



UV completion of Composite Higgs Models

Shahram Vatani

Composite Higgs Models

Composite Higgs Models

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graph TD; A[Composite Higgs Models] --> B[Dynamical EWSB]; A --> C[Hierarchy Problem];
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Dynamical EWSB

Hierarchy Problem

Composite Higgs Models

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graph TD; A[Composite Higgs Models] --> B[Dynamical EWSB]; A --> C[Hierarchy Problem]; B --- D[✓]; C --- E[✓]
```

Dynamical EWSB



Hierarchy Problem



Composite Higgs Models

Dynamical EWSB



Hierarchy Problem



$$\delta m^2_h \sim \Lambda^2$$

Composite Higgs Models

Dynamical EWSB



Hierarchy Problem



$$\delta m_h^2 \sim \Lambda^2$$
$$\delta m_h^2 \sim \frac{1}{\epsilon}$$

Composite Higgs Models

Dynamical EWSB



Hierarchy Problem



$$\begin{aligned} \delta m_h^2 &\sim \Lambda^2 && \rightarrow && \delta m_h^2 &\sim \Lambda^2 + m_{NP}^2 \\ \delta m_h^2 &\sim \frac{1}{\epsilon} && \rightarrow && \delta m_h^2 &\sim \frac{1}{\epsilon} + m_{NP}^2 \end{aligned}$$

Composite Higgs Models

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graph TD; A[Composite Higgs Models] --> B[Dynamical EWSB]; A --> C[Hierarchy Problem];
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Dynamical EWSB



Hierarchy Problem



Up to now... « Effective Composite Higgs Models »

Composite Higgs Models

Underlying Theory

Composite Higgs Models

Underlying Theory

Large N

Composite Higgs Models

Underlying Theory

Large N

TPS

- 1 Composite Higgs
- 2 UV road
- 3 Alternatives

Composite Higgs

The Basic Idea

- New Fermions, HyperFermions

The Basic Idea

- New Fermions, HyperFermions

HF

HF

HF

The Basic Idea

- New Fermions, HyperFermions
- New Interaction, HyperColor $\sim QCD$



HF



HF

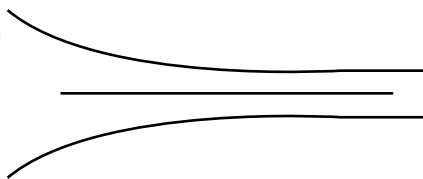
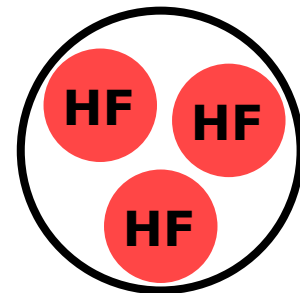


HF

The Basic Idea

- New Fermions, HyperFermions

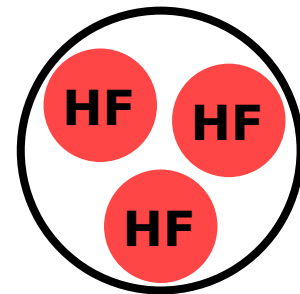
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The Basic Idea

- New Fermions, HyperFermions

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- Condensation

- Symmetry breaking pattern $\longrightarrow G/H$

- Pions

The Basic Idea

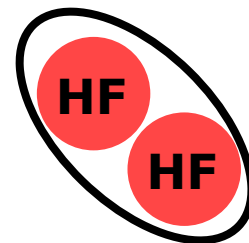
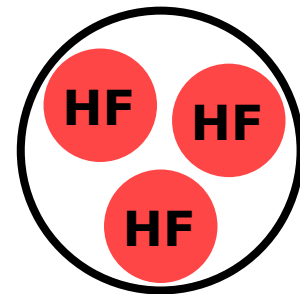
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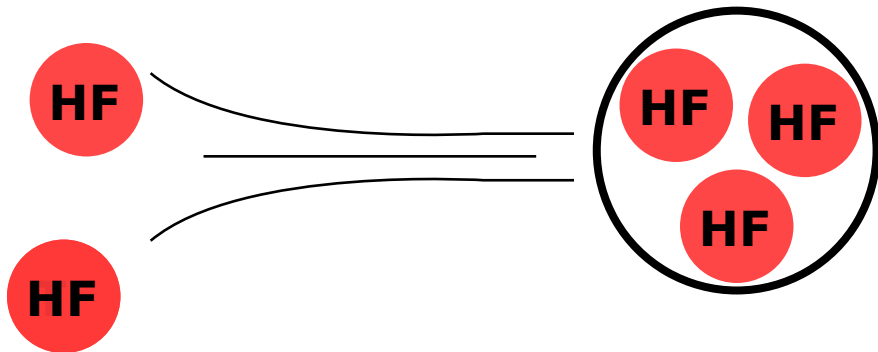
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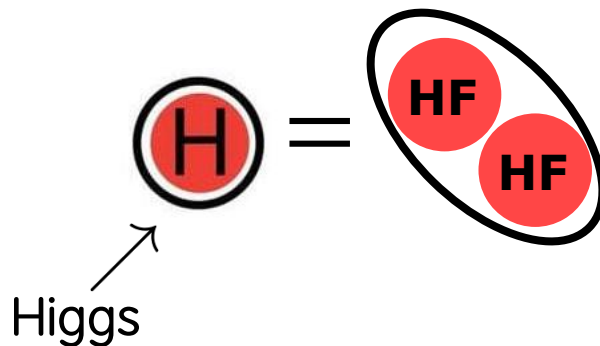
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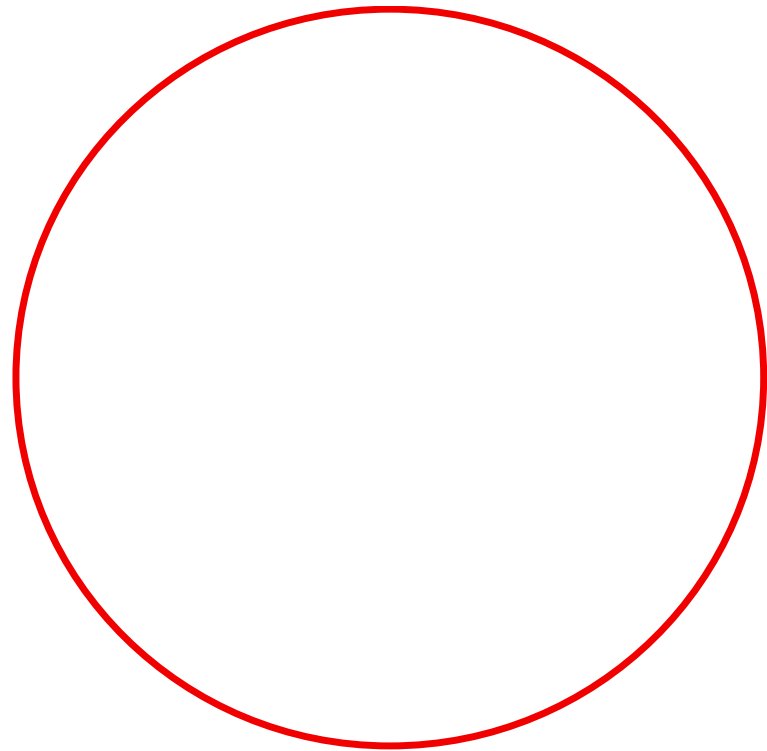


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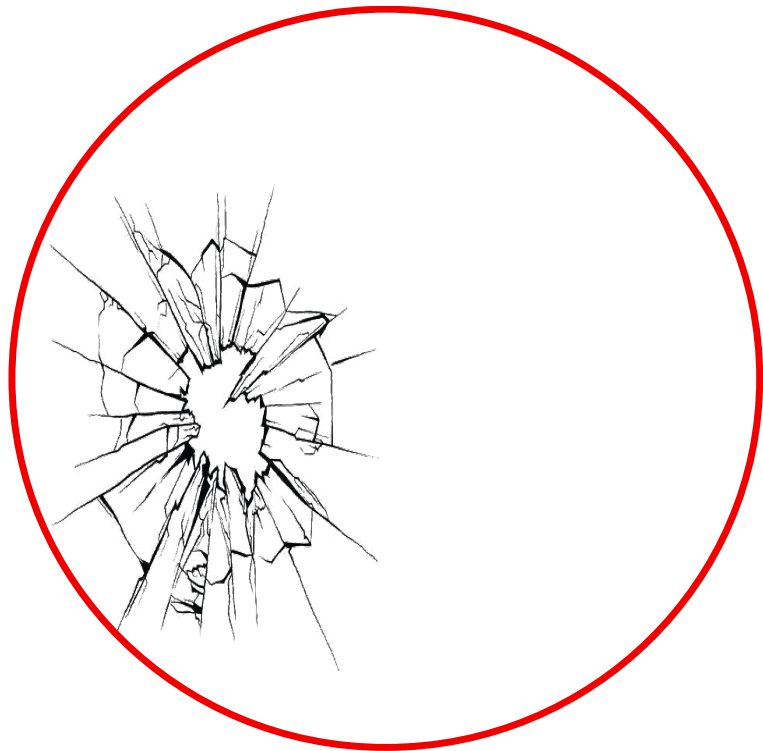
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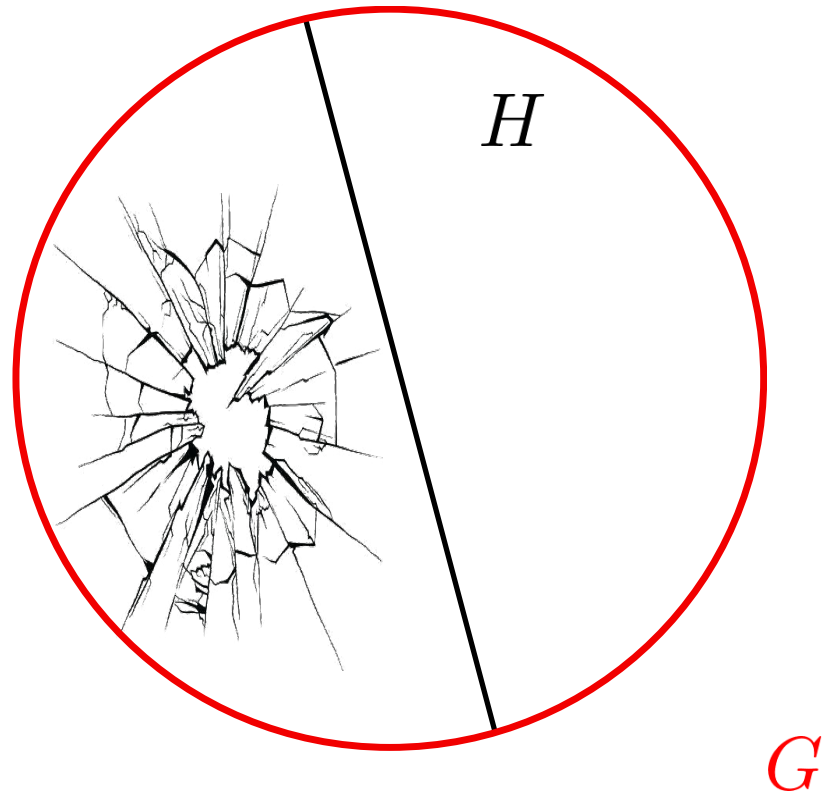


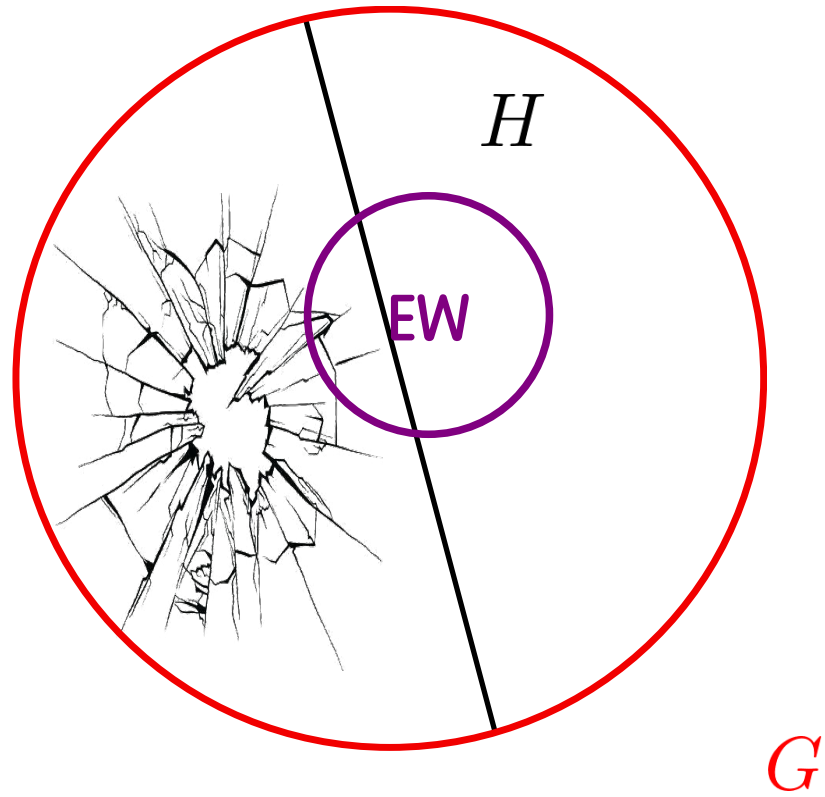


G



G





- How is this linked to the rest of SM ?
