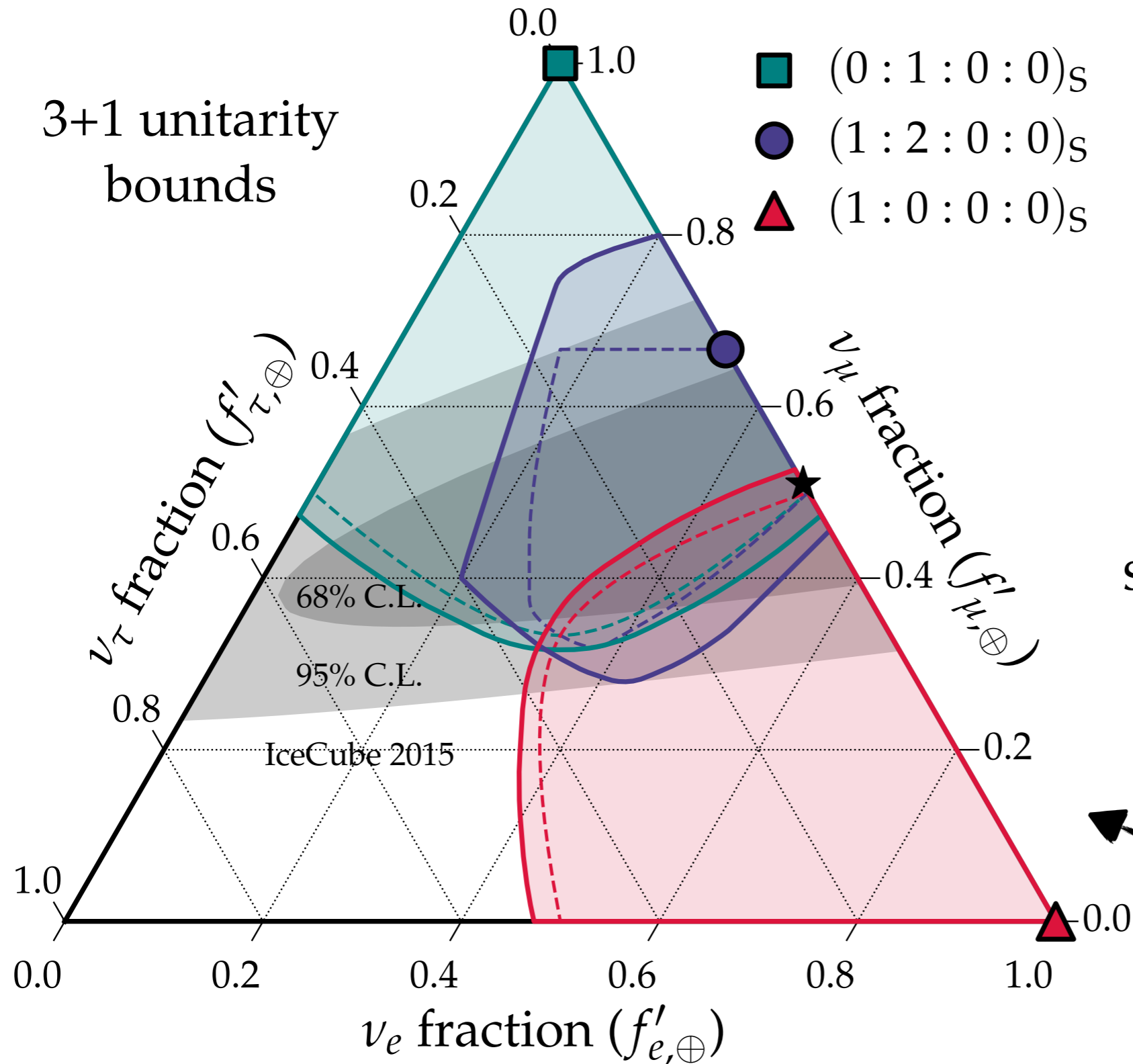


$$|\nu_\alpha\rangle = \sum_a U_{\alpha a}^* |\nu_a\rangle$$

superposition of flavor and LIV eigenstates

[MA, Bustamante & Mu'18]

Cosmic Neutrinos & LIV



unitary mixing matrix

$$U^\dagger U = 1$$



$$|\nu_\alpha\rangle = \sum_a U_{\alpha a}^* |\nu_a\rangle$$

superposition of flavor
and LIV eigenstates

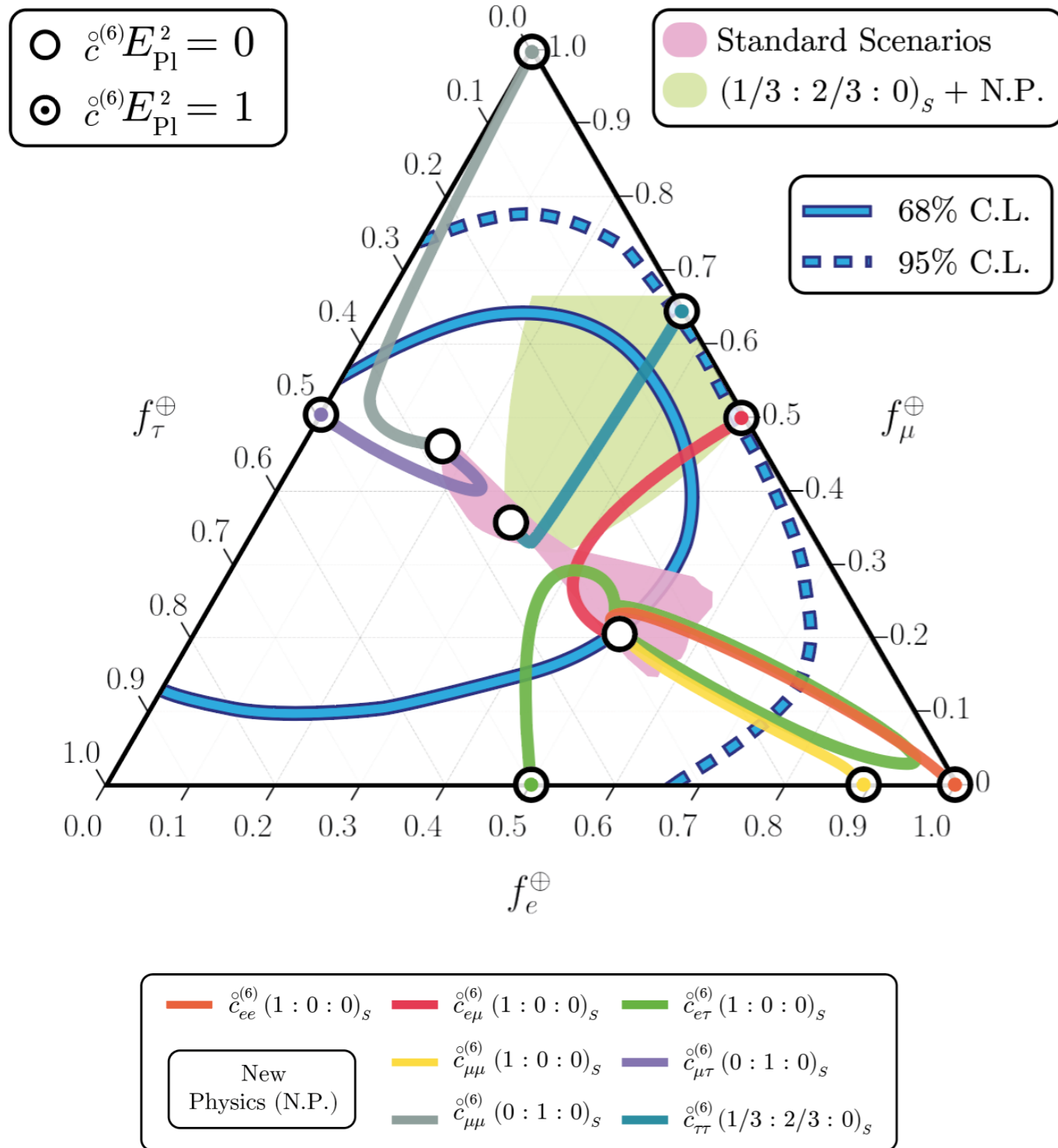
+ 1 sterile neutrino

$$f'_\alpha \equiv \frac{f_\alpha}{1 - f_s}$$

active flavor ratios

[MA, Bustamante & Willesen'21]

