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SB, Goertz, PRL 123 no.22, arXiv:1903.06146

SB, Csaki, Goertz, arXiv:2004.06120

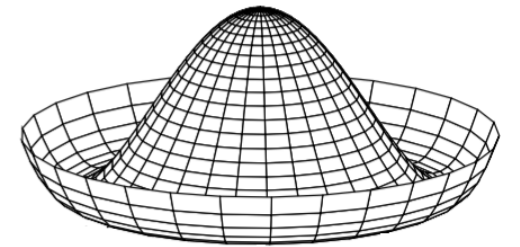
**SIMONE BLASI**

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# LITTLE HIERARCHY AND COMPOSITENESS

EOS be.h Winter Solstice Meeting, 16th December 2020

# THE HIERARCHY PROBLEM



New heavy thresholds introduce quadratic corrections to the BEH mass:  $\delta m_h^2 \sim \Lambda^2$

In the absence of an underlying mechanism the electroweak scale is unnatural.

## two possible approaches to BSM:

- ▶ Leave the HP aside and focus on more concrete issues of the SM.
- ▶ The HP may not be a problem at all, or solved in a way that can't be captured by EFT.
- ▶ Search for a structural solution to the HP based on QFT arguments.
- ▶ Uncovering the mechanism underlying EWSB will provide new insights for the other open questions.

# A COMPOSITE BEH BOSON?

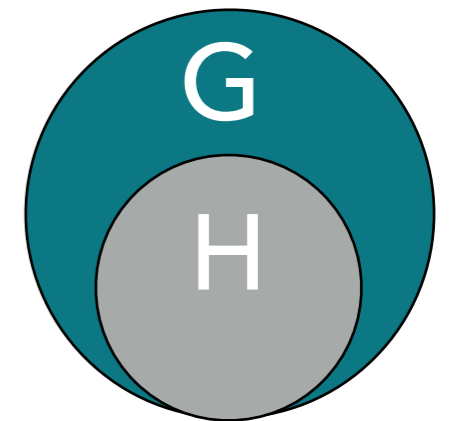
Kaplan, Georgi, Dimopoulos...



The BEH boson is no longer an elementary scalar but rather a **bound state** of a new strong dynamics which condenses not too far from the electroweak scale.

The HP is solved because the **finite size** of the BEH boson itself represents a cutoff for the corrections to the scalar potential.

Strong dynamics features a global symmetry  $G$  broken to  $H$  at the condensation scale:  $h$  boson as a **pseudo Nambu-Goldstone** boson.

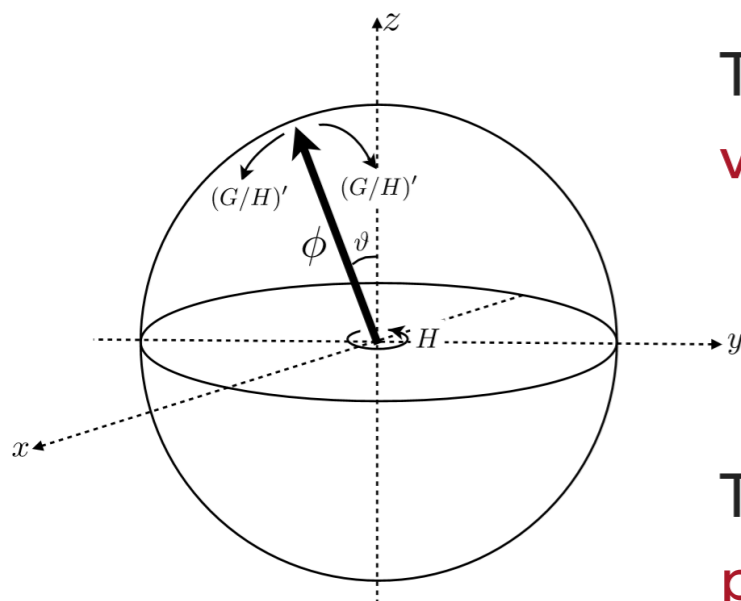


$$G \rightarrow H \supset SU(2) \times U(1)$$

The electroweak symmetry is broken via **vacuum misalignment**:

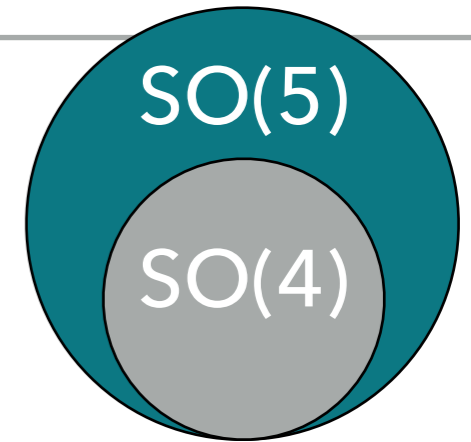
$$\xi \equiv \frac{v^2}{f^2} = \sin^2(\langle h \rangle / f)$$

The presence of a light SM-like  $h$  boson helps with **electroweak precision tests** (as opposed to *technicolor*).