- Mass of the SM fermions ?

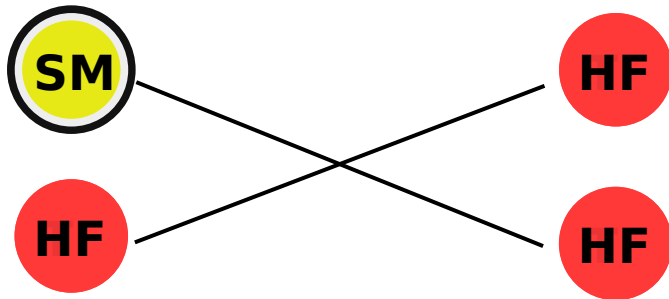
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Effective 4-Fermion Interactions !



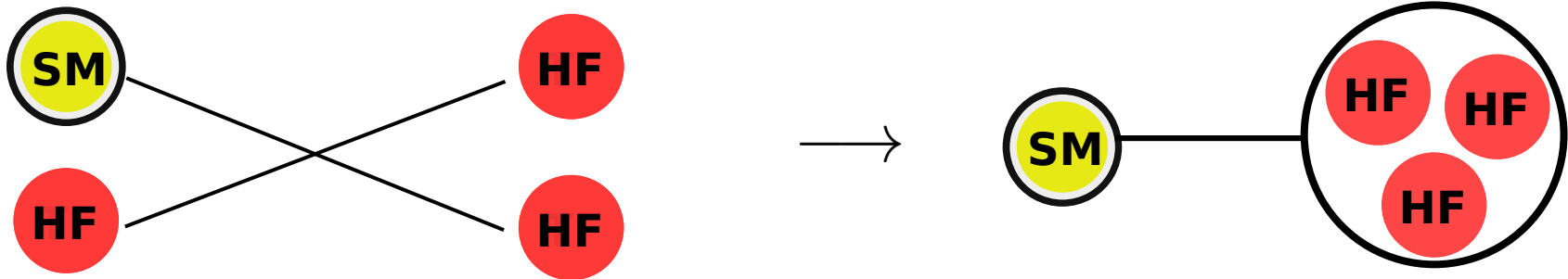
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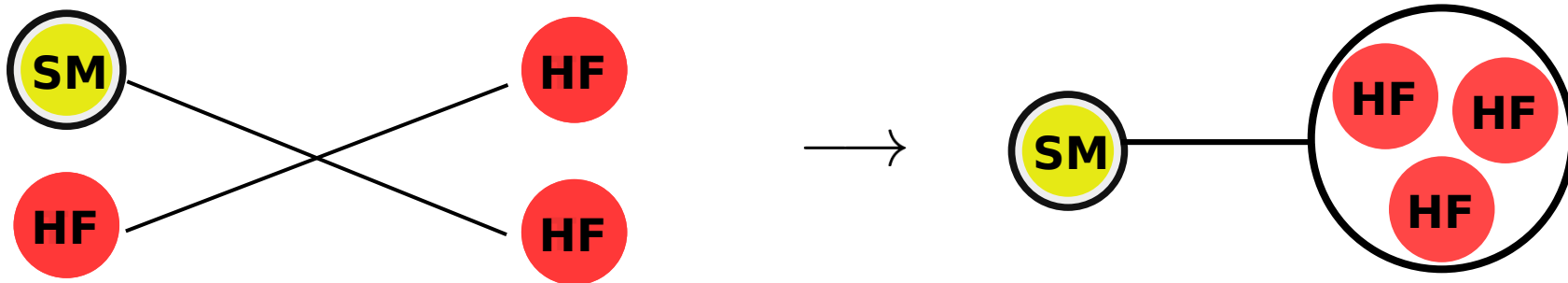
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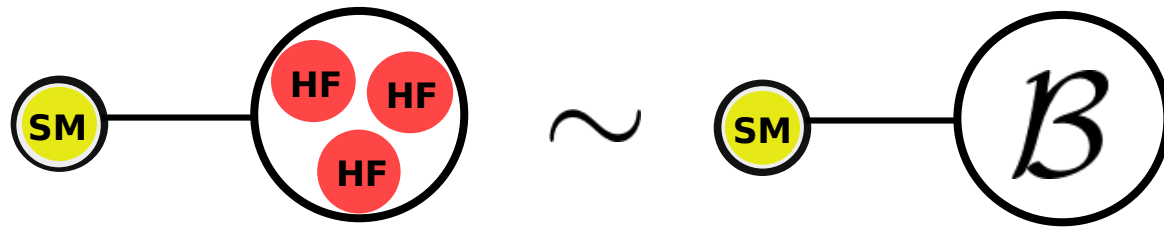


Partial Compositeness





- Effective linear mixing between **SM** and a baryon resonance \mathcal{B} (SM partner)



- Effective linear mixing between **SM** and a baryon resonance \mathcal{B} (SM partner)
- The interaction needs to be generated at some scale Λ_F



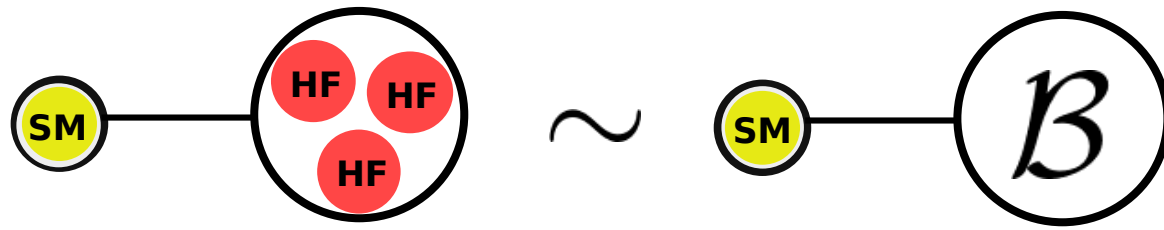
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Free Dynamic

$$c \frac{t\mathcal{H}\mathcal{H}\mathcal{H}}{\Lambda_F^2}$$



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Free Dynamic

$$\left[\frac{c(\mu)}{\Lambda_F^2} \right] t\mathcal{H}\mathcal{H}\mathcal{H}$$



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$$\left[c(\Lambda_{HC}) \frac{\Lambda_{HC}^3}{\Lambda_F^2} \right] t\mathcal{B}$$



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Near Conformal Dynamic



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Free Dynamic

$$\sim c \frac{\Lambda_{HC}^3}{\Lambda_F^2} t\mathcal{B}$$

Near Conformal Dynamic

$$\rightsquigarrow \left[c \left(\frac{\Lambda_F}{\Lambda_{HC}} \right)^\gamma \frac{\Lambda_{HC}^3}{\Lambda_F^2} \right] t\mathcal{B}$$



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$$\sim c \frac{\Lambda_{HC}^3}{\Lambda_F^2} t\mathcal{B}$$

Near Conformal Dynamic

$$\rightsquigarrow \left[c \left(\frac{\Lambda_F}{\Lambda_{HC}} \right)^\gamma \frac{\Lambda_{HC}^3}{\Lambda_F^2} \right] t\mathcal{B}$$

$$\rightsquigarrow [c \Lambda_{HC}] t\mathcal{B} \quad (\gamma = 2)$$

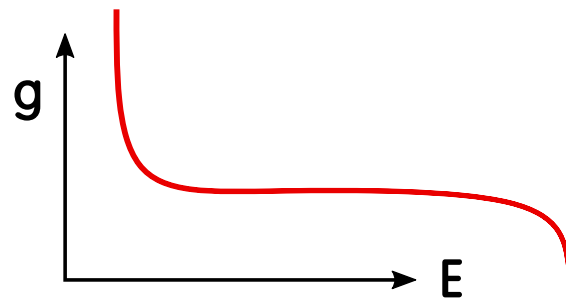


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Free Dynamic

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Near Conformal Dynamic



What is Natural ?

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A model dependant question ?

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(B)SM

• $y_t \sim 1$

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Natural

• $y_{b,c,s,d,u} \ll 1$

Need for a
Mechanism

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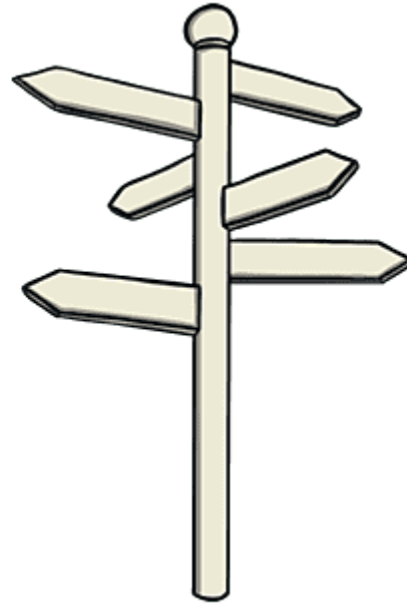
• $y_{b,c,s,d,u} \ll 1$

Natural

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Need for a
Mechanism

Where do we go ?