Cosmic Neutrinos & LIV



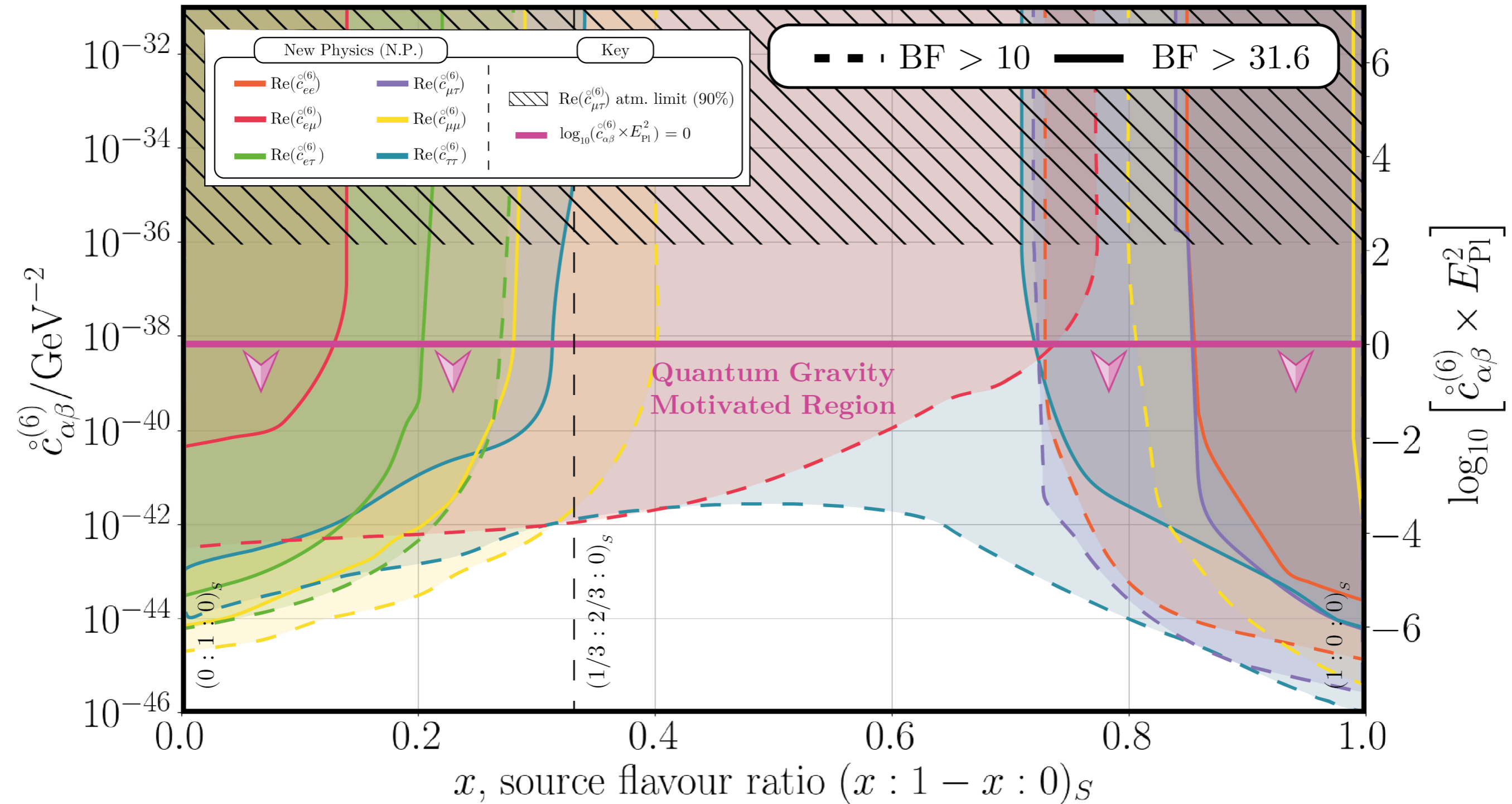
Limits on LIV operators using cosmic neutrinos

dim	coefficient	limit	dim	coefficient	limit	$(\phi_e^i : \phi_\mu^i : \phi_\tau^i)_S$
3	$\text{Re}(a_{e\mu}^{(5)})$	$6 \times 10^{-26} \text{ GeV}$	4	$\text{Re}(c_{e\mu}^{(6)})$	2×10^{-31}	$(0:1:0)_S$
	$\text{Re}(a_{e\tau}^{(5)})$	$3 \times 10^{-27} \text{ GeV}$		$\text{Re}(c_{e\tau}^{(6)})$	7×10^{-33}	$(0:1:0)_S$
	$\text{Re}(a_{\mu\mu}^{(5)})$	$3 \times 10^{-27} \text{ GeV}$		$\text{Re}(c_{\mu\mu}^{(6)})$	4×10^{-33}	$(0:1:0)_S$
	$\text{Re}(a_{\tau\tau}^{(5)})$	$5 \times 10^{-27} \text{ GeV}$		$\text{Re}(c_{\tau\tau}^{(6)})$	1×10^{-32}	$(0:1:0)_S$
	$\text{Re}(a_{ee}^{(3)})$	$4 \times 10^{-28} \text{ GeV}$		$\text{Re}(c_{ee}^{(4)})$	6×10^{-33}	$(1:0:0)_S$
	$\text{Re}(a_{\mu\tau}^{(3)})$	$6 \times 10^{-27} \text{ GeV}$		$\text{Re}(c_{\mu\tau}^{(4)})$	7×10^{-34}	$(1:0:0)_S$
	$\text{Re}(a_{\tau\tau}^{(3)})$	$2 \times 10^{-27} \text{ GeV}$		$\text{Re}(c_{\tau\tau}^{(4)})$	8×10^{-34}	$(1:0:0)_S$
5	$\text{Re}(a_{e\mu}^{(5)})$	$3 \times 10^{-36} \text{ GeV}^{-1}$	6	$\text{Re}(c_{e\mu}^{(6)})$	$4 \times 10^{-41} \text{ GeV}^{-2}$	$(0:1:0)_S$
	$\text{Re}(a_{e\tau}^{(5)})$	$9 \times 10^{-39} \text{ GeV}^{-1}$		$\text{Re}(c_{e\tau}^{(6)})$	$3 \times 10^{-44} \text{ GeV}^{-2}$	$(0:1:0)_S$
	$\text{Re}(a_{\mu\mu}^{(5)})$	$8 \times 10^{-39} \text{ GeV}^{-1}$		$\text{Re}(c_{\mu\mu}^{(6)})$	$7 \times 10^{-45} \text{ GeV}^{-2}$	$(0:1:0)_S$
	$\text{Re}(a_{\tau\tau}^{(5)})$	$3 \times 10^{-38} \text{ GeV}^{-1}$		$\text{Re}(c_{\tau\tau}^{(6)})$	$1 \times 10^{-43} \text{ GeV}^{-2}$	$(0:1:0)_S$
	$\text{Re}(a_{\tau\tau}^{(5)})$	$2 \times 10^{-35} \text{ GeV}^{-1}$		$\text{Re}(c_{\tau\tau}^{(6)})$	$3 \times 10^{-36} \text{ GeV}^{-2}$	$(1/3:2/3:0)_S$
	$\text{Re}(a_{ee}^{(5)})$	$7 \times 10^{-40} \text{ GeV}^{-1}$		$\text{Re}(c_{ee}^{(6)})$	$2 \times 10^{-44} \text{ GeV}^{-2}$	$(1:0:0)_S$
	$\text{Re}(a_{\mu\tau}^{(5)})$	$4 \times 10^{-39} \text{ GeV}^{-1}$		$\text{Re}(c_{\mu\tau}^{(6)})$	$6 \times 10^{-45} \text{ GeV}^{-2}$	$(1:0:0)_S$
$\text{Re}(a_{\tau\tau}^{(5)})$	$2 \times 10^{-38} \text{ GeV}^{-1}$	$\text{Re}(c_{\tau\tau}^{(6)})$	$6 \times 10^{-45} \text{ GeV}^{-2}$	$(1:0:0)_S$		
7	$\text{Re}(a_{e\mu}^{(7)})$	$5 \times 10^{-46} \text{ GeV}^{-3}$	8	$\text{Re}(c_{e\mu}^{(8)})$	$1 \times 10^{-50} \text{ GeV}^{-4}$	$(0:1:0)_S$
	$\text{Re}(a_{e\tau}^{(7)})$	$4 \times 10^{-50} \text{ GeV}^{-3}$		$\text{Re}(c_{e\tau}^{(8)})$	$6 \times 10^{-56} \text{ GeV}^{-4}$	$(0:1:0)_S$
	$\text{Re}(a_{\mu\mu}^{(7)})$	$4 \times 10^{-50} \text{ GeV}^{-3}$		$\text{Re}(c_{\mu\mu}^{(8)})$	$5 \times 10^{-56} \text{ GeV}^{-4}$	$(0:1:0)_S$
	$\text{Re}(a_{\tau\tau}^{(7)})$	$2 \times 10^{-49} \text{ GeV}^{-3}$		$\text{Re}(c_{\tau\tau}^{(8)})$	$6 \times 10^{-55} \text{ GeV}^{-4}$	$(0:1:0)_S$
	$\text{Re}(a_{ee}^{(7)})$	$3 \times 10^{-45} \text{ GeV}^{-3}$		$\text{Re}(c_{ee}^{(8)})$	$3 \times 10^{-49} \text{ GeV}^{-4}$	$(1/3:2/3:0)_S$
	$\text{Re}(a_{\mu\tau}^{(7)})$	$8 \times 10^{-51} \text{ GeV}^{-3}$		$\text{Re}(c_{\mu\tau}^{(8)})$	$3 \times 10^{-55} \text{ GeV}^{-4}$	$(1:0:0)_S$
	$\text{Re}(a_{\tau\tau}^{(7)})$	$2 \times 10^{-49} \text{ GeV}^{-3}$		$\text{Re}(c_{\tau\tau}^{(8)})$	$5 \times 10^{-55} \text{ GeV}^{-4}$	$(1:0:0)_S$
	$3 \times 10^{-49} \text{ GeV}^{-3}$		$8 \times 10^{-56} \text{ GeV}^{-4}$	$(1:0:0)_S$		

[IceCube, Nature 18 (2022) 11]

Cosmic Neutrinos & LIV

Limits on the **dimension-six operator**.