# THE MINIMAL COMPOSITE HIGGS MODEL

Agashe, Contino, Pomarol 2005

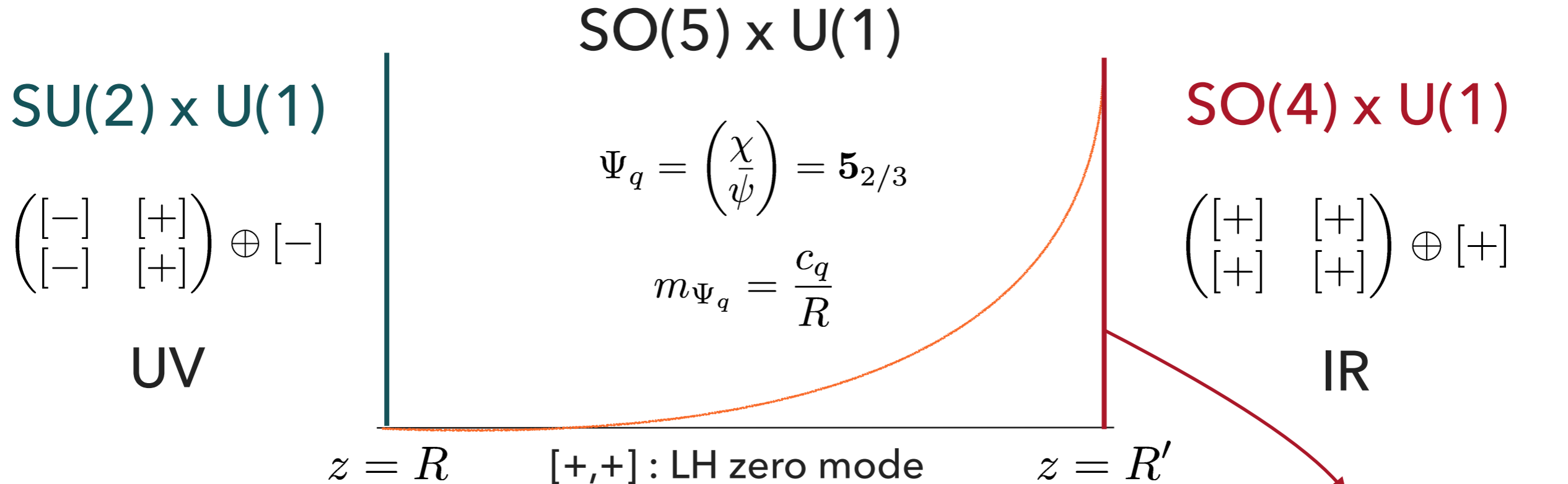


- $G = SO(5)$  and  $H = SO(4)$ :  $G/H$  contains 4 dofs + custodial protection, best realization by means of holography.
  - ▶ Slice of AdS delimited by UV brane and IR brane.
  - ▶  $SO(5)$  gauge symmetry in the bulk reduced to  $SU(2) \times U(1)$  on the UV brane,  $SO(4)$  on the IR brane via dedicated boundary conditions + brane-localized terms.
  - ▶ Gauge-Higgs unification:  $h$  doublet as scalar component of  $SO(5)/SO(4)$  broken gauge fields.
  - ▶ SM fermions embedded in 5D fields, flavor puzzle addressed by partial compositeness + explicit breaking.

\*One also needs an extra  $U(1)$  factor to reproduce fermion hypercharges.