Composite Higgs Models

- Higgs as pNGB
- *SM* partner as HyperBaryons
- Asymptotically Free Theory

Composite Higgs Models

G_{HC}	ψ	χ	Restrictions	$-q_\chi/q_\psi$	Y_χ	Non Conformal	Model Name
	Real	Real	SU(5)/SO(5) \times SU(6)/SO(6)				
$SO(N_{\text{HC}})$	$5 \times \mathbf{S}_2$	$6 \times \mathbf{F}$	$N_{\text{HC}} \geq 55$	$\frac{5(N_{\text{HC}}+2)}{6}$	1/3	/	
$SO(N_{\text{HC}})$	$5 \times \mathbf{Ad}$	$6 \times \mathbf{F}$	$N_{\text{HC}} \geq 15$	$\frac{5(N_{\text{HC}}-2)}{6}$	1/3	/	
$SO(N_{\text{HC}})$	$5 \times \mathbf{F}$	$6 \times \mathbf{Spin}$	$N_{\text{HC}} = 7, 9$	$\frac{5}{6}, \frac{5}{12}$	1/3	$N_{\text{HC}} = 7, 9$	M1, M2
$SO(N_{\text{HC}})$	$5 \times \mathbf{Spin}$	$6 \times \mathbf{F}$	$N_{\text{HC}} = 7, 9$	$\frac{5}{6}, \frac{5}{3}$	2/3	$N_{\text{HC}} = 7, 9$	M3, M4
	Real	Pseudo-Real	SU(5)/SO(5) \times SU(6)/Sp(6)				
$Sp(2N_{\text{HC}})$	$5 \times \mathbf{Ad}$	$6 \times \mathbf{F}$	$2N_{\text{HC}} \geq 12$	$\frac{5(N_{\text{HC}}+1)}{3}$	1/3	/	
$Sp(2N_{\text{HC}})$	$5 \times \mathbf{A}_2$	$6 \times \mathbf{F}$	$2N_{\text{HC}} \geq 4$	$\frac{5(N_{\text{HC}}-1)}{3}$	1/3	$2N_{\text{HC}} = 4$	M5
$SO(N_{\text{HC}})$	$5 \times \mathbf{F}$	$6 \times \mathbf{Spin}$	$N_{\text{HC}} = 11, 13$	$\frac{5}{24}, \frac{5}{48}$	1/3	/	
	Real	Complex	SU(5)/SO(5) \times SU(3) ² /SU(3)				
$SU(N_{\text{HC}})$	$5 \times \mathbf{A}_2$	$3 \times (\mathbf{F}, \bar{\mathbf{F}})$	$N_{\text{HC}} = 4$	$\frac{5}{3}$	1/3	$N_{\text{HC}} = 4$	M6
$SO(N_{\text{HC}})$	$5 \times \mathbf{F}$	$3 \times (\mathbf{Spin}, \bar{\mathbf{Spin}})$	$N_{\text{HC}} = 10, 14$	$\frac{5}{12}, \frac{5}{48}$	1/3	$N_{\text{HC}} = 10$	M7
	Pseudo-Real	Real	SU(4)/Sp(4) \times SU(6)/SO(6)				
$Sp(2N_{\text{HC}})$	$4 \times \mathbf{F}$	$6 \times \mathbf{A}_2$	$2N_{\text{HC}} \leq 36$	$\frac{1}{3(N_{\text{HC}}-1)}$	2/3	$2N_{\text{HC}} = 4$	M8
$SO(N_{\text{HC}})$	$4 \times \mathbf{Spin}$	$6 \times \mathbf{F}$	$N_{\text{HC}} = 11, 13$	$\frac{8}{3}, \frac{16}{3}$	2/3	$N_{\text{HC}} = 11$	M9
	Complex	Real	SU(4) ² /SU(4) \times SU(6)/SO(6)				
$SO(N_{\text{HC}})$	$4 \times (\mathbf{Spin}, \bar{\mathbf{Spin}})$	$6 \times \mathbf{F}$	$N_{\text{HC}} = 10$	$\frac{8}{3}$	2/3	$N_{\text{HC}} = 10$	M10
$SU(N_{\text{HC}})$	$4 \times (\mathbf{F}, \bar{\mathbf{F}})$	$6 \times \mathbf{A}_2$	$N_{\text{HC}} = 4$	$\frac{2}{3}$	2/3	$N_{\text{HC}} = 4$	M11
	Complex	Complex	SU(4) ² /SU(4) \times SU(3) ² /SU(3)				
$SU(N_{\text{HC}})$	$4 \times (\mathbf{F}, \bar{\mathbf{F}})$	$3 \times (\mathbf{A}_2, \bar{\mathbf{A}}_2)$	$N_{\text{HC}} \geq 5$	$\frac{4}{3(N_{\text{HC}}-2)}$	2/3	$N_{\text{HC}} = 5$	M12