[IceCube, Nature 18 (2022) 11]

Neutrino Decoherence

- Quantum gravity could also induce decoherence in the evolution of the neutrino density operator:

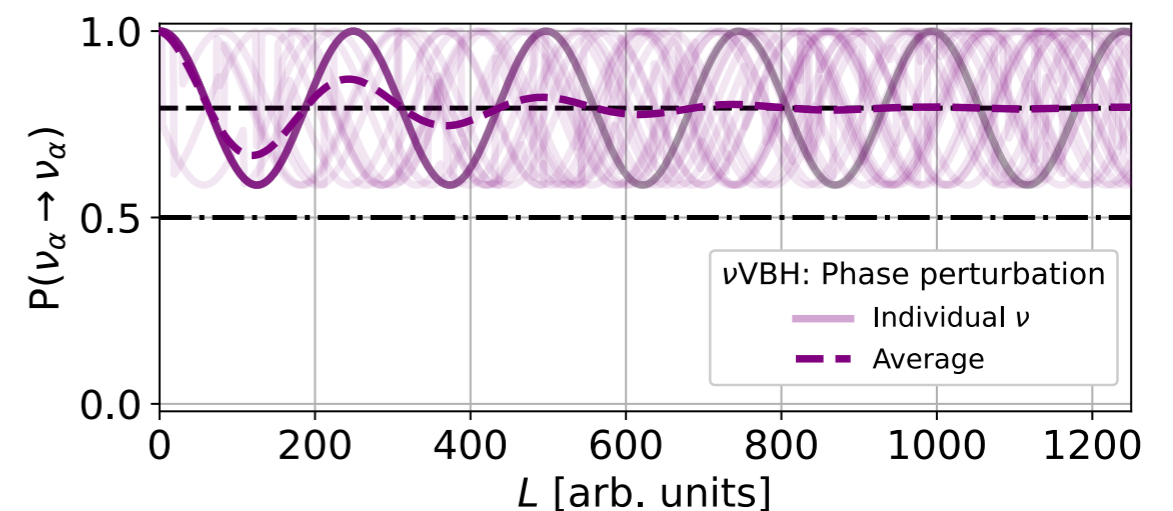
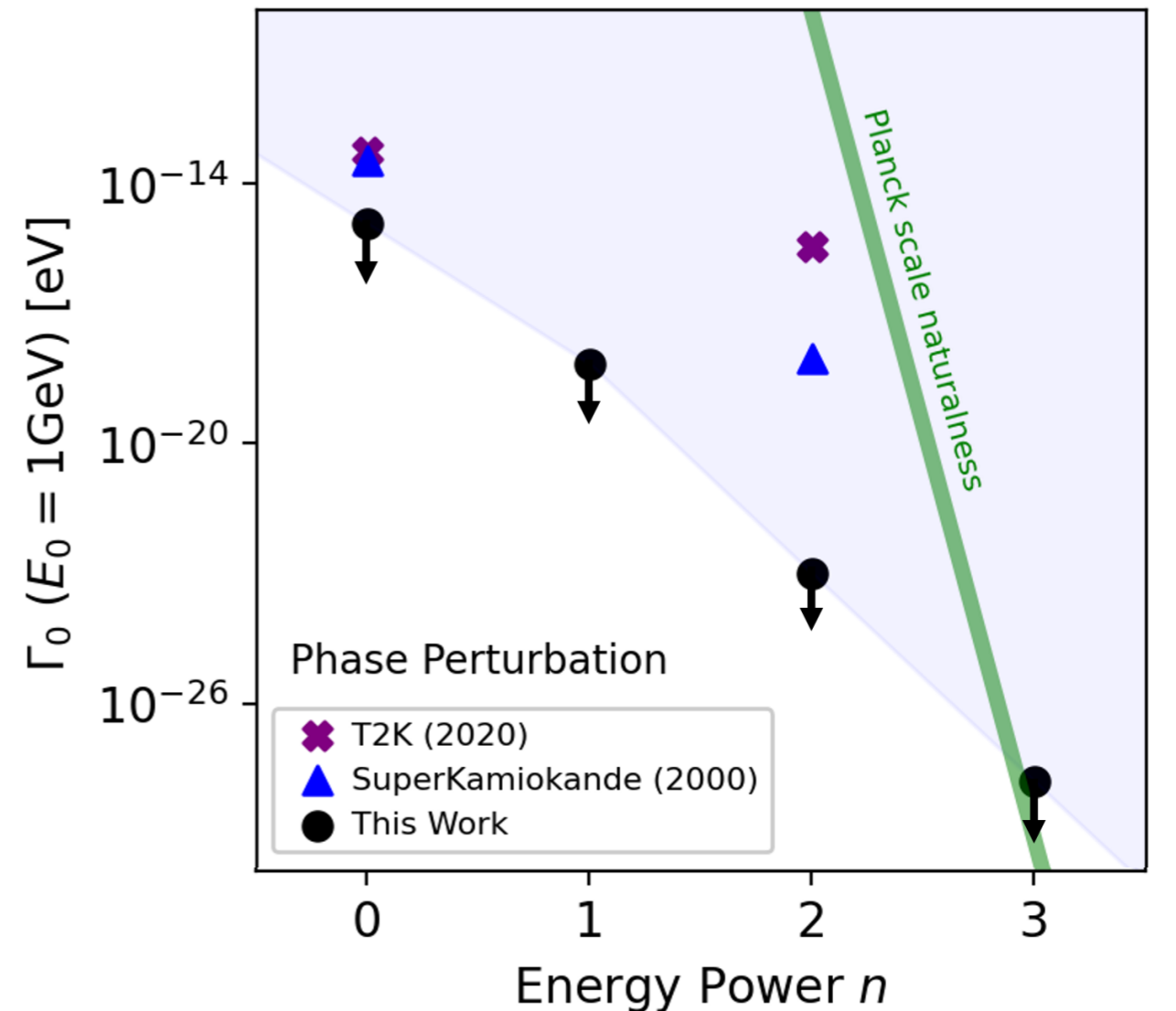
$$\dot{\rho} = -i[H, \rho] - \mathcal{D}[\rho]$$

- The non-unitary **decoherence term** $\mathcal{D}[\rho]$ can be parametrized via **Lindblad operators**.

- For instance, uniform decoherence in the basis of mass eigenstates:

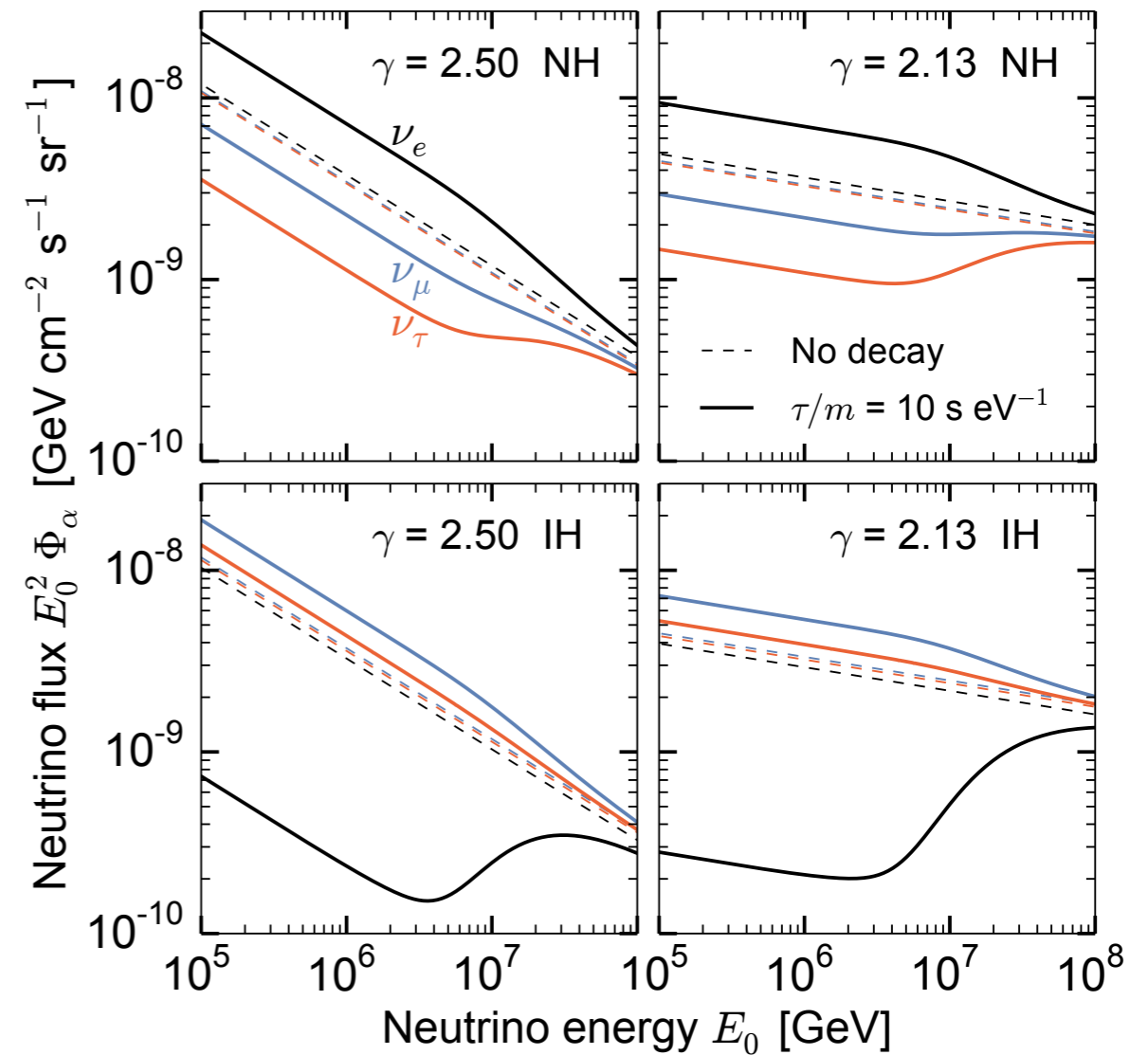
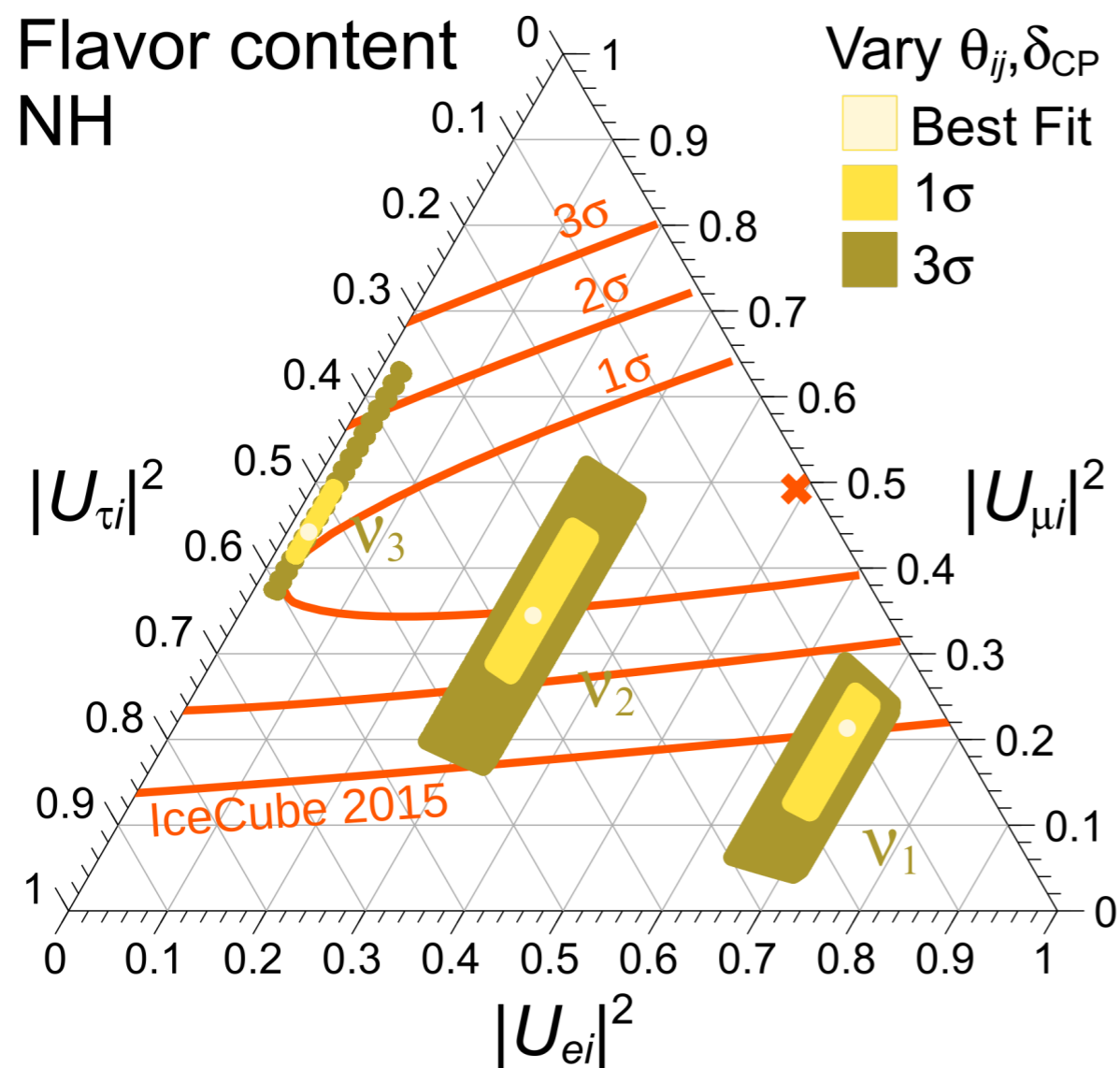
$$\mathcal{D}(\rho) = \Gamma_0 \left(\frac{E_\nu}{E_0} \right)^n \begin{pmatrix} 0 & \rho_{12} & \rho_{13} \\ \rho_{21} & 0 & \rho_{23} \\ \rho_{31} & \rho_{32} & 0 \end{pmatrix}$$

[IceCube, arXiv:2308.00105]



Visible Neutrino Decay

Slow decay of neutrino mass states $\nu_i \rightarrow \nu_j + X$ over cosmological time scales impacts neutrino **flavour fractions** (left) and **spectra** (right).

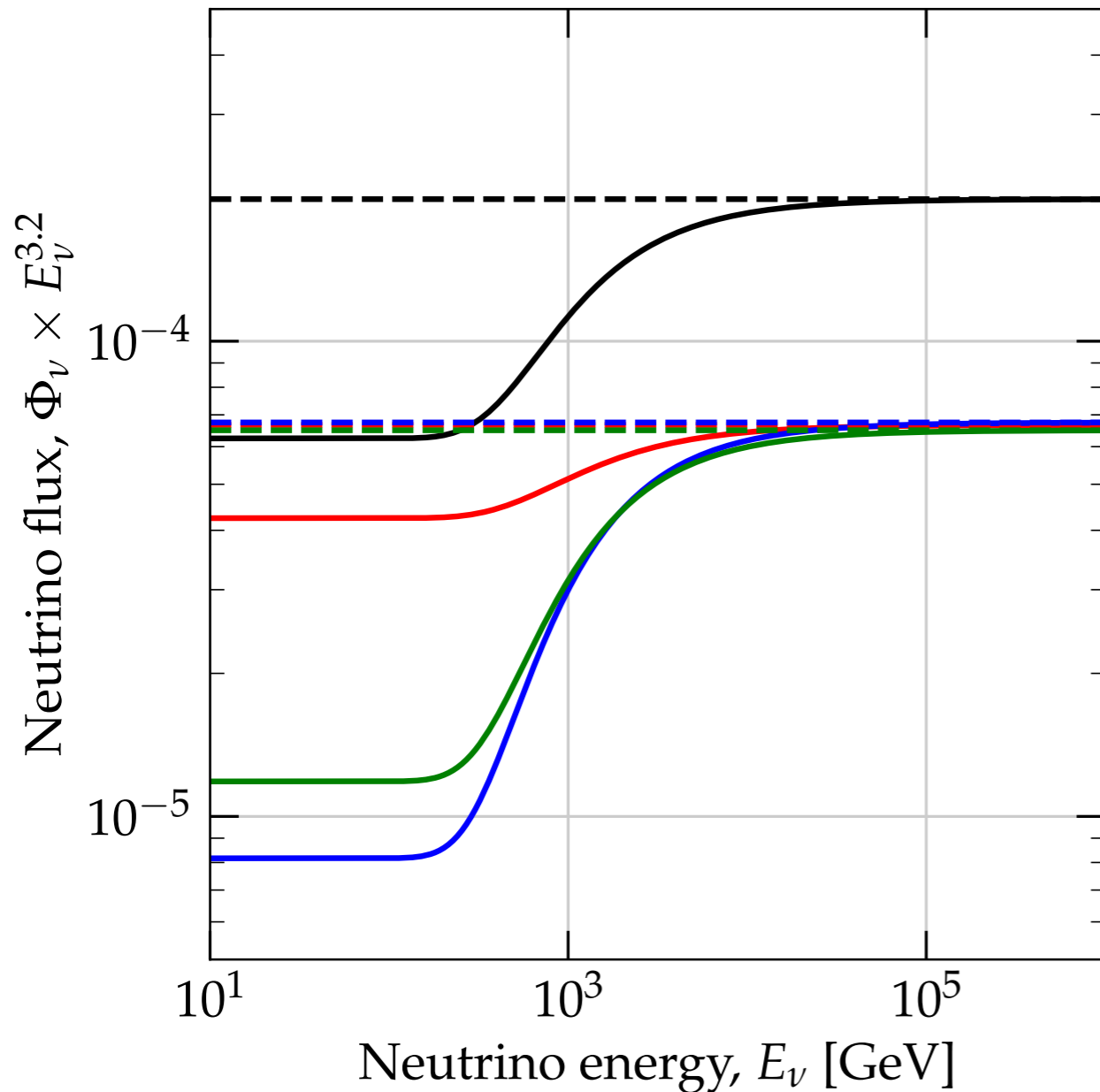


[Bustamante, Beacom & Murase'17]