# PARTIAL COMPOSITENESS

DIRICHLET TYPE  $[+] : \psi = 0$   
 $[-] : \chi = 0$



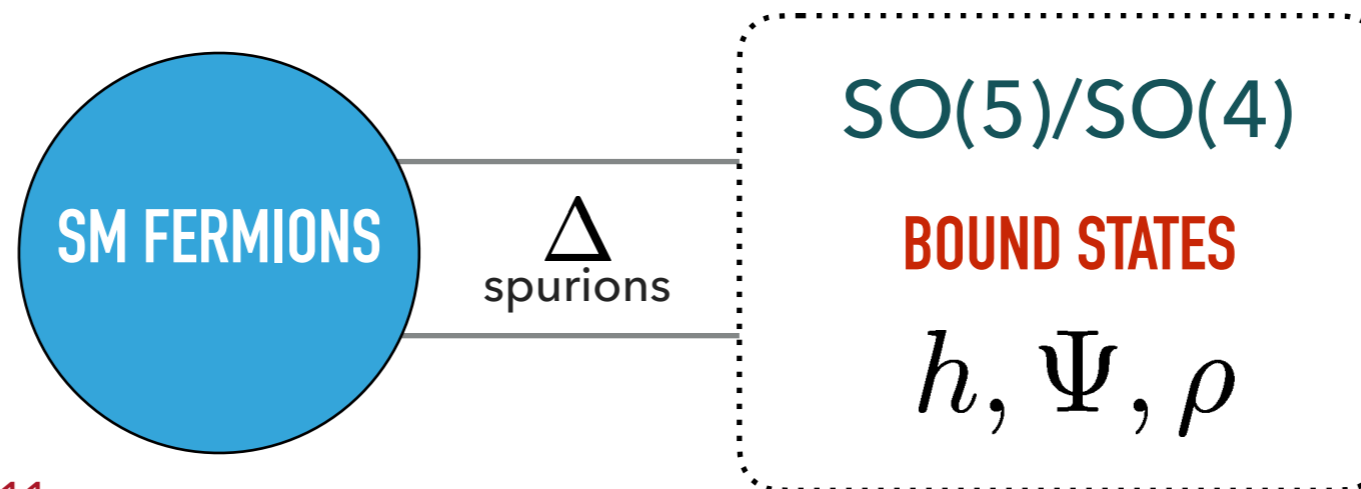
brane localized terms to  
give mass to SM fermions

- ▶ SM fermions as zero-modes.
- ▶ Specific boundary conditions break  $SO(5)$ .
- ▶ 5D bulk masses impact localization of the zero-modes and hence their masses after EWSB.

$$R \sim M_{\text{Pl}}^{-1}$$

$$R' \sim \text{TeV}^{-1}$$

# PARTIAL COMPOSITENESS



DeCurtis et al.'11, Panico et al.11..

- ▶ 4D effective theory below the condensation scale describes a **mixing** between SM fermions and composite resonances:

$$\mathcal{L}_{\text{mixing}} = \lambda_L \bar{q}_L \Delta_L U \Psi_R + \lambda_R \bar{t}_R \Delta_R U \Psi_L + \text{h.c.}, \quad U = \exp \left( -i \frac{\sqrt{2}}{f} T^{\hat{a}} h_a \right)$$

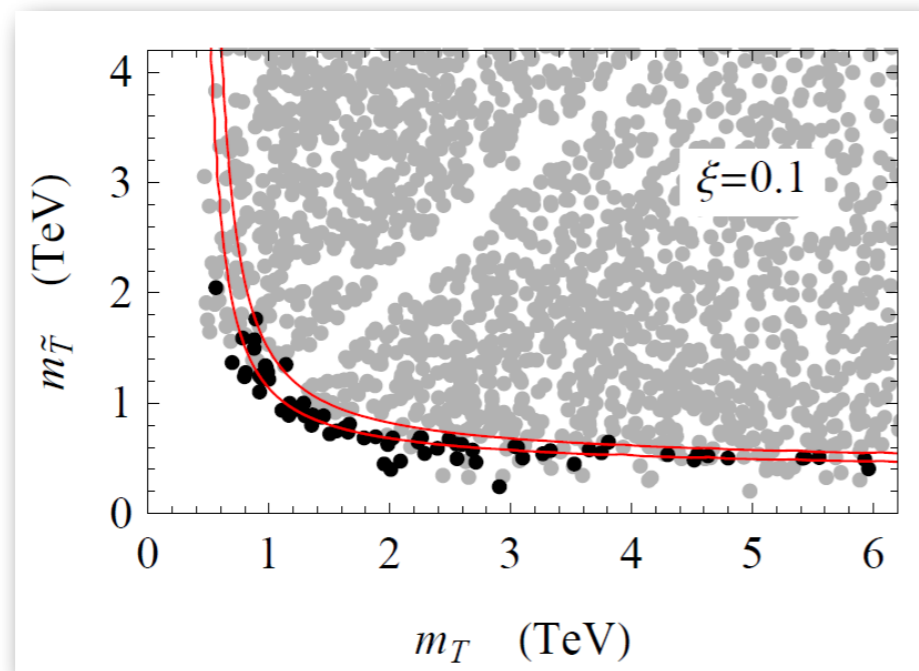
- ▶ Spurions signal explicit breaking due to SM fermions being **incomplete** SO(5) **irreps** (specific boundary conditions in 5D): largest contribution from the top quark.