$SU(N_{\text{HC}})$	$4 \times (\mathbf{F}, \bar{\mathbf{F}})$	$3 \times (\mathbf{S}_2, \bar{\mathbf{S}}_2)$	$N_{\text{HC}} \geq 5$	$\frac{4}{3(N_{\text{HC}}+2)}$	2/3	/	
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Composite Higgs Models

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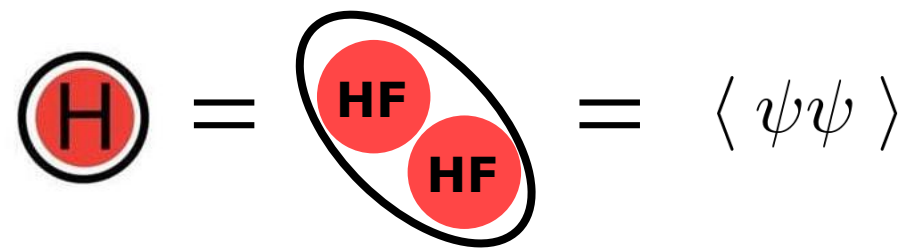
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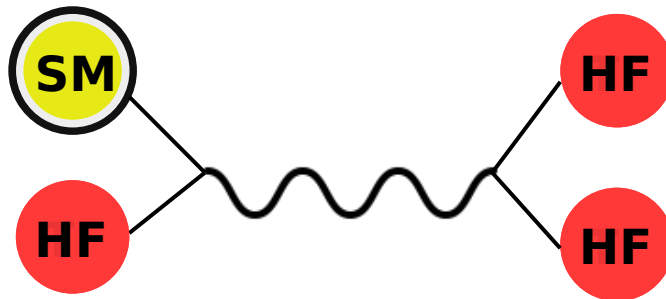
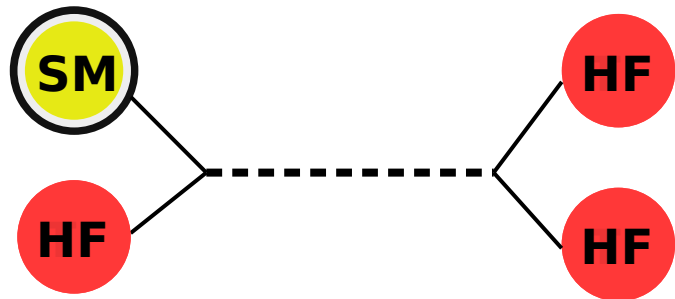
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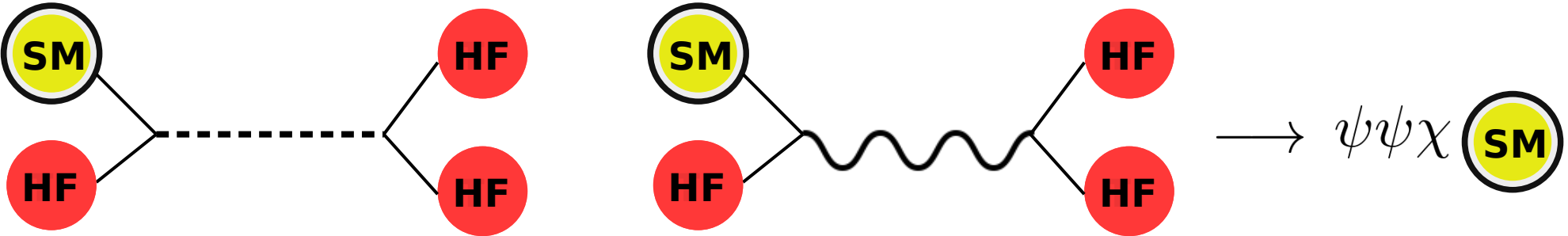
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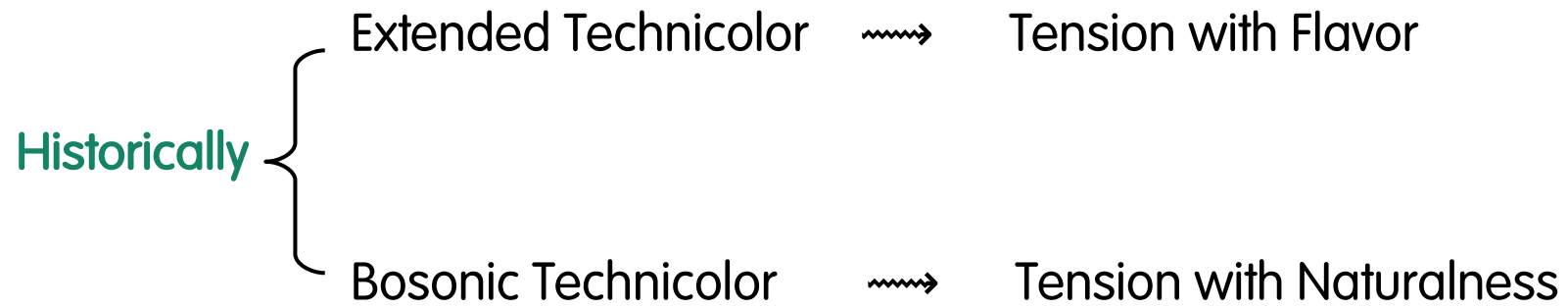
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Historically {







- Partially unify HC and SM
- High scale scalars to break the gauge group
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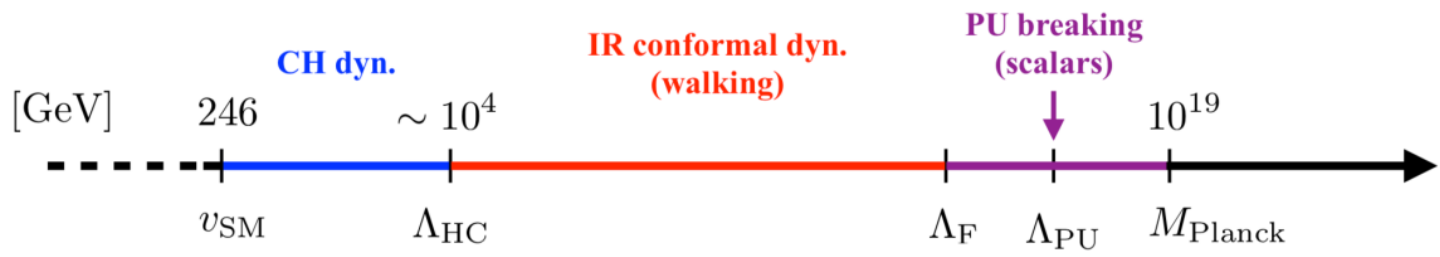
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Goals

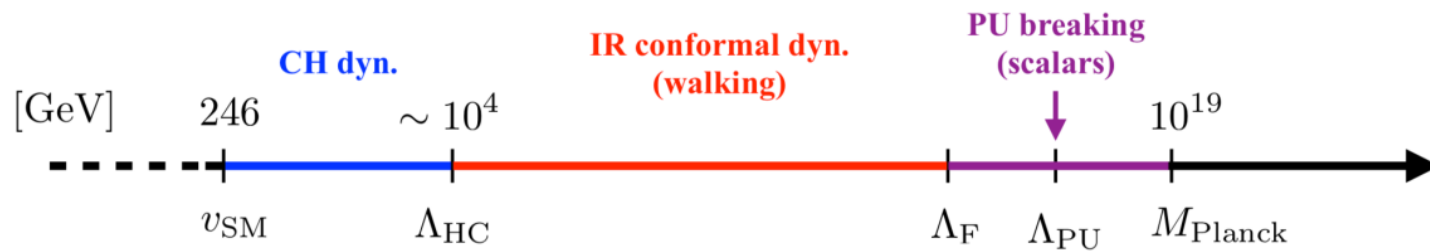
- Generate 4-F
- In a well defined theory
- Target at low energy a Composite Higgs scenario
- Realistic Flavor structure

**The Techni-Pati-Salam
(TPS)
a possible UV completion**

Set-Up

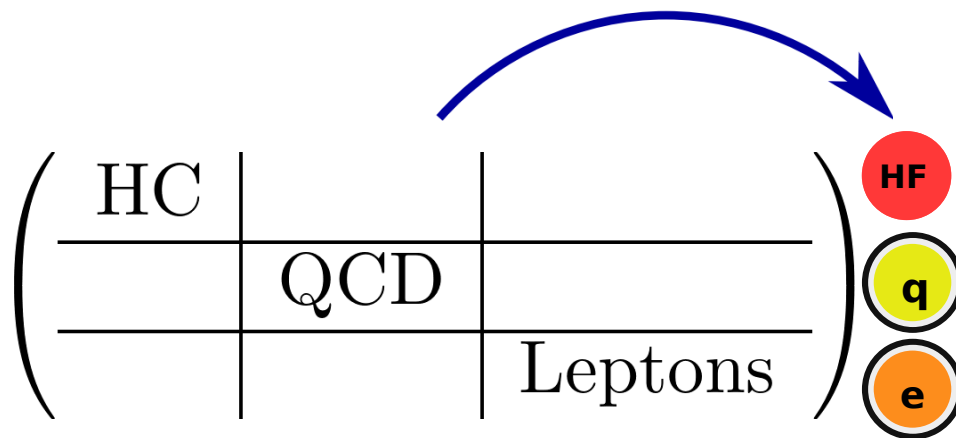
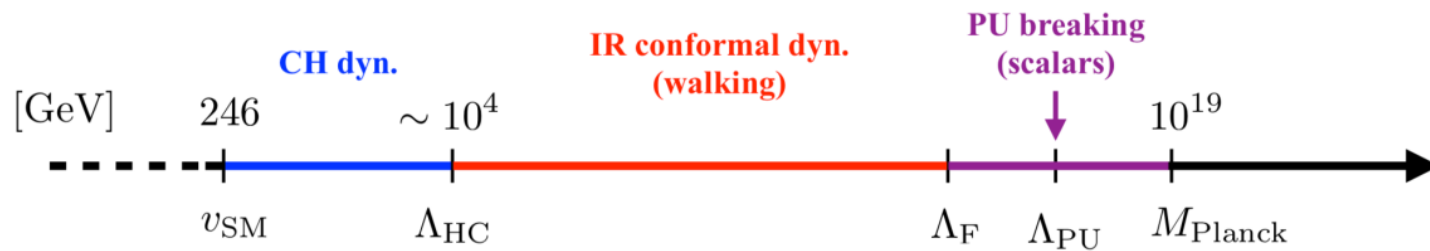


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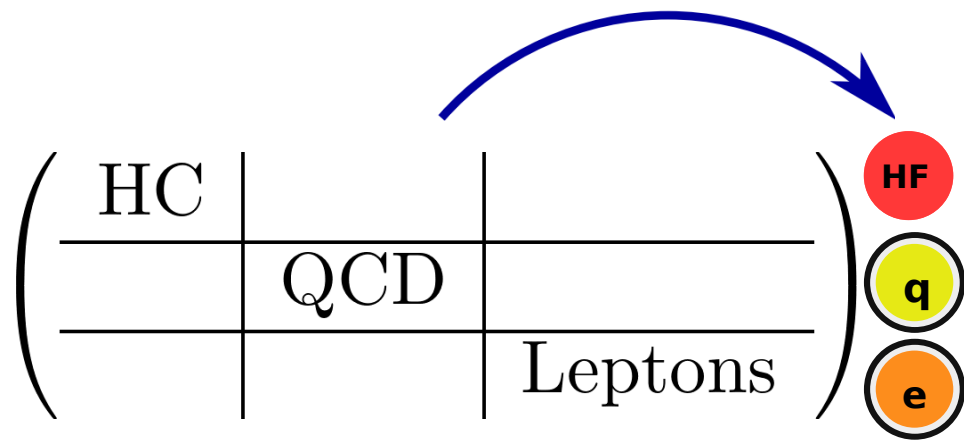
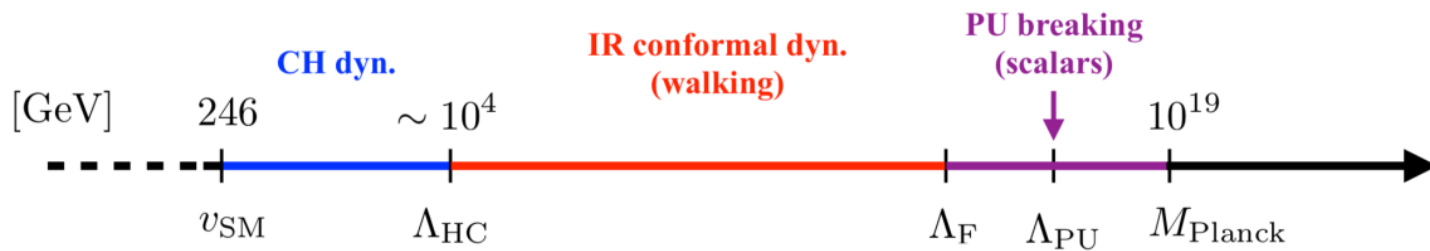


$$\left(\begin{array}{c|c|c} \text{HC} & & \\ \hline & \text{QCD} & \\ \hline & & \text{Leptons} \end{array} \right)$$

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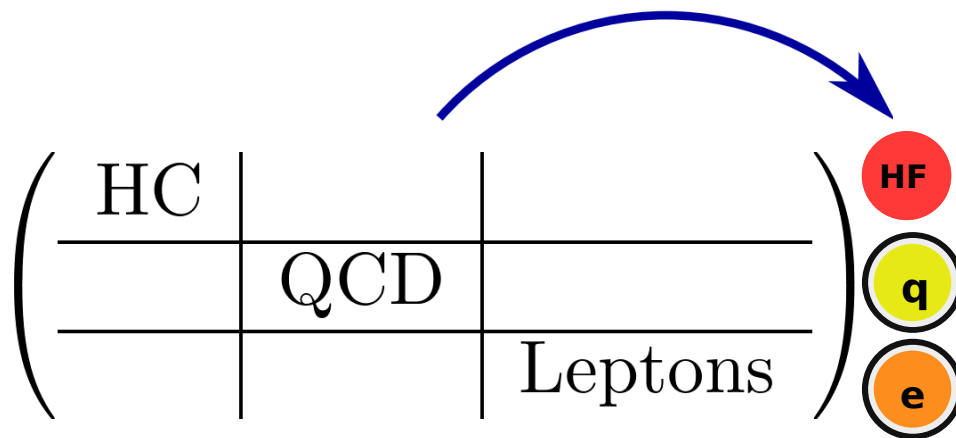
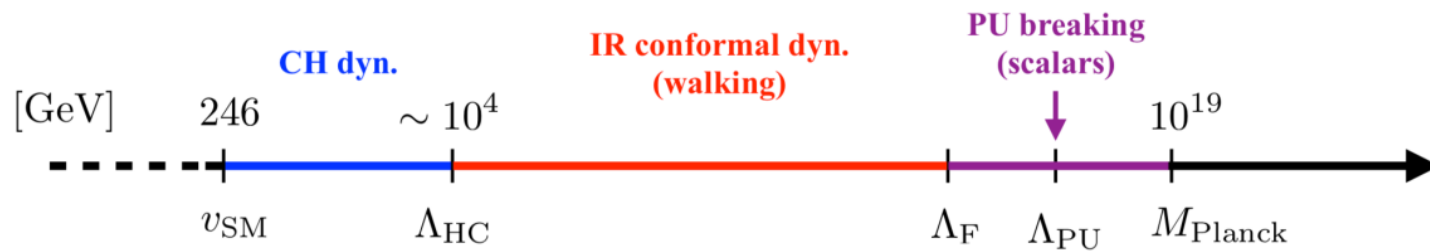


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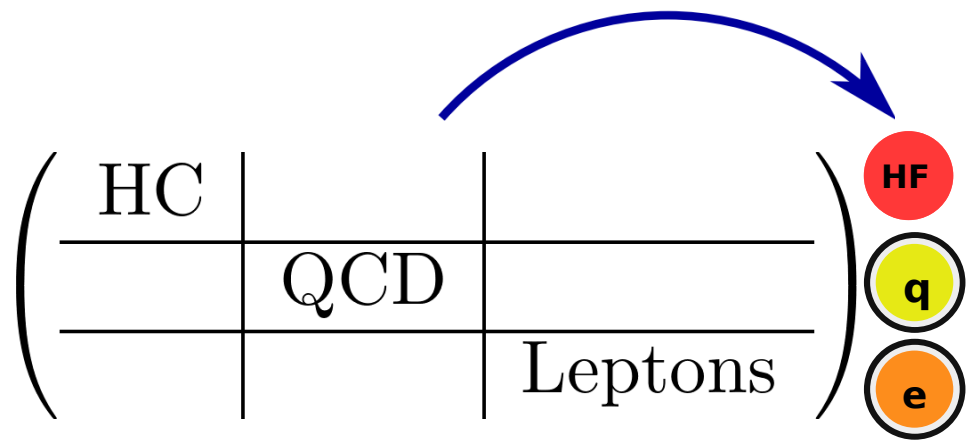
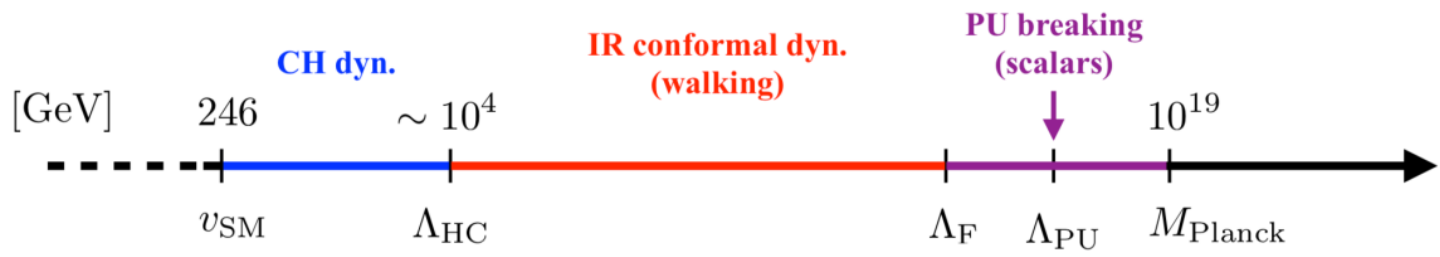
HC =

Set-Up



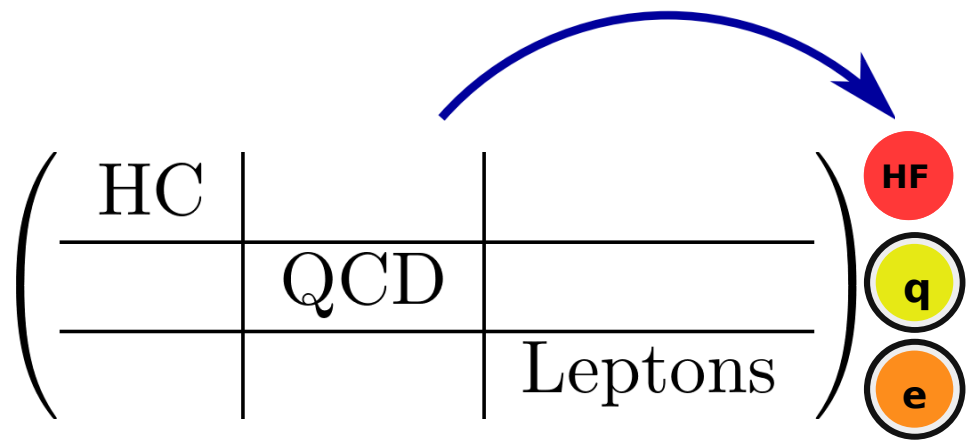
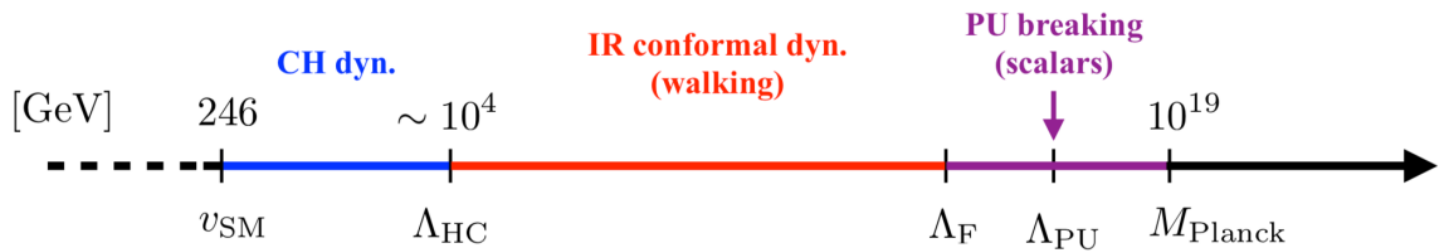
$$HC = SU(N)$$

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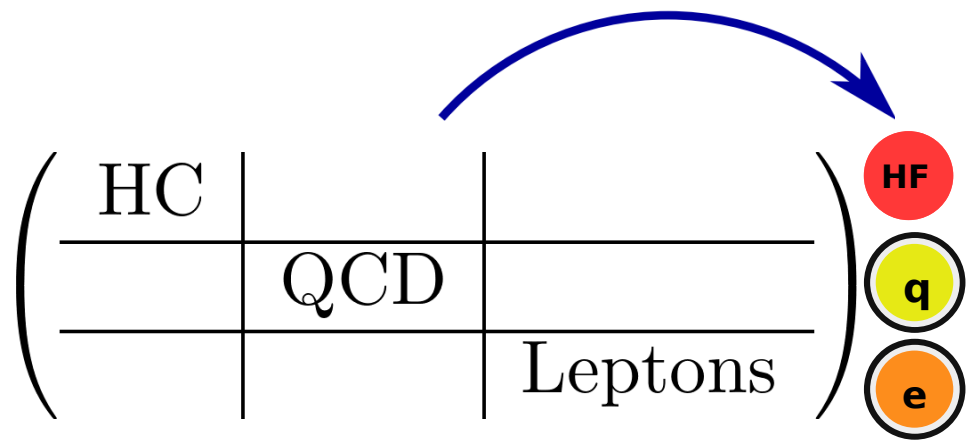
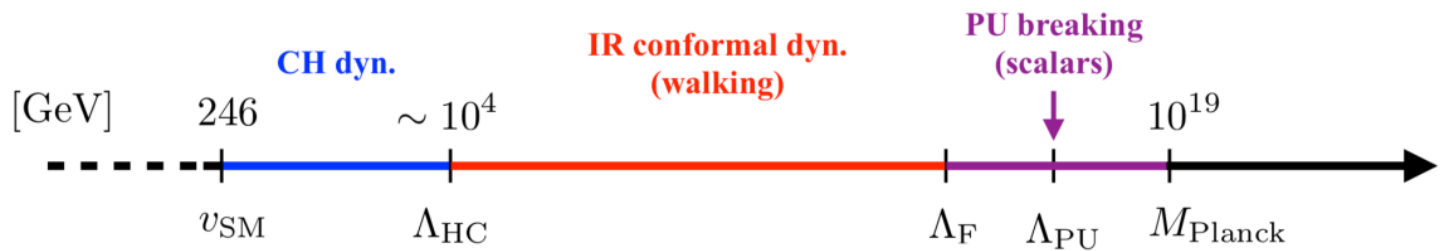
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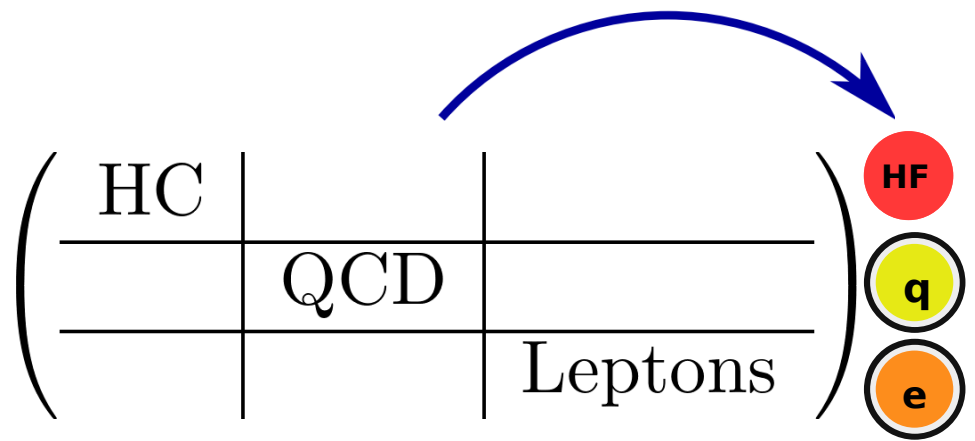
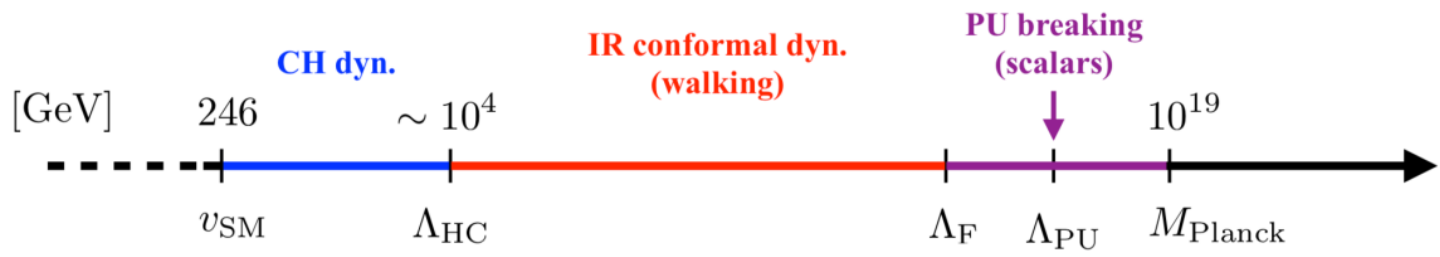
$$HC = S\cancel{U}(N), SO(N)$$

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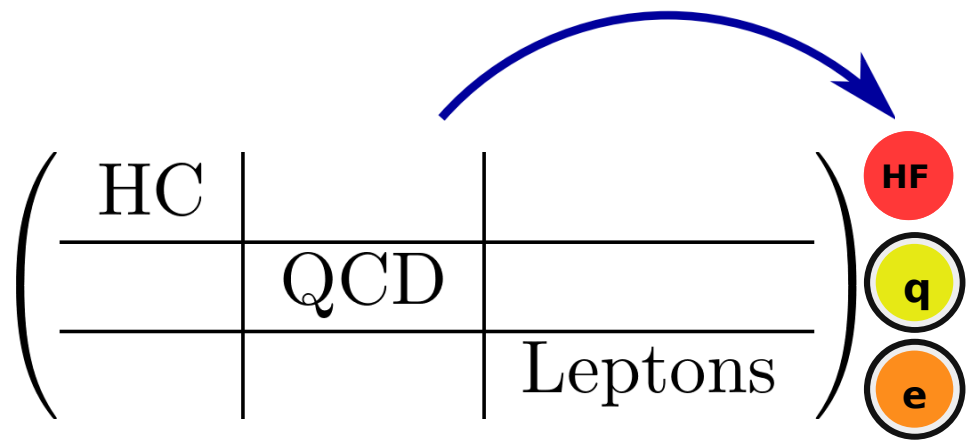
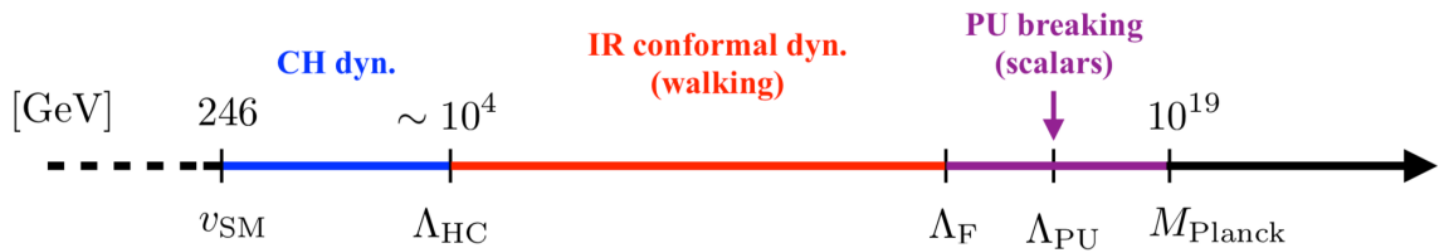
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Set-Up



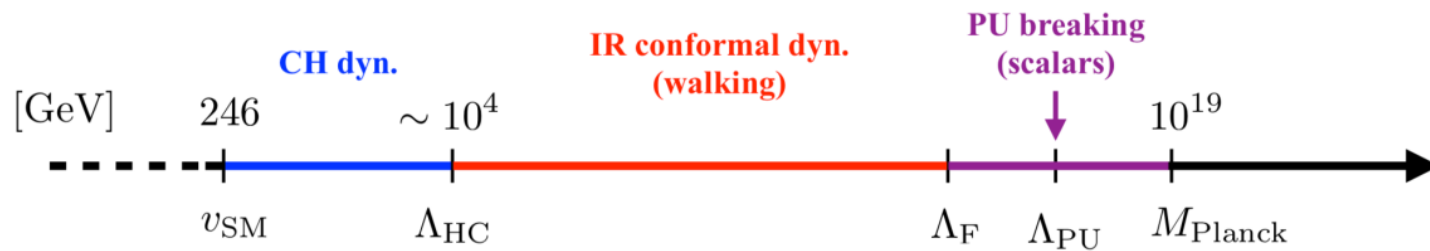
$$HC = S(U(N), S(O(N)), Sp(N))$$

Set-Up