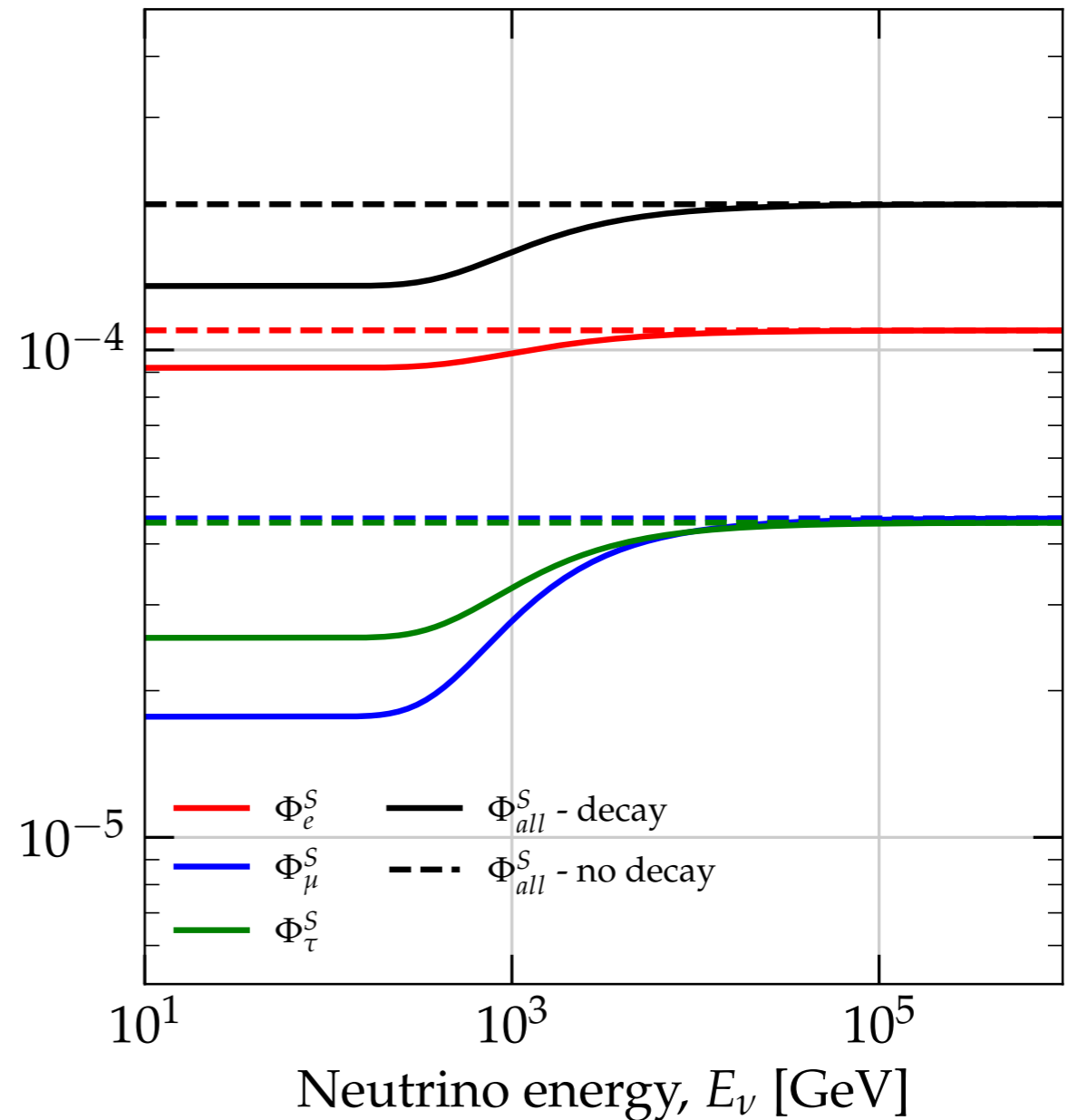
Visible Neutrino Decay

Energy-dependent flavour ratios testable with IceCube-Gen2.

$$f_{\alpha}^S = (0.33:0.67:0)$$

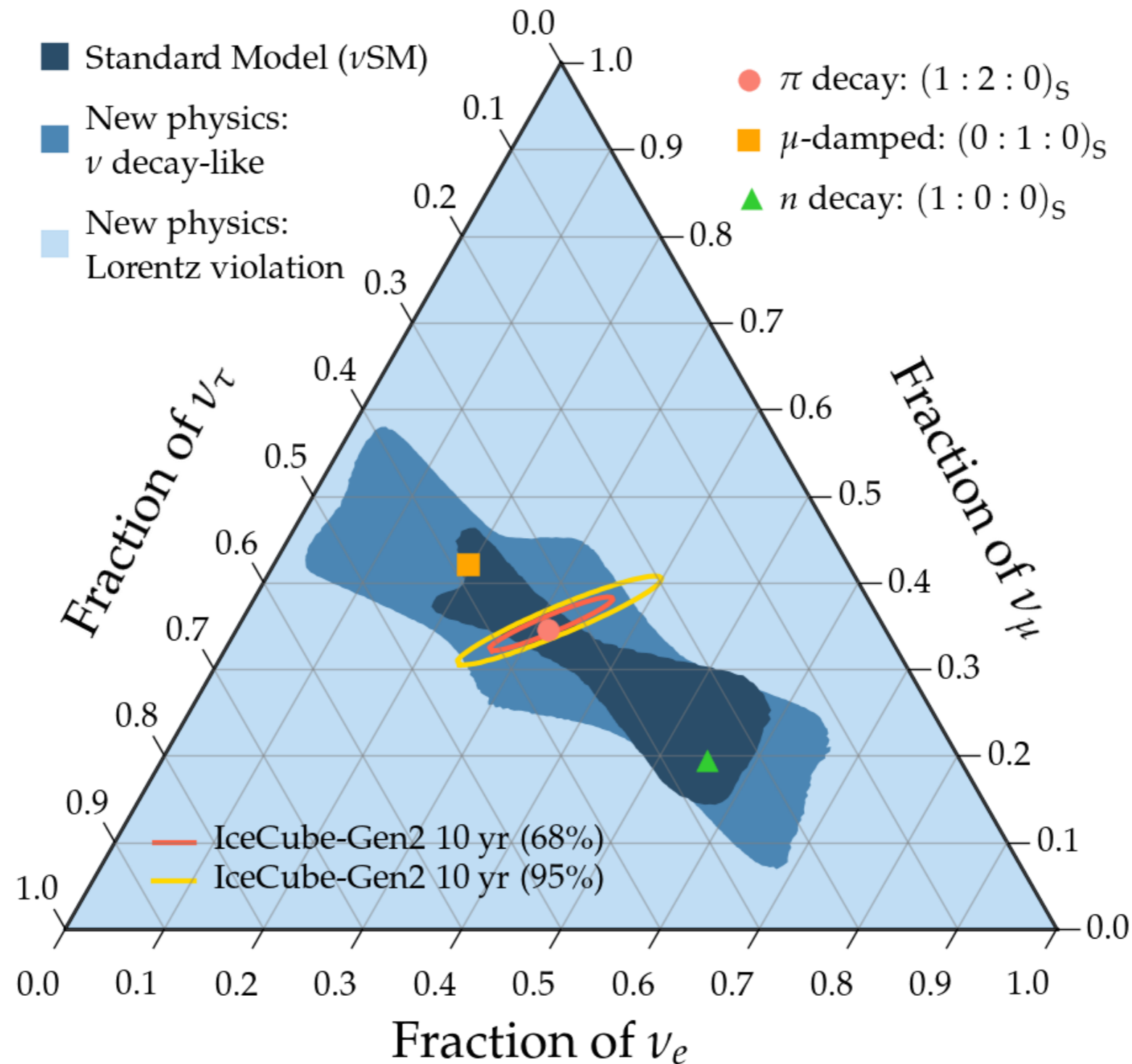


$$f_{\alpha}^S = (1:0:0)$$



[Valera, Fiorillo, Esteban & Bustamante'23]