$$\Delta_R = (0, 0, 0, 0, 1) \quad \Leftrightarrow \quad \left( \begin{array}{cc} [-, +] & [-, +] \\ [-, +] & [-, +] \end{array} \right) \oplus [-, -]$$

# LIGHT TOP PARTNERS

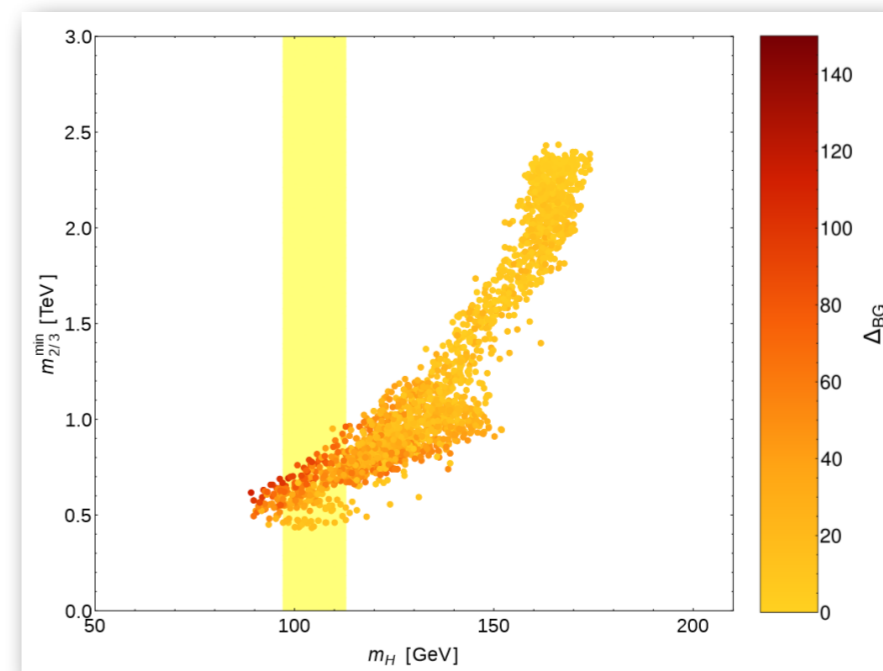
$$m_h \sim \frac{m_T}{f} m_t$$

4D effective theory



Matsedonskyi, Panico, Wulzer 2012

5D holographic

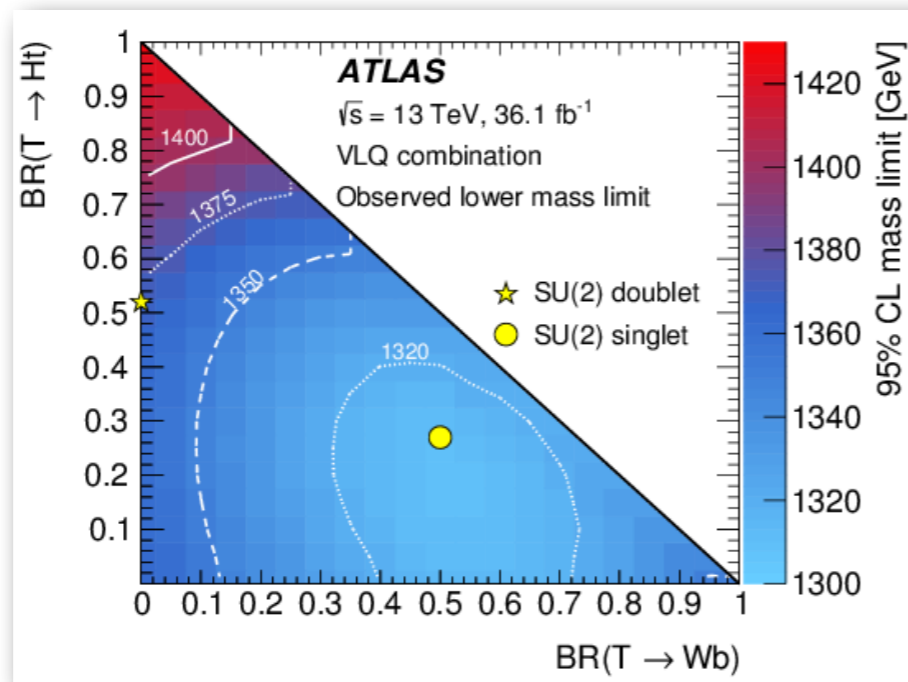


Carmona, Goertz 2015

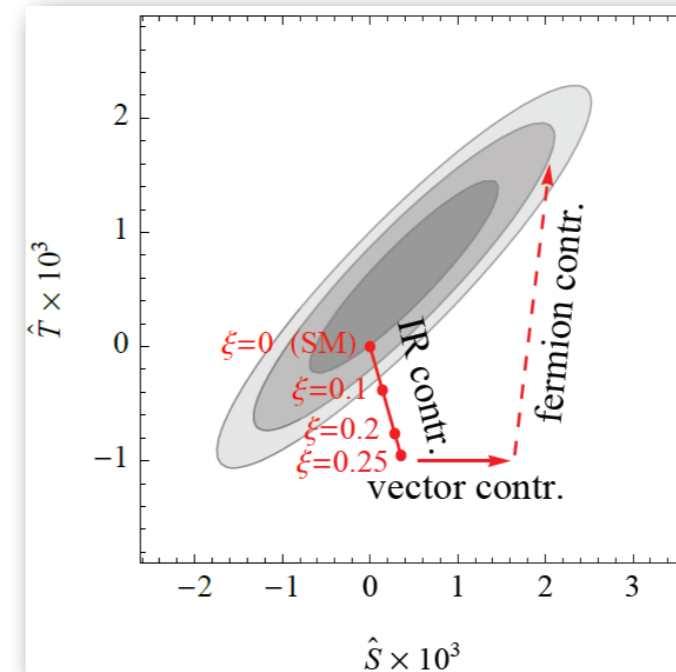
- ▶ Minimal realizations such as the MCHM5 and MCHM10 predict **light top partners** in order to be compatible with a light h boson (anomalously light KK in 5D).
- ▶ **Strong correlation** between top yukawa and explicit breaking requires light states to cure it.

# EXPERIMENTAL CONSTRAINTS

$$m_h \sim \frac{m_T}{f} m_t$$



Grojean et al. 2013



- ▶ Direct searches can constrain top partners as heavy as 1.4 TeV.
- ▶ The only way minimal models can comply with this is by making the h boson more elementary, namely increasing the condensation scale.

**THE TUNING INCREASES AND SURPASSES THE 10% IMPLIED BY LEP**

$$\Delta \propto \frac{1}{\xi} = \frac{f^2}{v^2}$$



# POSSIBLE SOLUTIONS

- ▶ **Raise** the scale  $f$  as much as necessary to comply with current constraints
- ▶ Move to **non-minimal** models
- ▶ Keep the MCHM but change representations (**14**) *Panico et al.'12*
- ▶ Inclusion of a realistic **lepton** sector *Carmona, Goertz'15*
- ▶ Enhance the (**maximal**) symmetry *Csaki et al.'17*
- ▶ New physics as a **continuum** rather than particle excitation *Georgi'05, Csaki et al.'18*
- ▶ Make partners **uncolored** (twin-Higgs) *Chacko et al.'05, Barbieri et al.'05..*
- ▶ ...

**THIS TALK**

- ▶ **Soften** the explicit breaking & **maximal** symmetry *SB, Goertz '19, SB, Goertz, Csaki '20*