HC = ~~$SU(N)$~~ , ~~$SO(N)$~~ , $Sp(N)$ ✓

Set-Up



$$SU(8)_{PS} \times SU(2)_R \times SU(2)_L$$

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	$SU(8)_{PS}$	$SU(2)_R$	$SU(2)_L$	vev
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Θ	A_2	1	1	v_{CHC}^Θ
Δ	A_3	2	1	

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Fermion Content

	$SU(8)_{PS}$	$SU(2)_R$	$SU(2)_L$
Ω^p	8	1	2
Υ^p	$\bar{8}$	2	1
Ξ	$70 = A_4$	1	1
N^p	1	1	1

Fermion Content

Higgs Components

	$SU(8)_{PS}$	$SU(2)_R$	$SU(2)_L$
$\Omega^p = \begin{pmatrix} L_{u/d}^p \\ q_L^p \\ l_L^p \end{pmatrix}$	8	1	2
$\Upsilon^p = \begin{pmatrix} U_d & D_u \\ d_R^{c\ p} & u_R^{c\ p} \\ e_R^{c\ p} & \nu_R^{c\ p} \end{pmatrix}$	$\bar{8}$	2	1
$\Xi = \begin{pmatrix} U_u & \chi & \rho & \eta & \omega \\ D_d & \tilde{\chi} & \tilde{\rho} & \tilde{\eta} & \tilde{\omega} \end{pmatrix}$	$70 = A_4$	1	1
N^p	1	1	1

Partial Compositeness

4-F : Gauge Mediation

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$$A^\mu = \left(\begin{array}{c|c|c} \text{HC} & & \\ \hline & \text{QCD} & \\ \hline & & \text{Leptons} \end{array} \right)$$



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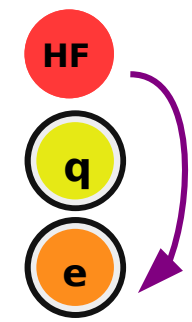
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Quark-Lepton mass splitting !

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$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi \\ - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

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	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$		(χb_R^c) (χt_R^c)		$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$ $(U_t D_u^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	$(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 t_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$		(χb_R^c) (χt_R^c)		$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$		(χb_R^c) (χt_R^c)		$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

$$\frac{\lambda_\Delta^2}{M_{\varphi_4}^2} c_4 (\bar{U}_t \bar{U}_d^3) (\chi b_R^c)$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	 (χb_R^c)	 (χt_R^c)	 $(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	 $(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

$$\frac{\lambda_\Delta^2}{M_{\varphi_4}^2} c_4 (\bar{U}_t \bar{U}_d^3) (\chi b_R^c)$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$		(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$ $(U_t D_u^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$ $(\tilde{\eta} D_u^3)$

Scalar Mediation ?