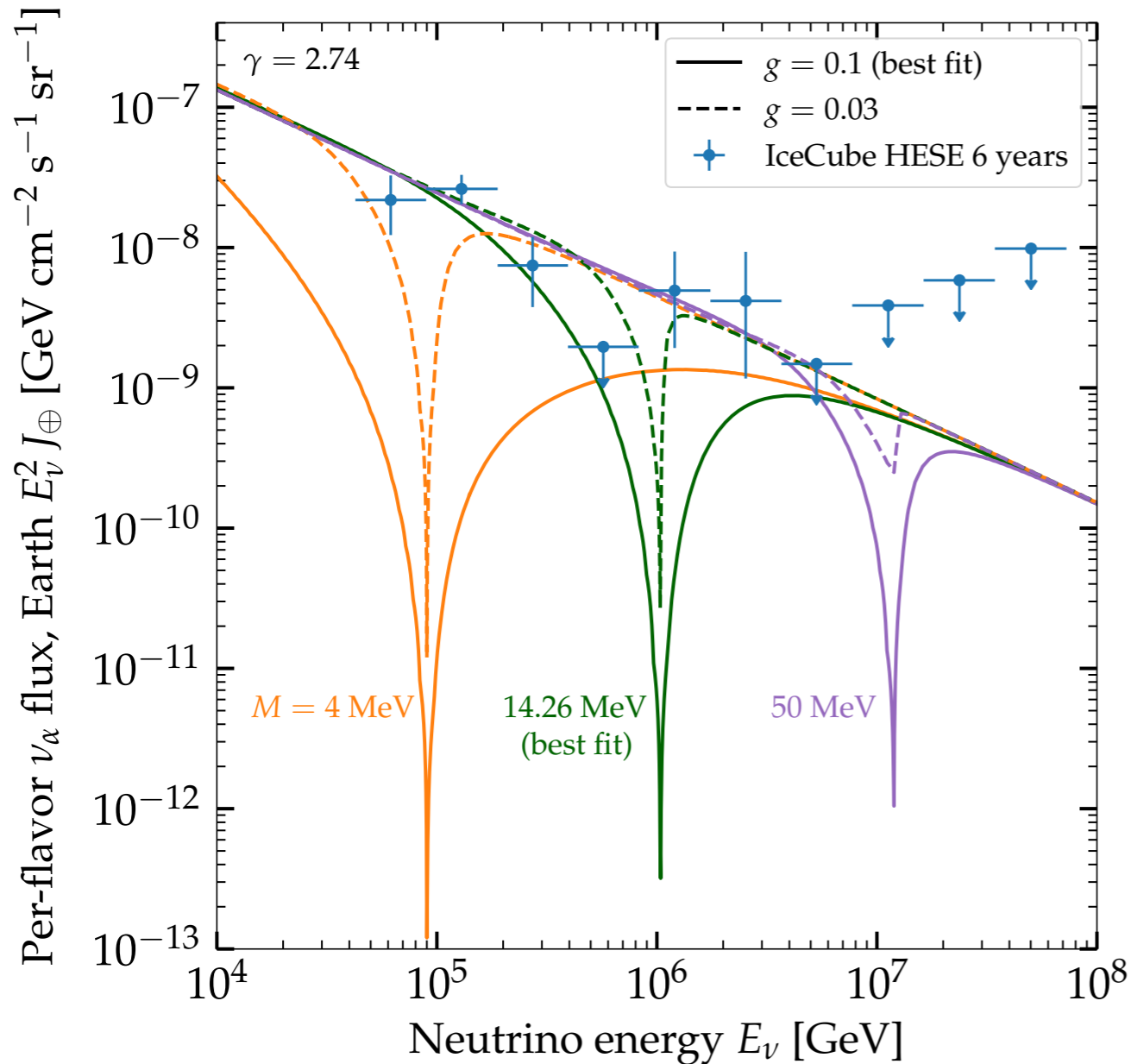
IceCube-Gen2 Flavour Sensitivity



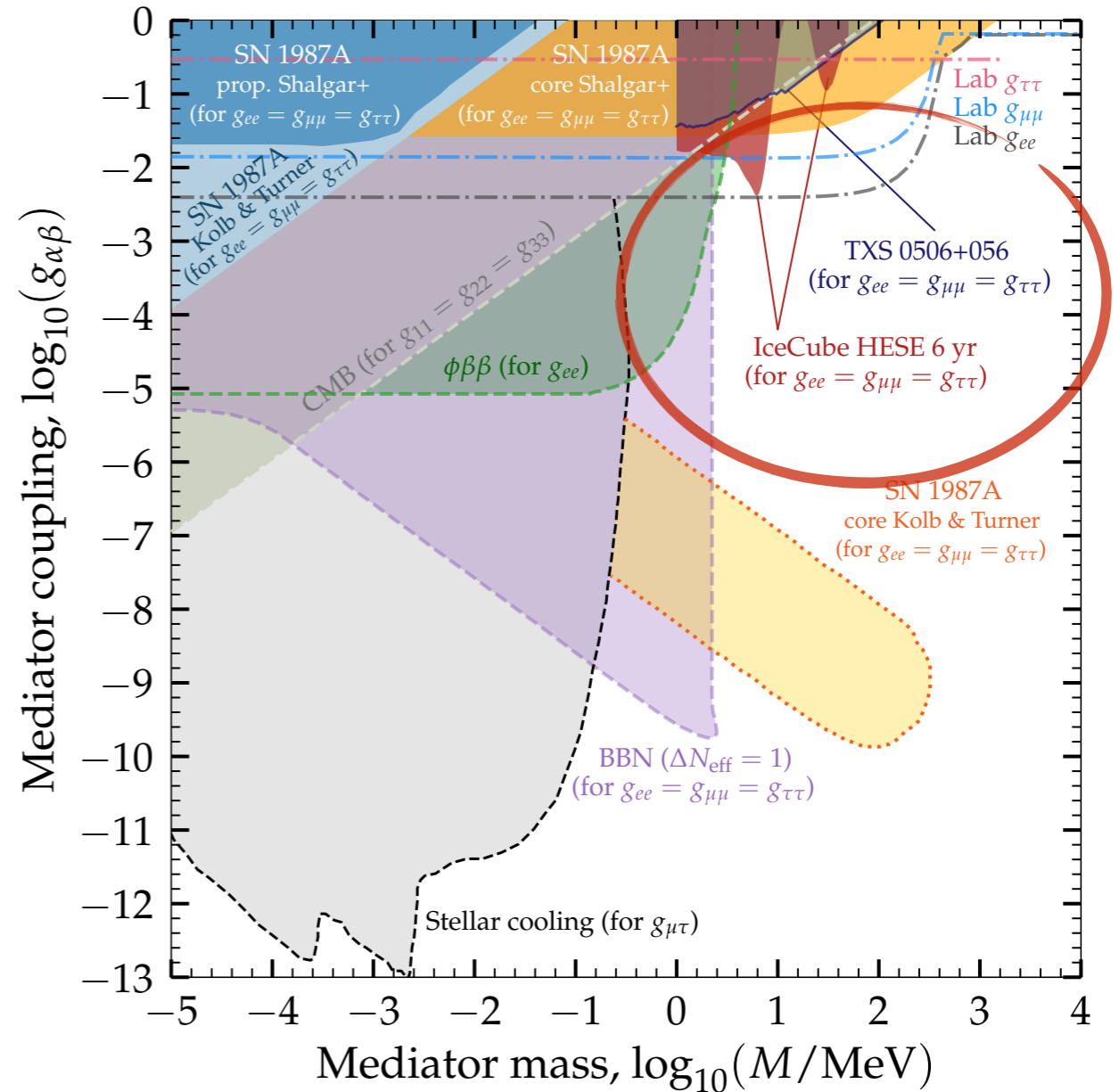
[IceCube-Gen2 *Technical Design Report*: icecube-gen2.wisc.edu/science/publications/tdr/]

Neutrino Self Interactions

Neutrino self interactions can modify cosmic neutrino emission, for instance, by resonant scattering on the $C\nu B$.