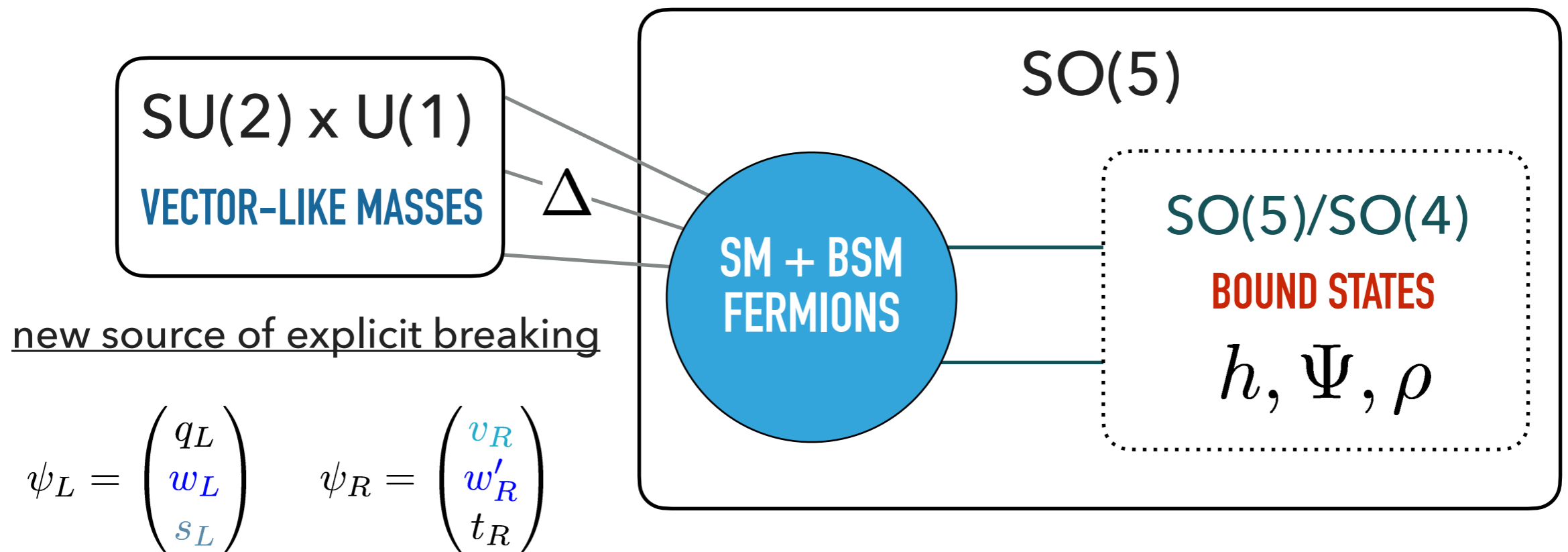
# A SOFT COMPOSITE BEH

SB, Goertz 2019



We want to construct a model that:

- keeps **minimality** and the nice features of **partial compositeness**
- **gets rid** of the **correlation** between h boson mass and top partners



new source of explicit breaking

$$\psi_L = \begin{pmatrix} q_L \\ w_L \\ s_L \end{pmatrix} \quad \psi_R = \begin{pmatrix} v_R \\ w'_R \\ t_R \end{pmatrix}$$

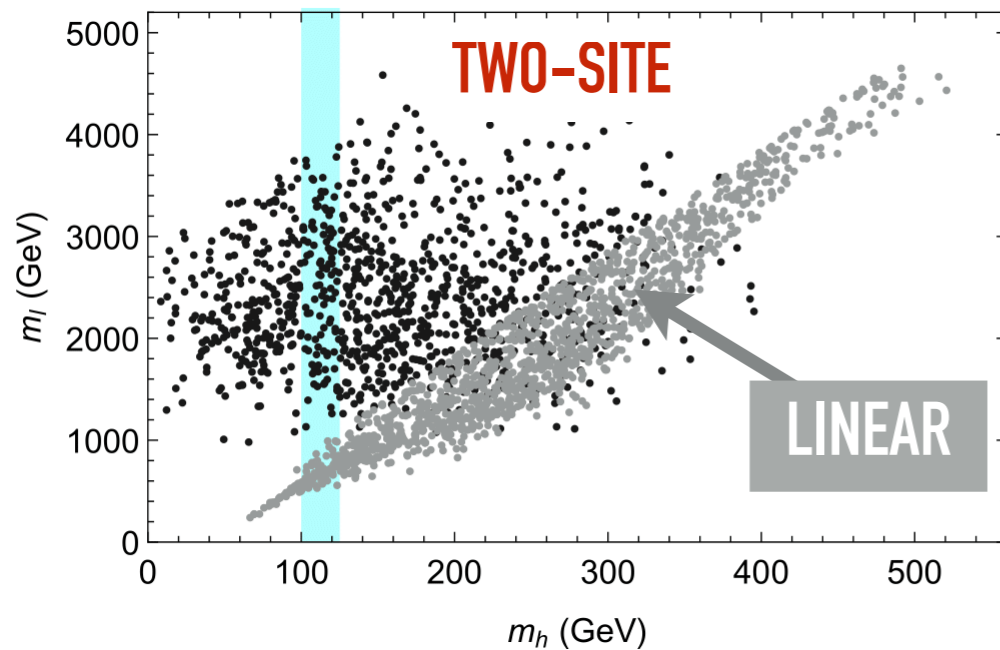
\*SM gauge bosons still couple directly to strong sector

