

Towards an improved ice model for the Radio Neutrino Observatory Greenland (RNO-G).

Bob Oeyen for the RNO-G collaboration

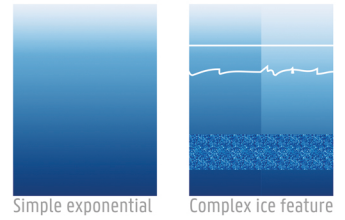
Knowing the radio optics of ice allows for more precise antenna position calibration of RNO-G

- Index of refraction at each point
- Internal reflections
- Absorption length
- Birefringence

single exponential,
double exponential,
exponential polynomial

Radio Neutrino Observatory - Greenland

In-ice askaryan radio detection of ultra-high-energy astrophysical neutrinos at Summit Station (Greenland)



We discovered an exponential ice model to be incompatible with pulser data → which can be resolved by modelling the ice data more carefully

First principles suggest $n(z) \sim \rho(z) \sim \exp(-z/z_0)$

$$n(z) = 1 + \text{cst} \cdot \rho(z) \quad \text{AND}$$

1. Densification due to stress of weight snow Simple exponential

$$\frac{d\rho}{\rho_{\text{ice}} - \rho} = \text{cst} \cdot \rho \cdot dz \quad \Rightarrow \quad \rho(z) = \rho_{\text{ice}} - (\rho_{\text{ice}} - \rho_{\text{snow}}) \exp(-z/z_0)$$

2. Steepening of densification at $\rho(z_{\text{crit}}) = 550 \text{ kg/m}^3$ Double exponential

$$\rho(z) = \rho_{\text{ice}} - (\rho_{\text{ice}} - \rho_{\text{snow}}) \exp(-z/z_{01}) \quad \text{for } z \leq z_{\text{crit}}$$

$$\rho(z) = \rho_{\text{ice}} - (\rho_{\text{ice}} - \rho_{\text{crit}}) \exp(-(z - z_{\text{crit}})/z_{02}) \quad \text{for } z > z_{\text{crit}}$$

3. Higher order features ?? Exponential polynomial

$$\rho(z) = \rho_{\text{ice}} + a_1 \exp(-z/z_0) + a_2 \exp^2(-z/z_0) + \dots + a_n \exp^n(-z/z_0) + \dots$$

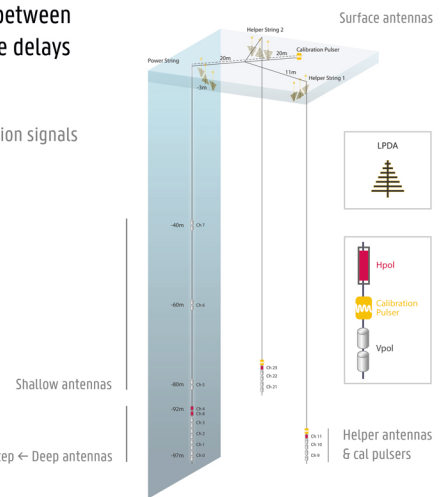
RNO-G antenna position calibration depends on ice optics

Minimize the difference between observed & expected time delays by moving antenna

$$\Delta t_{\text{obs}} \leftarrow \text{cross-correlation signals}$$

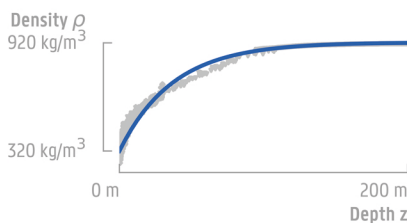
$$\Delta t_{\text{exp}} \sim n_{\text{avg}}$$

$$n_{\text{avg}} = \frac{\int_{z_{\text{pulsar}}}^{z_{\text{antenna}}} n(z) dz}{(z_{\text{antenna}} - z_{\text{pulsar}})}$$

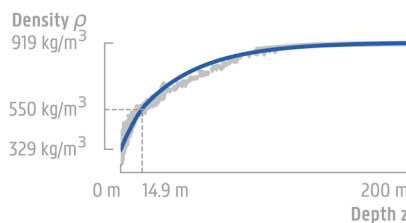


An exponential polynomial fit describes the upper ice better, resulting in more accurate timing

Simple exponential fit



Double exponential fit



Exponential polynomial fit