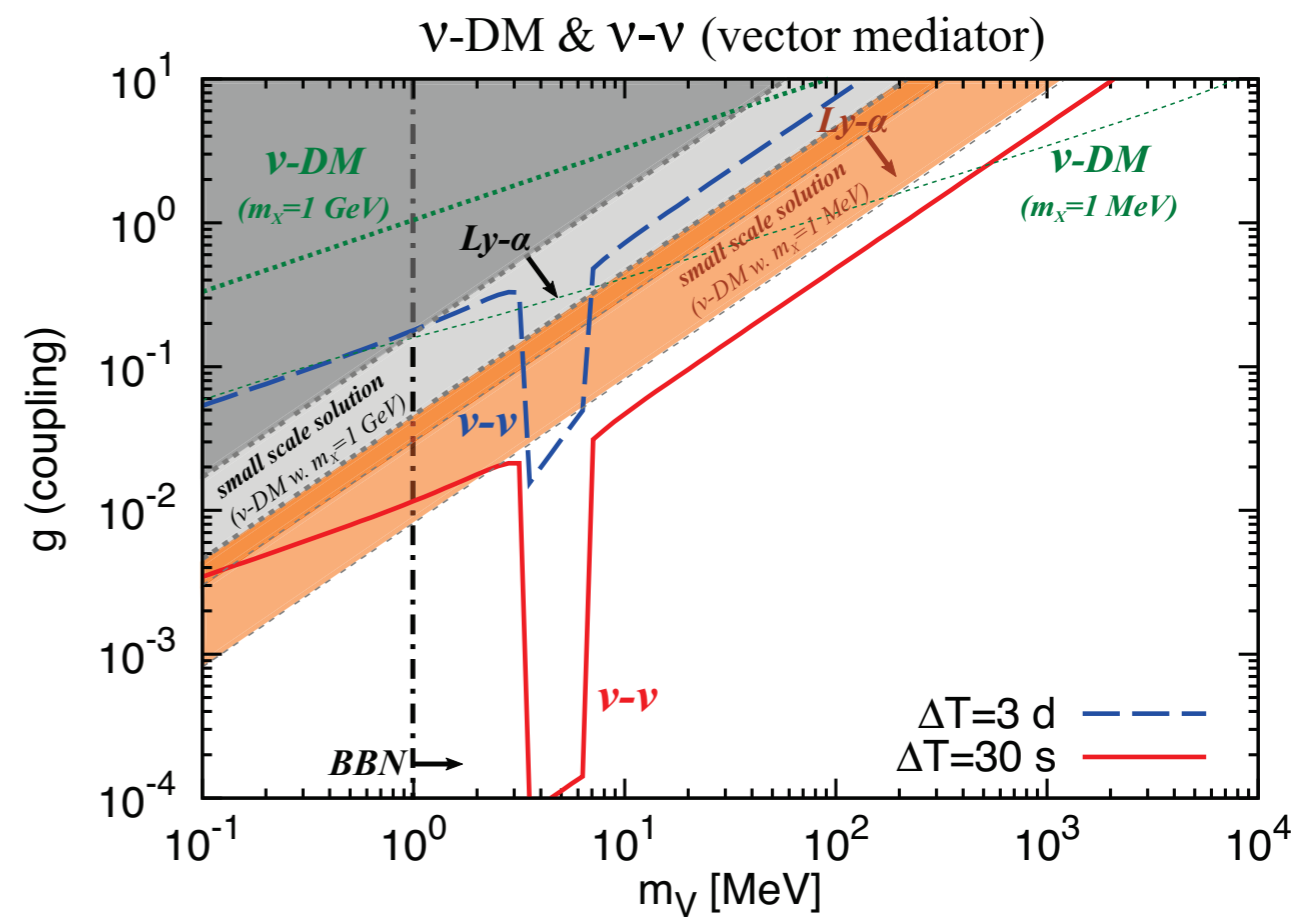
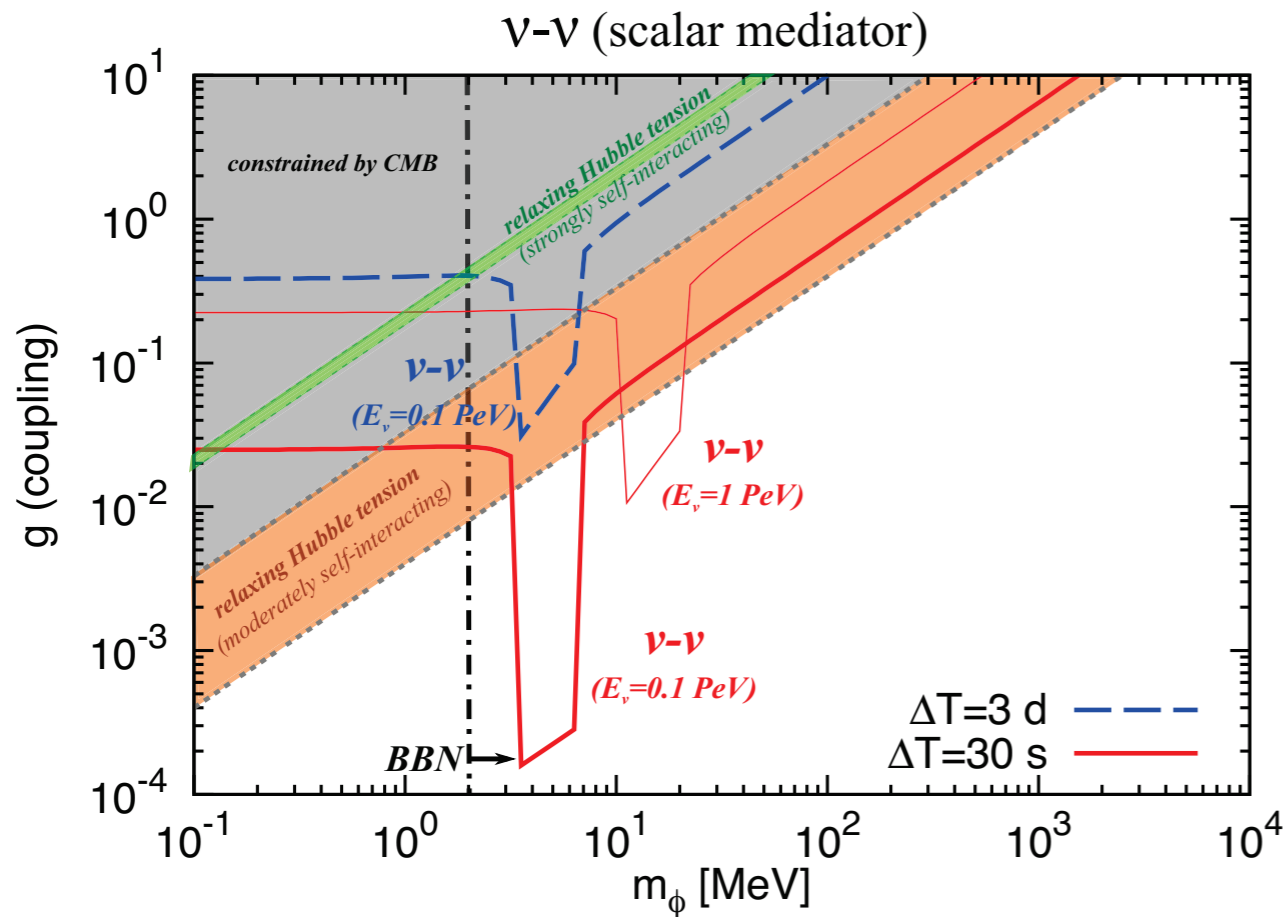


[Bustamante, Rosenstroem, Shalgar & Tamborra'20]

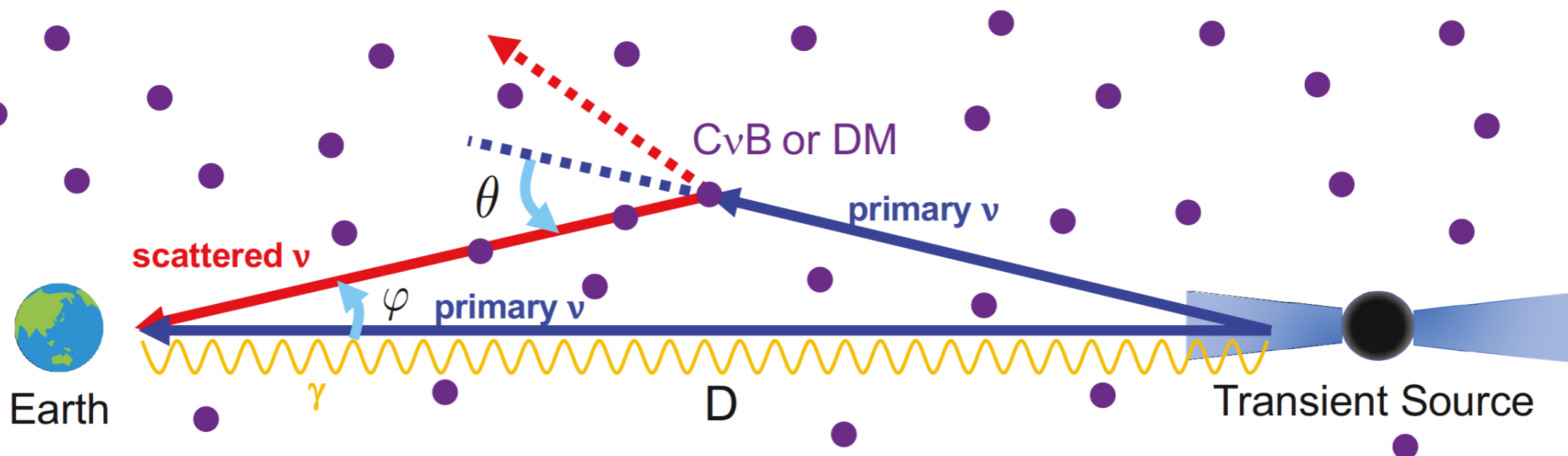


[Blinov, Bustamante, Kell & Zhang'22]

Neutrino "Echos" in TXS 0506+056

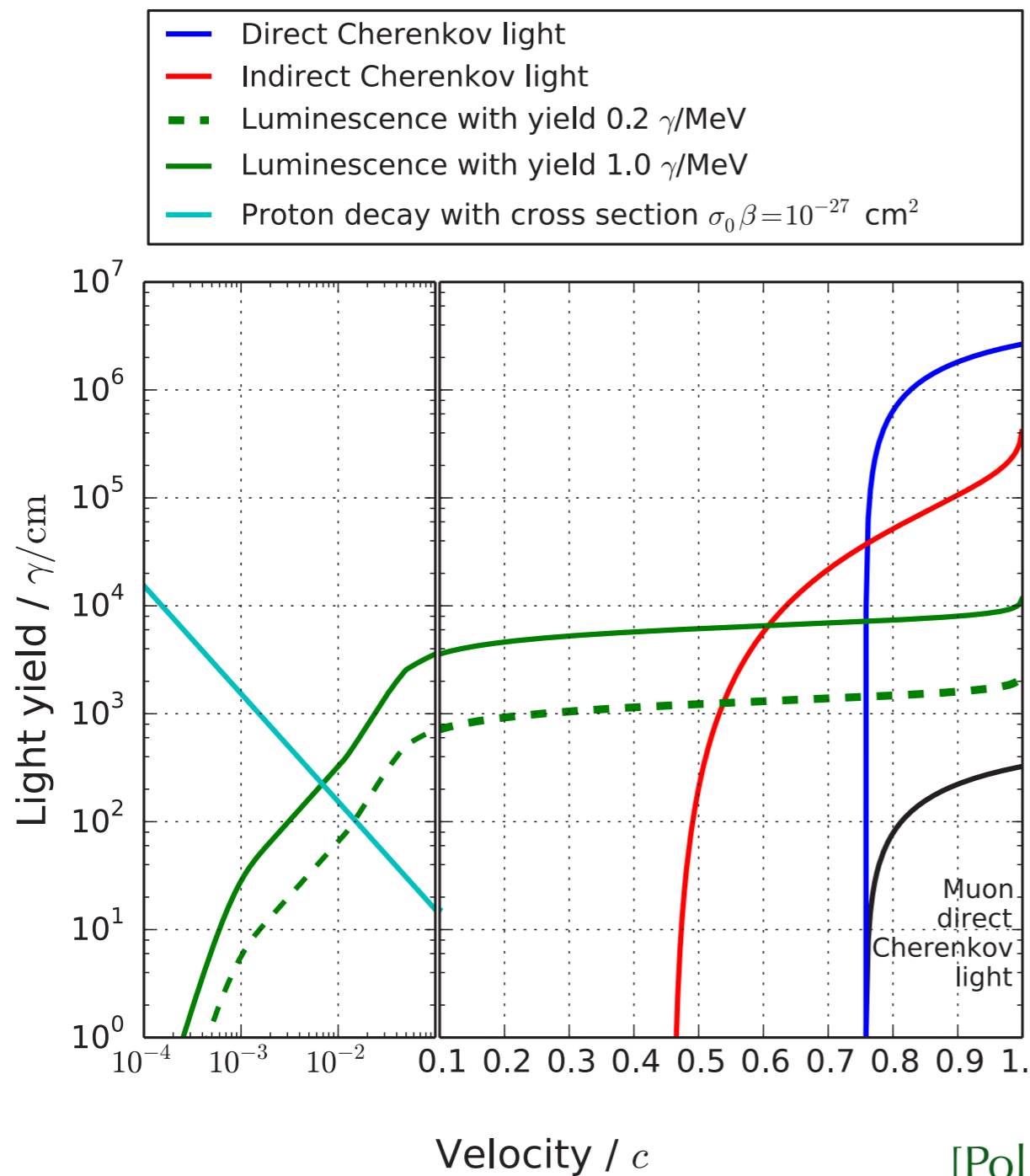


[Murase & Shoemaker '19]