# A SOFT COMPOSITE BEH

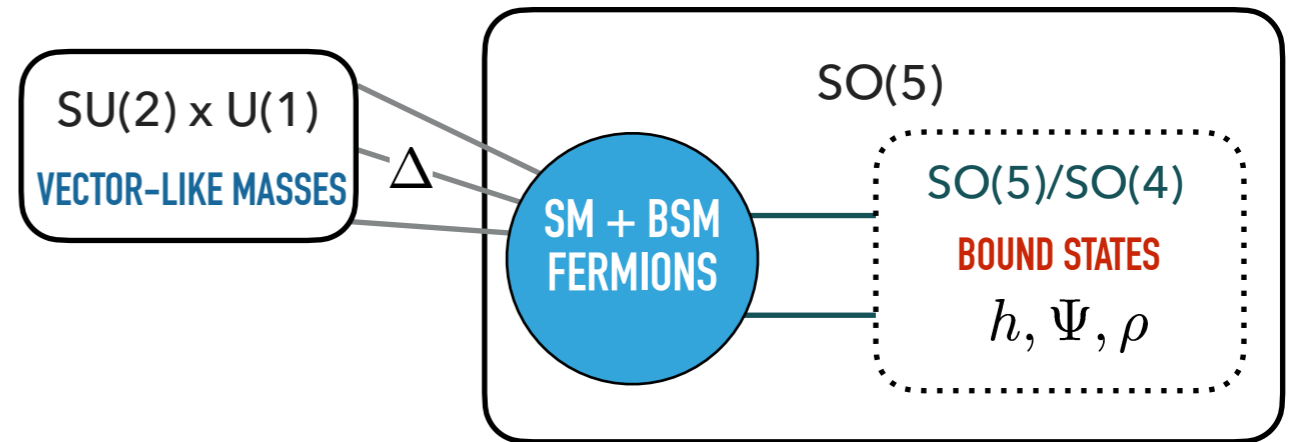
SB, Goertz 2019

## TWO RELEVANT LIMITS:

- Vector-like masses  $\gg$  compositeness scale: no effect (decoupling).



- Intermediate case: correlation between h mass and top partner masses is broken!



- Vector-like masses  $\ll$  compositeness scale: light top partners "by hand".

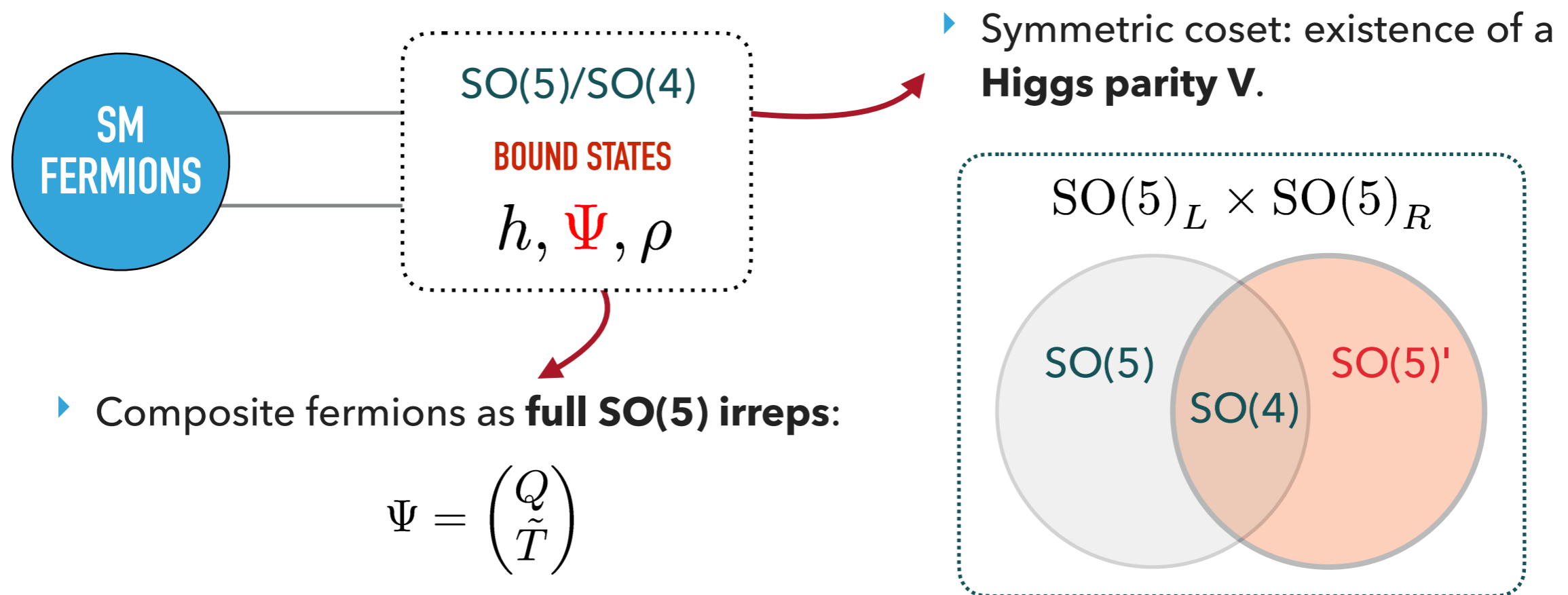
- ▶ h boson generically **lighter** wrt standard partial compositeness
- ▶ Heavy top partners are now compatible **without** raising **f**