We add Yukawa couplings:

$$\mathcal{L}_Y = -\mu_N NN - \lambda_\Phi \Upsilon \Phi N - \mu_\Xi \Xi \Xi - \lambda_\Psi \Xi \Psi \Xi - \lambda_{\Theta L} \Omega \Theta^* \Omega - \lambda_{\Theta R} \Upsilon \Theta \Upsilon - \lambda_\Delta \Upsilon \Delta \Xi + \text{c.c.}$$

$$\frac{\lambda_\Delta^2}{M_{\varphi_4}^2} c_4 (\bar{U}_t \bar{U}_d^3) (\chi b_R^c)$$

	1 SM field							0 SM field						
φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$		(χb_R^c) (χt_R^c)		$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$ $(U_t D_u^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

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$$\frac{\lambda_\Delta^2}{M_{\varphi_4}^2} c_4 (\bar{U}_t \bar{U}_d^3) (\chi b_R^c)$$

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φ_i	$(\mathbf{4}, \mathbf{1})_{-\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{4}, \mathbf{1})_{\frac{1}{2}}$	$(\mathbf{4}, \mathbf{3})_{\frac{1}{6}}$	$(\mathbf{4}, \mathbf{3})_{-\frac{5}{6}}$	$(\mathbf{5}, \mathbf{1})_0$	$(\mathbf{5}, \mathbf{1})_{-1}$	$(\mathbf{5}, \mathbf{3})_{\frac{2}{3}}$	$(\mathbf{5}, \mathbf{3})_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(U_t \tilde{\chi})$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(U_t \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$		(χb_R^c) (χt_R^c)		$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$ $(U_t D_u^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

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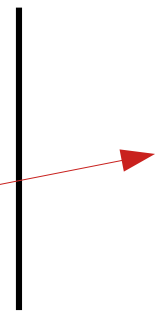
$$\frac{\lambda_\Delta^2}{M_{\varphi_5}^2} c_5 (\bar{U}_t \bar{D}_u^3) (\chi t_R^c)$$

	1 SM field							0 SM field						
φ_i	$(4, 1)_{-\frac{1}{2}}$	$(4, 3)_{\frac{1}{6}}$	$(4, 3)_{-\frac{5}{6}}$	$(5, 1)_0$	$(5, 1)_{-1}$	$(5, 3)_{\frac{2}{3}}$	$(5, 3)_{-\frac{1}{3}}$	$(4, 1)_{\frac{1}{2}}$	$(4, 3)_{\frac{1}{6}}$	$(4, 3)_{-\frac{5}{6}}$	$(5, 1)_0$	$(5, 1)_{-1}$	$(5, 3)_{\frac{2}{3}}$	$(5, 3)_{-\frac{1}{3}}$
$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(\tilde{\chi} \tilde{\chi})$	$(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

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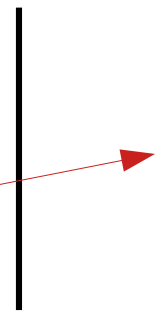
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$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