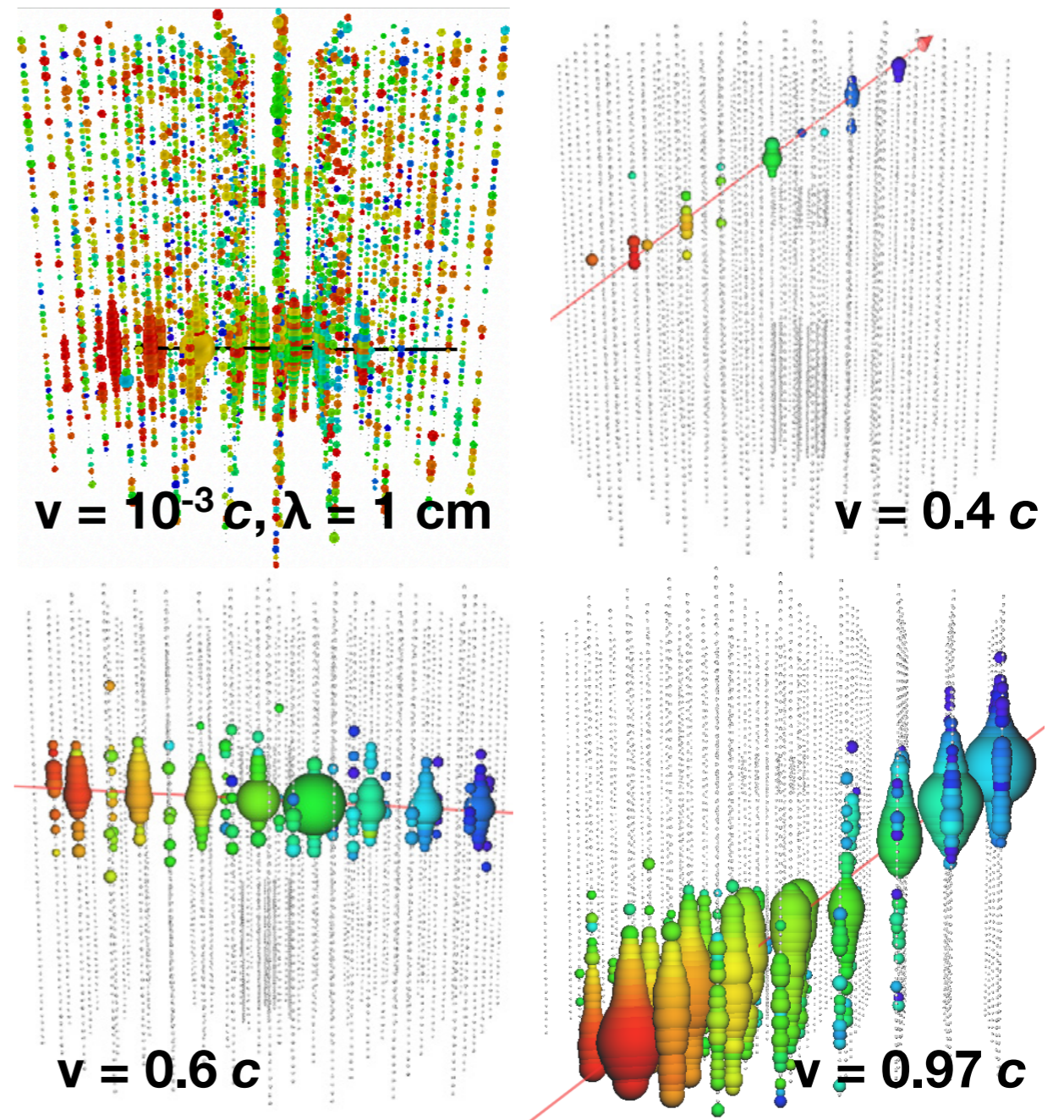


Exotic Signatures: Monopoles

Magnetic monopoles visible via characteristic electromagnetic interactions or via monopole-catalyzed baryon decays in GUTs.

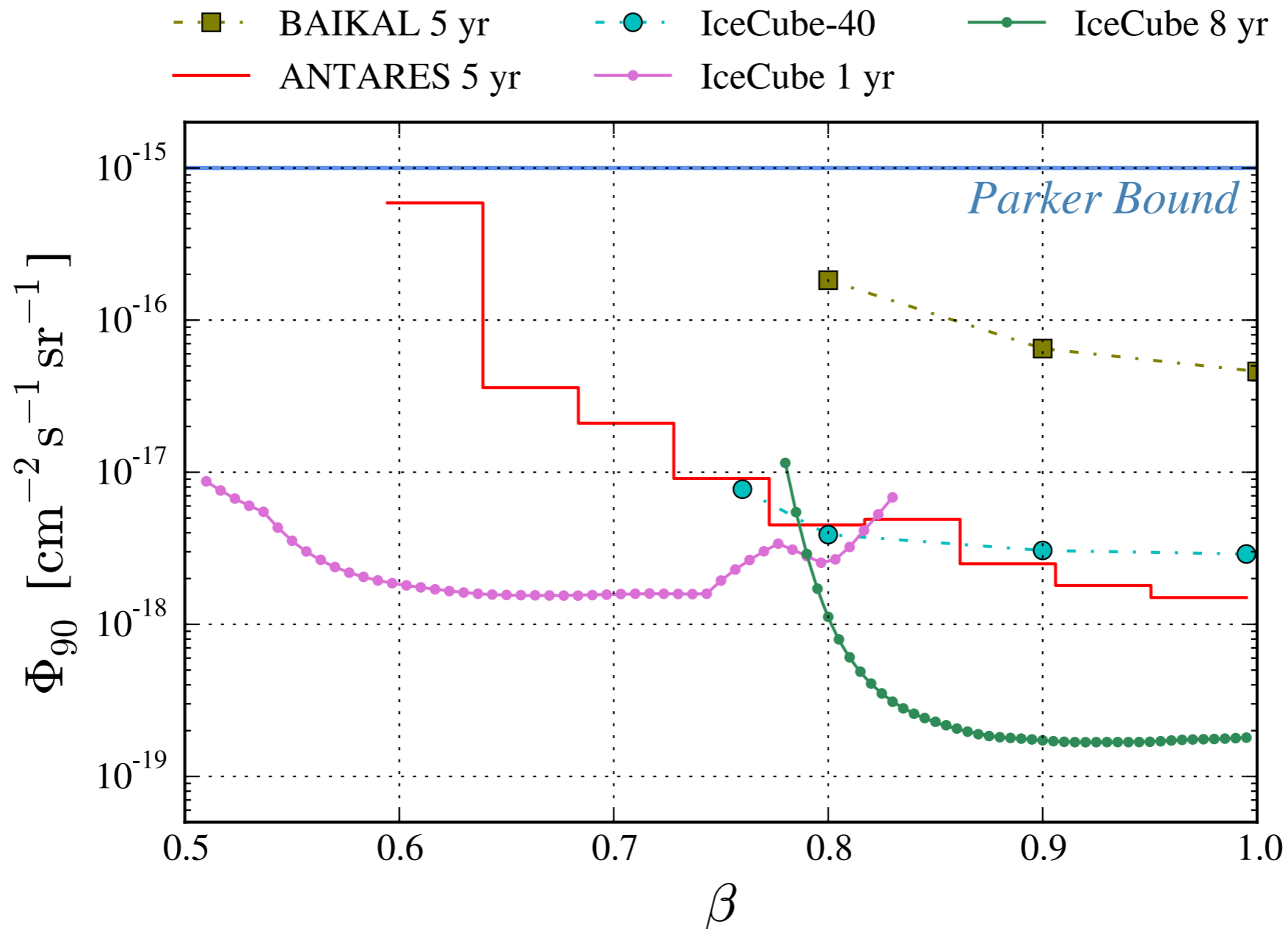


[Pollmann'18]



Limits on Primordial Monopoles

Neutrino telescopes sets meaningful limits on primordial monopoles below the *Parker bound* (short-circuit of Galactic magnetic fields).



[IceCube PRL 128 (2022) 5]

Summary

- High-energy cosmic radiation has been a powerful probe of particle physics in the 20th century (discovery of *positron*, *muon*, *pion*, ...).
- **Neutrino astronomy** offers complementary and unique probes of fundamental physics.
- *Long propagation baselines and large neutrino energies beyond the reach of accelerator facilities.*
- This allows us to study:
 - atmospheric **neutrino oscillations** and **neutrino interactions** in SM
 - **dark matter** in Milky Way, Sun, Earth, nearby galaxies, etc.
 - **neutrino decay, feeble interactions, non-standard oscillations**
 - *etc.*
- *We only highlighted a few selected topics and probes!*