$\Upsilon \Theta \Upsilon$	$(U_d^3 \nu_R^c)$ $(D_u^3 \tau_R^c)$	$(U_d^3 t_R^c)$ $(D_u^3 b_R^c)$	-	-	-	-	-	-	-	-	$(U_d^3 D_u^3)$	-	-	-
$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(\tilde{\chi} \tilde{\eta})$	$(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

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$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(\tilde{\chi} \tilde{\eta})$	$(\chi \tilde{\chi})$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

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$\Omega \Theta^* \Omega$	$(L^3 l_L)$	$(L^3 q_L)$	-	-	-	-	-	-	-	-	$(L^3 L^3)$	-	-	-
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$\Xi \Psi \Xi$	-	-	-	-	-	-	-	(χD_b) $(\tilde{\chi} \chi)$ $(\chi \eta)$ $(\tilde{\chi} \tilde{\eta})$	(χD_b) $(\tilde{\chi} \chi)$ $(\eta \tilde{\chi})$ $(\chi \tilde{\eta})$	-	$(U_t D_b)$ $(\eta \tilde{\eta})$	-	-	-
$\Upsilon \Delta^* \Xi$	$(U_t \nu_R^c)$ $(U_t \tau_R^c)$ $(\tilde{\eta} t_R^c)$ $(\tilde{\eta} b_R^c)$	$(D_b t_R^c)$ (ηb_R^c) $(\eta \nu_R^c)$	$(D_b b_R^c)$ (ηt_R^c) $(\eta \tau_R^c)$	(χb_R^c)	(χt_R^c)	$(\tilde{\chi} b_R^c)$ $(\chi \tau_R^c)$	$(\tilde{\chi} t_R^c)$ $(\chi \nu_R^c)$	-	(χU_d^3) $(\tilde{\chi} D_u^3)$	(χD_u^3) $(\tilde{\chi} U_d^3)$	$(U_t U_d^3)$	$(U_t D_u^3)$	$(\tilde{\eta} U_d^3)$	$(\tilde{\eta} D_u^3)$

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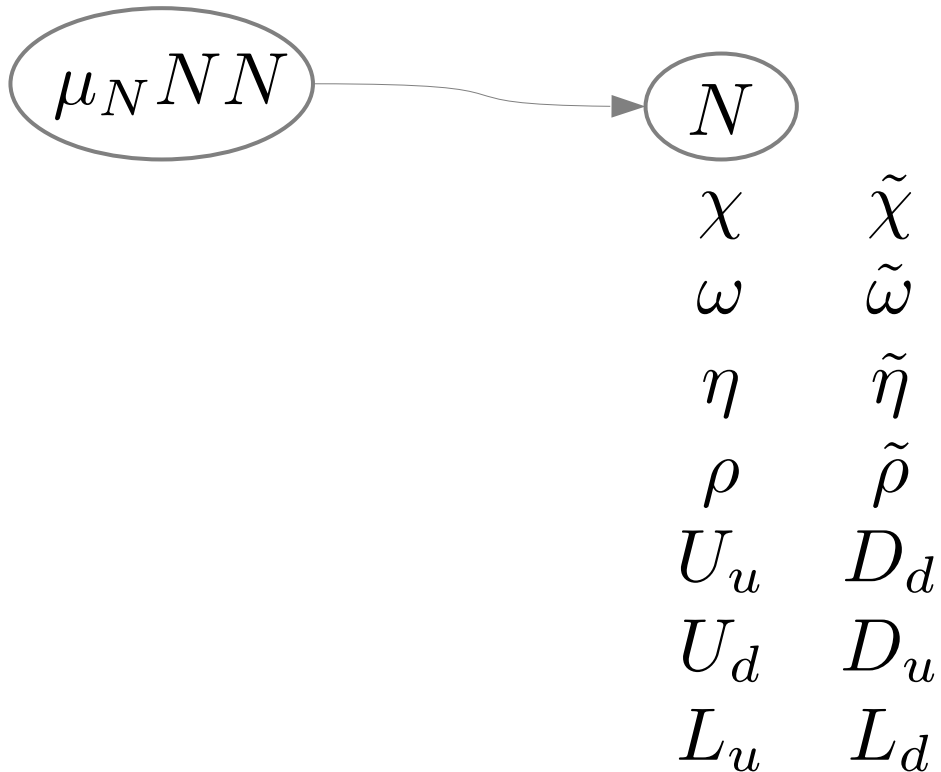
HyperFermion Masses

- Relevant for HyperColor Dynamics, low energy symmetry breaking pattern

$$\begin{array}{cc} N & \\ \chi & \tilde{\chi} \\ \omega & \tilde{\omega} \\ \eta & \tilde{\eta} \\ \rho & \tilde{\rho} \\ U_u & D_d \\ U_d & D_u \\ L_u & L_d \end{array}$$

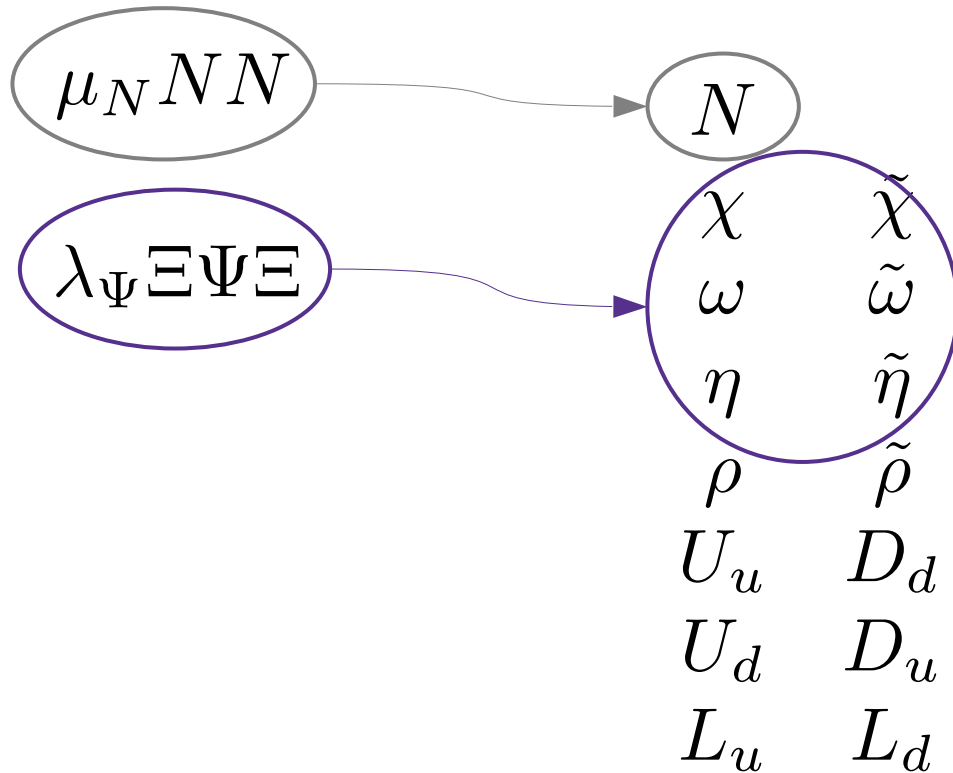
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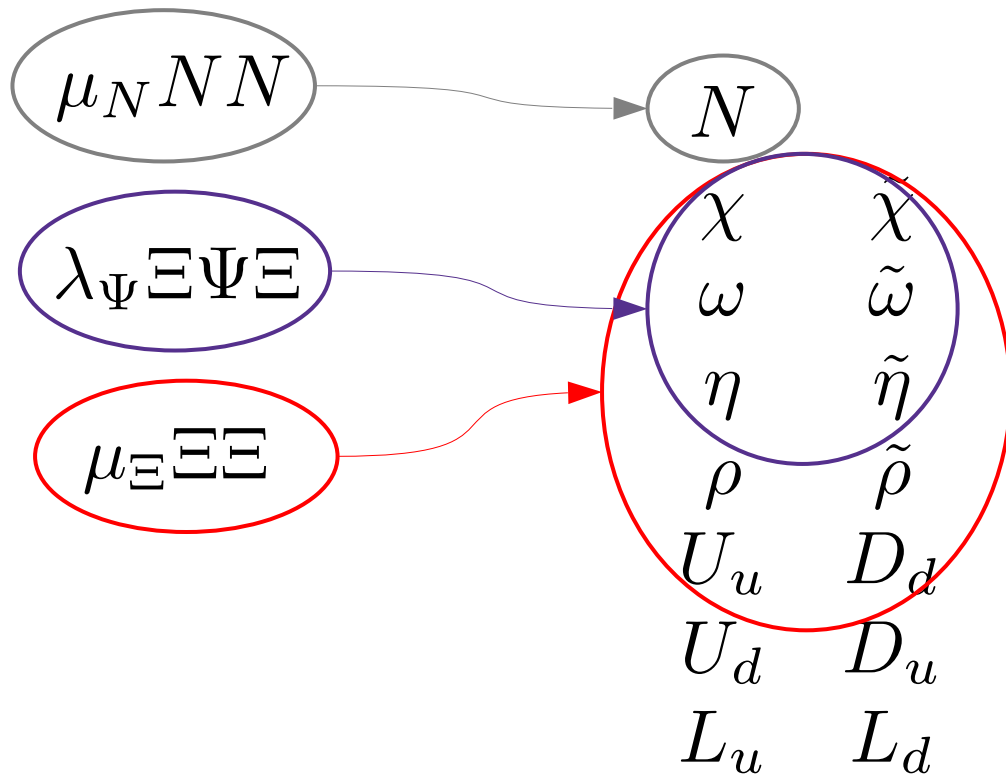
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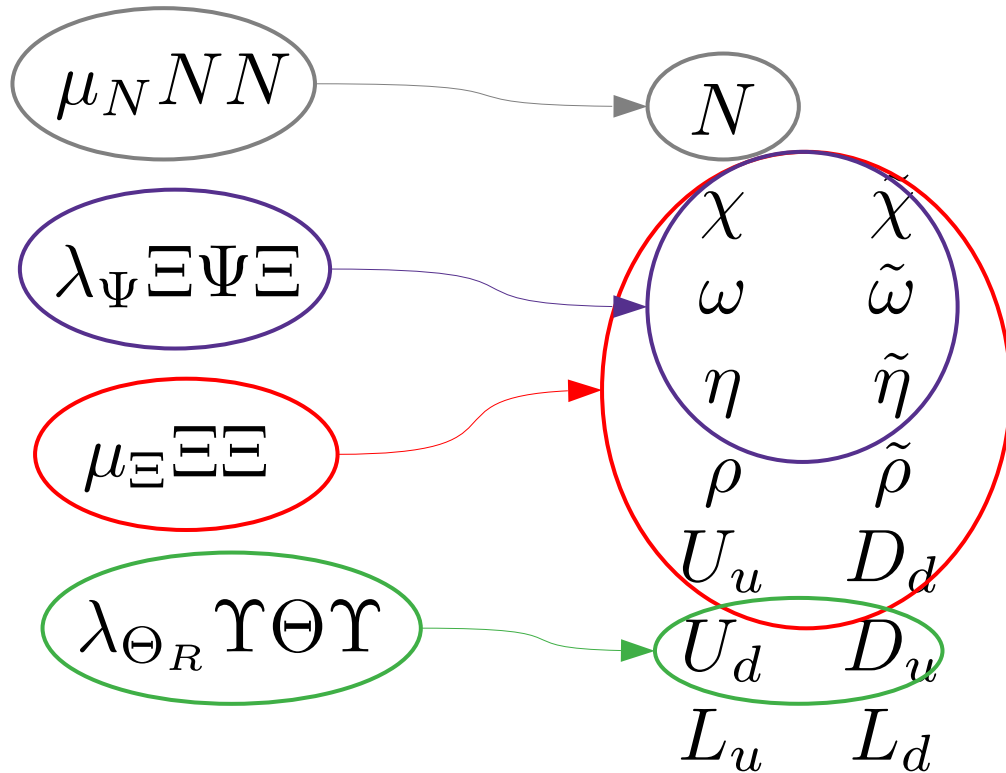
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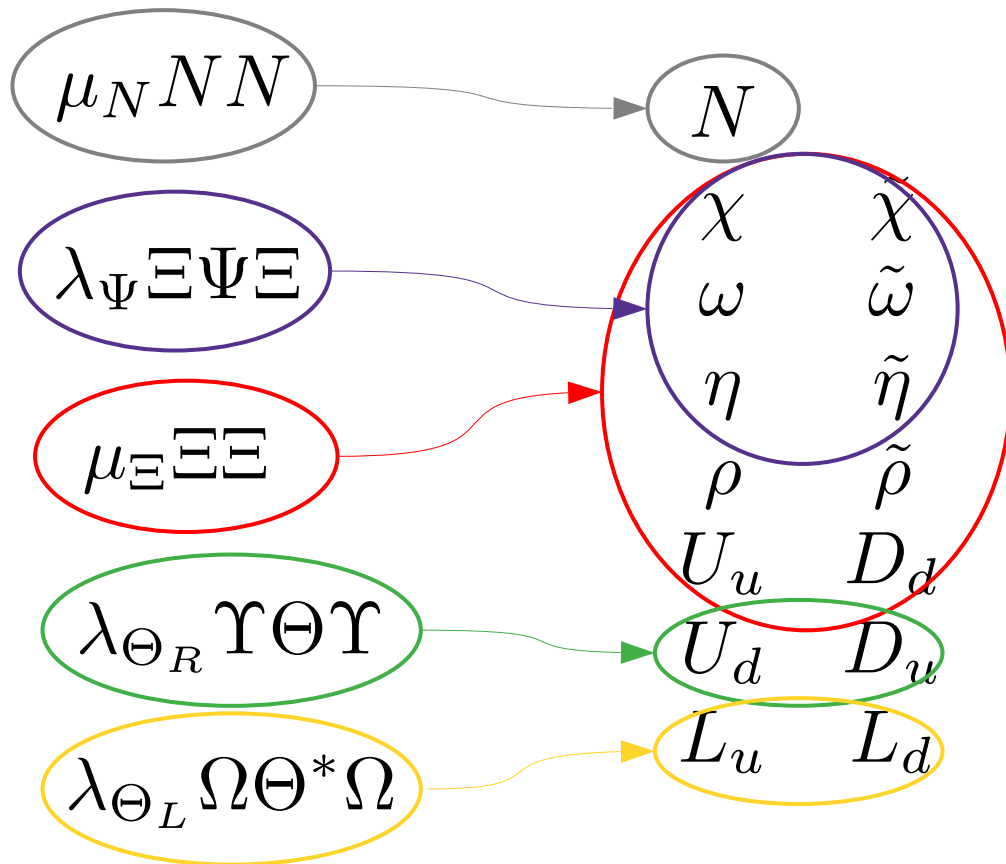
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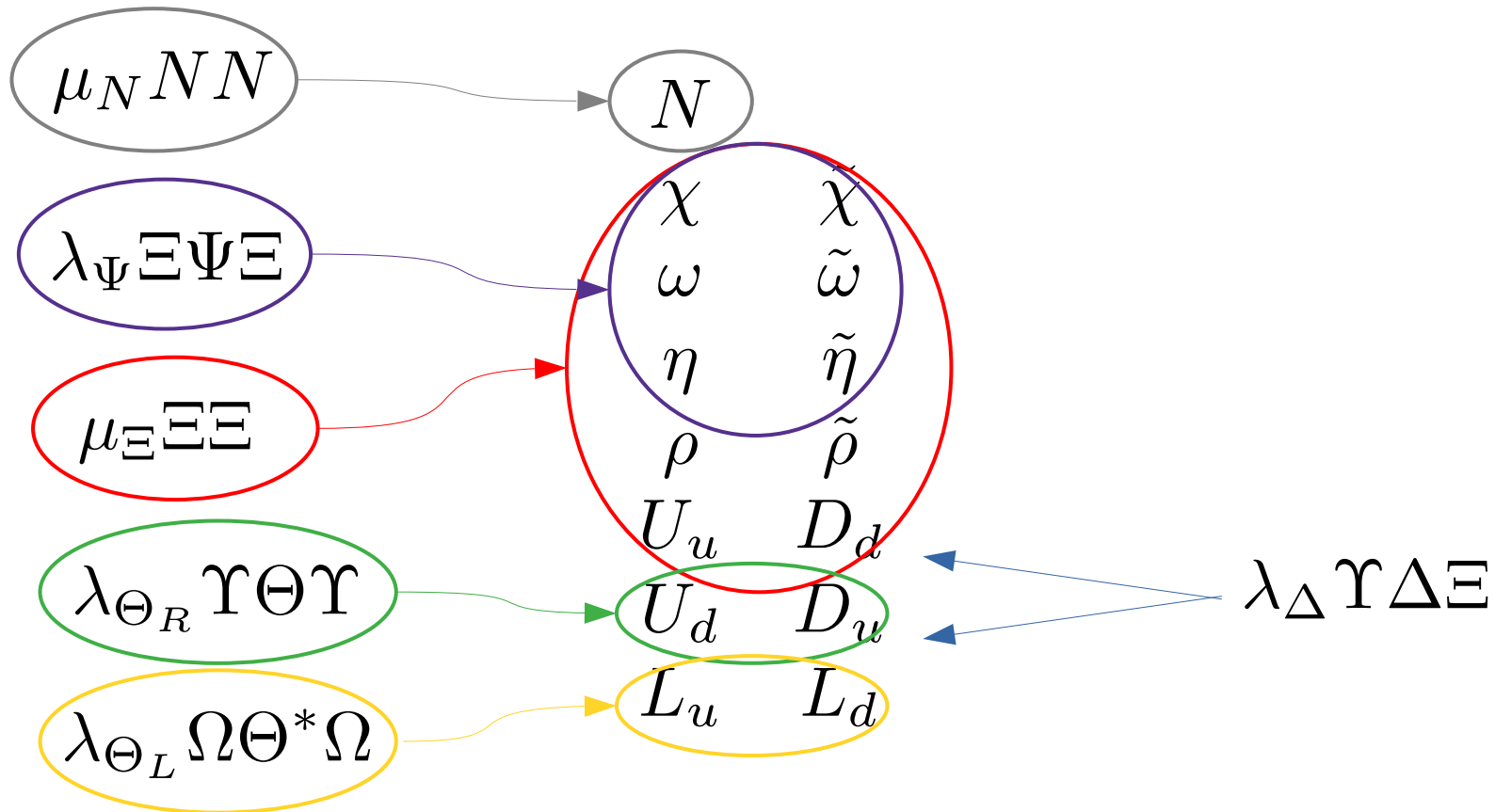
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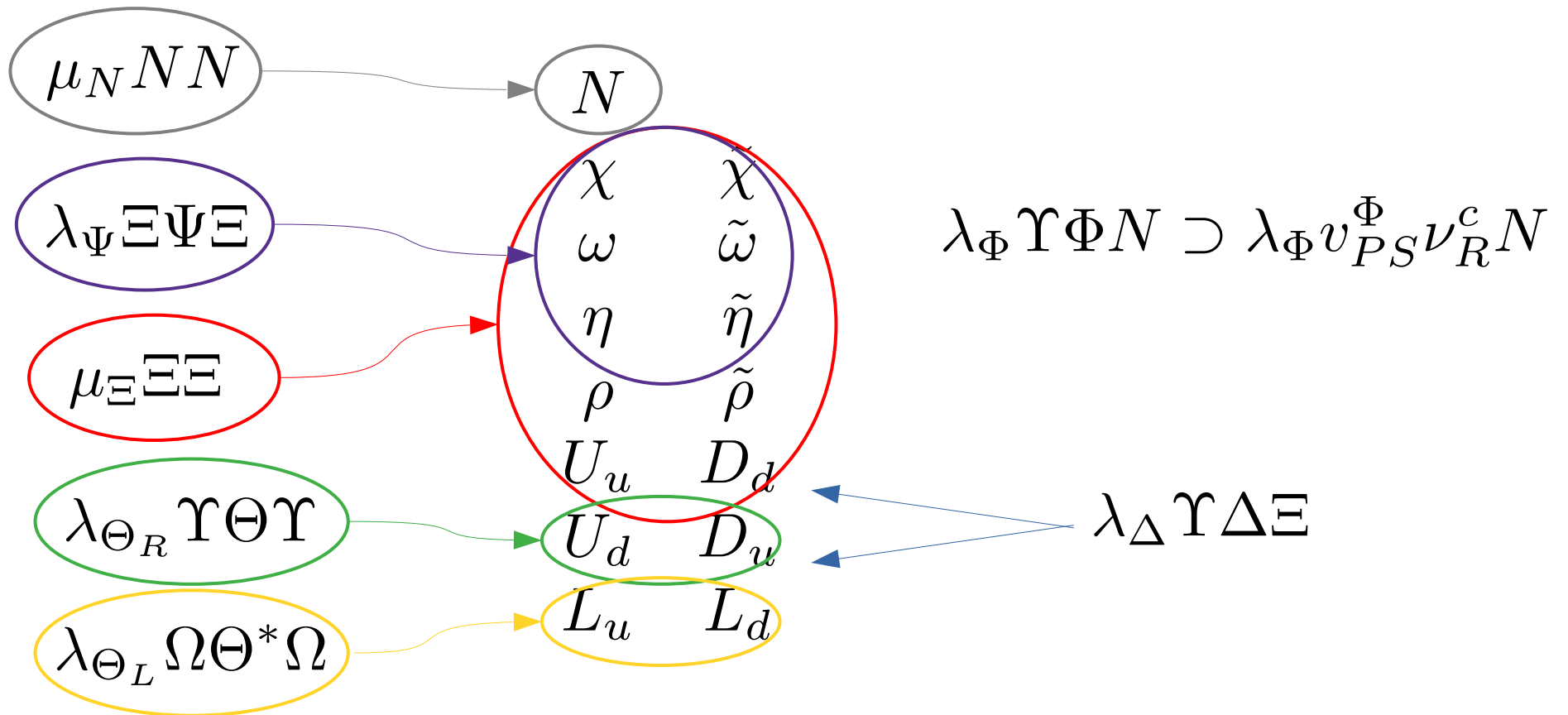
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- What about neutrinos ?

Fermion Masses

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- Neutrinos \rightarrow Inverse seesaw mechanism

So far so good

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Need Lattice Input !!

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How can we generalize that for the 3 families ?

Fermion Content

	$SU(8)_{PS}$	$SU(2)_R$	$SU(2)_L$
$\Omega^p = \begin{pmatrix} L_{u/d}^p \\ q_L^p \\ l_L^p \end{pmatrix}$	8	1	2
$\Upsilon^p = \begin{pmatrix} U_d & D_u \\ d_R^{c\ p} & u_R^{c\ p} \\ e_R^{c\ p} & \nu_R^{c\ p} \end{pmatrix}$	$\bar{8}$	2	1
$\Xi = \begin{pmatrix} U_u & \chi & \rho & \eta & \omega \\ D_d & \tilde{\chi} & \tilde{\rho} & \tilde{\eta} & \tilde{\omega} \end{pmatrix}$	$70 = A_4$	1	1
N^p	1	1	1

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Rank of the Mass Matrix

- Each species of fermion, t , b , τ , ν_τ gets its own mass matrix :

$$\begin{pmatrix} \langle O_{R1} O_{L1} \rangle & \langle O_{R1} O_{L2} \rangle & \langle O_{R1} O_{L3} \rangle \\ \langle O_{R2} O_{L1} \rangle & \langle O_{R2} O_{L2} \rangle & \langle O_{R2} O_{L3} \rangle \\ \langle O_{R3} O_{L1} \rangle & \langle O_{R3} O_{L2} \rangle & \langle O_{R3} O_{L3} \rangle \end{pmatrix}$$

- 3 families if rank 3 !

$$\mathcal{O}_{L,a} = y_{L,a} \mathcal{O}_L \quad \mathcal{O}_{R,a} = y_{R,a} \mathcal{O}_R \quad \rightarrow \quad \text{rank 1}$$

- We need different Baryonic Operators. How can we generate them ?

3 Flavors

3 Flavors

- Gauge mediation +1

3 Flavors

- Gauge mediation +1
- Scalar mediation

3 Flavors

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- Scalar mediation + 0

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- New Θ , scalar mediation +1
- New Δ_L , or Loops induced +1

So far so good

- UV completed the 4F (with scalars and gauge bosons)
- Generate mass for the **entire family**
- **Mass Hierarchy** between the fermions
- Large window to get a **Conformal Dynamic**

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- Large window to get a **Conformal Dynamic**
- Enough ingredients for a **Flavor Structure**

What is next ?

- Study of the complete potential
- Lattice input
- Well running of the gauge coupling

Alternatives ?

4-F=Scalars, scalars, scalars...

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- Use of a scalar to generate 4-F

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How to avoid the naturalness issue ?

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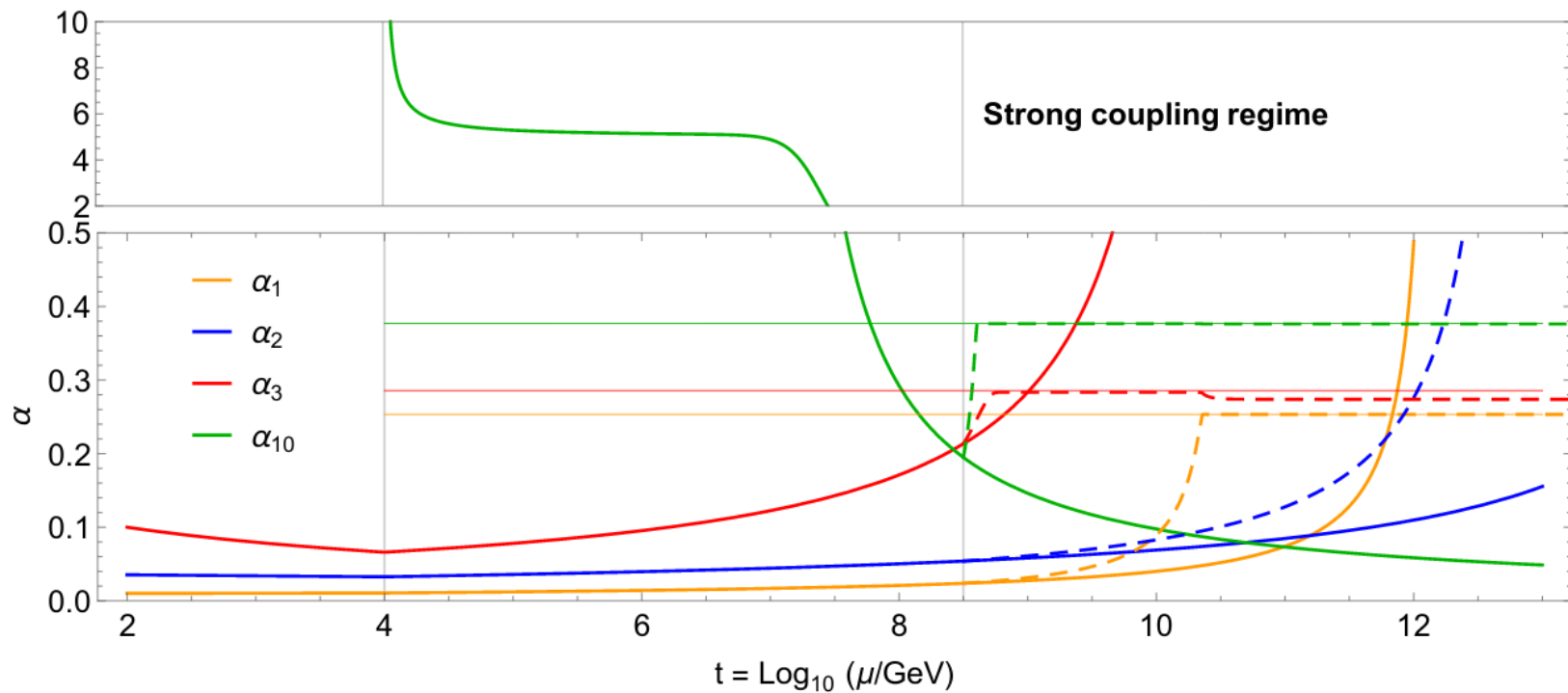
$$\beta = \sum_k \lambda_k \alpha^k = \sum_k \frac{F^{(k)}(\alpha)}{N^k}$$

Naturalness ?

$$\beta \cong \alpha^2 \left[1 + \frac{F(\alpha)}{N} \right]$$

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- **Composite Mediator ?**

Thank you !

Set-Up

Low energy target M8 \rightarrow Global Symmetry Pattern $SU(4)/Sp(4)$

Fundamental : 4 ψ

AntiSymmetric : 6 χ

$$\textcircled{H} = \langle LU \rangle = \langle LD \rangle$$

ψ	$SU(2)_L$	$U(1)_Y$
L	2	0
U	1	1/2
D	1	-1/2

Strong Dynamics

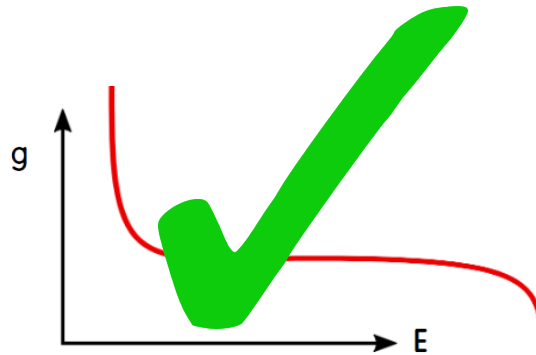
ψ Fundamental : $U_d, D_u, U_u, D_d, L, \eta, \tilde{\eta}$
 4 + 2 + 6 = 12 HyperFermions

$$\rightarrow G = SU(n), n \leq 12$$

How many are light ($\leq \Lambda_{HC}$)?
 $L + 2$ neutral

χ AntiSymmetric : $\chi, \tilde{\chi} = 6$ HyperFermions

Analytic tools : (PS & SD) \rightarrow



Need Lattice Input !!

4-F : Gauge Mediation

Step	Breaking Pattern
PS	$SU(8)_{PS} \times SU(2)_R \rightarrow SU(7)_{EHC} \times U(1)_E$
EHC	$SU(7)_{EHC} \rightarrow SU(4)_{CHC} \times SU(3)_c \times U(1)_X$
CHC	$SU(4)_{CHC} \times U(1)_X \times U(1)_E \rightarrow Sp(4)_{HC} \times U(1)_Y$

$$E_\mu : M_E^2 = \frac{g_{PS}^2}{4} (v_{EHC}^\Psi)^2$$

$$C_\mu : M_C^2 = \frac{g_{PS}^2}{4} (v_{EHC}^\Psi + v_{PS}^\Phi)^2$$

$$\mathcal{L}_{\text{Kinetic}} \supset -\frac{g_{EHC}^2}{2M_E^2} \left(\bar{L}^3 \bar{\sigma}^\mu q_L - \bar{t}_R^c \bar{\sigma}^\mu D_u^3 - \bar{b}_R^c \bar{\sigma}^\mu U_d^3 \right) \left(\frac{1}{2} \bar{\chi} \bar{\sigma}_\mu U_t - \frac{1}{2} \bar{D}_b \bar{\sigma}_\mu \tilde{\chi} - \bar{\eta} \bar{\sigma}_\mu \chi + \tilde{\chi} \bar{\sigma}_\mu \tilde{\eta} \right) \\ - \frac{g_{PS}^2}{2M_C^2} \left(\bar{L}^3 \bar{\sigma}^\mu l_L - \bar{\nu}_{\tau R}^c \bar{\sigma}^\mu D_u^3 - \bar{\tau}_R^c \bar{\sigma}^\mu U_d^3 \right) \left(-\frac{1}{2} \bar{\chi} \bar{\sigma}_\mu \tilde{\eta} - \frac{1}{2} \bar{\eta} \bar{\sigma}_\mu \tilde{\chi} \right)$$

Quark-Lepton mass splitting !

HyperFermion Masses

$$M_{\chi \tilde{\chi}} = M_{\omega \tilde{\omega}} \leq \Lambda_{HC}$$

$$M_{U/D} \leq \Lambda_{HC}$$

$$M_L \leq \Lambda_{HC}$$

$$M_{\eta \tilde{\eta}} \leq \mathcal{O}(10) \Lambda_{HC}$$

This is possible !



(only λ_{Δ} can be large)