# MAXIMAL SYMMETRY

Csaki et al.'17,'18

$$V^\dagger T^a V = T^a, \quad V^\dagger T^{\hat{a}} V = -T^{\hat{a}}$$

It is a symmetry of the strong sector that can emerge under certain assumptions.



- **Largest symmetry group** with non-zero masses for composite fermions still generating a potential for h:

$$\mathcal{L}_{\text{mass}} = \bar{\Psi}_L [(m_Q + \cancel{\tilde{m}_T}) + (m_Q - \tilde{m}_T)V] \Psi_R + \text{h.c.}$$

# MAXIMAL SYMMETRY

Csaki et al.'17,'18

$$V^\dagger T^a V = T^a, \quad V^\dagger T^{\hat{a}} V = -T^{\hat{a}}$$

Imposing maximal symmetry further constrains the structure of the generated h potential ensuring structural cancellations.

In particular, there is unbroken **Higgs parity** as long as fermions are concerned:

$$\sin^2(h/f) \leftrightarrow -\cos^2(h/f) \Rightarrow \xi \equiv \frac{v^2}{f^2} = 0.5$$

Gauge contribution can however be important as well, and helps misalign the vacuum in the right way.

$$\Delta_{\text{max sym}} \simeq \frac{f^2}{v^2} = 9 \left( \frac{m_T}{1 \text{ TeV}} \right)^2$$

$$\Delta_5 \simeq \frac{f^2}{v^2} \left( \frac{g_*}{\lambda} \right)^2 \sim 90 \left( \frac{m_T}{1 \text{ TeV}} \right)^2$$

**DOUBLE TUNING IS REMOVED!**

(Standard MCHM5 [Panico, Redi, Tesi 2012](#))

# SMALL SUMMARY

Minimal models with partial compositeness predict light top partners: their non-observation at the LHC cuts in parameter space previously unconstrained by LEP and worsens the fine-tuning.

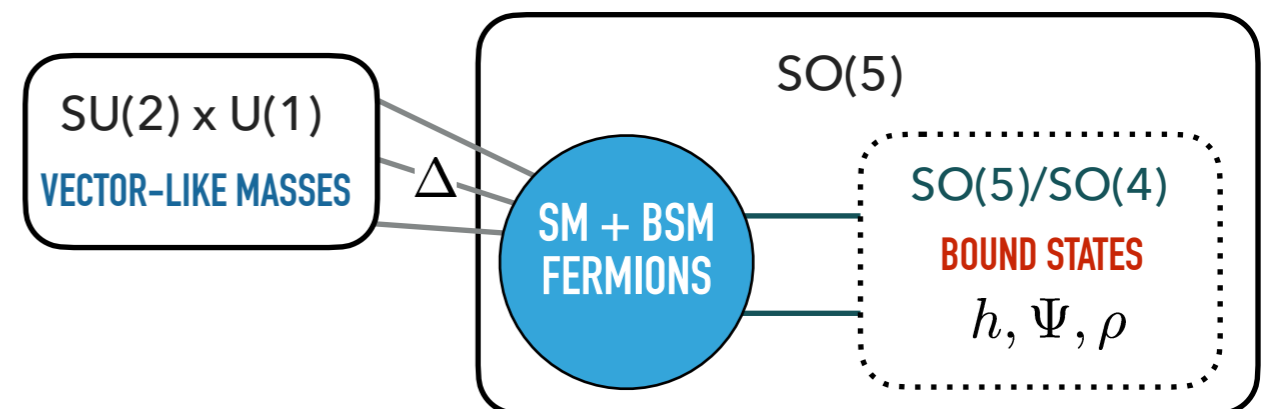
## FULL SO(5) MULTIPLETS

### MAXIMAL SYMMETRY



- Solves **double tuning**, but still quadratic growth with **top partner** masses.
- **Trigonometric parity** unbroken, **needs cancellation** against gauge contribution.

### SOFT BREAKING

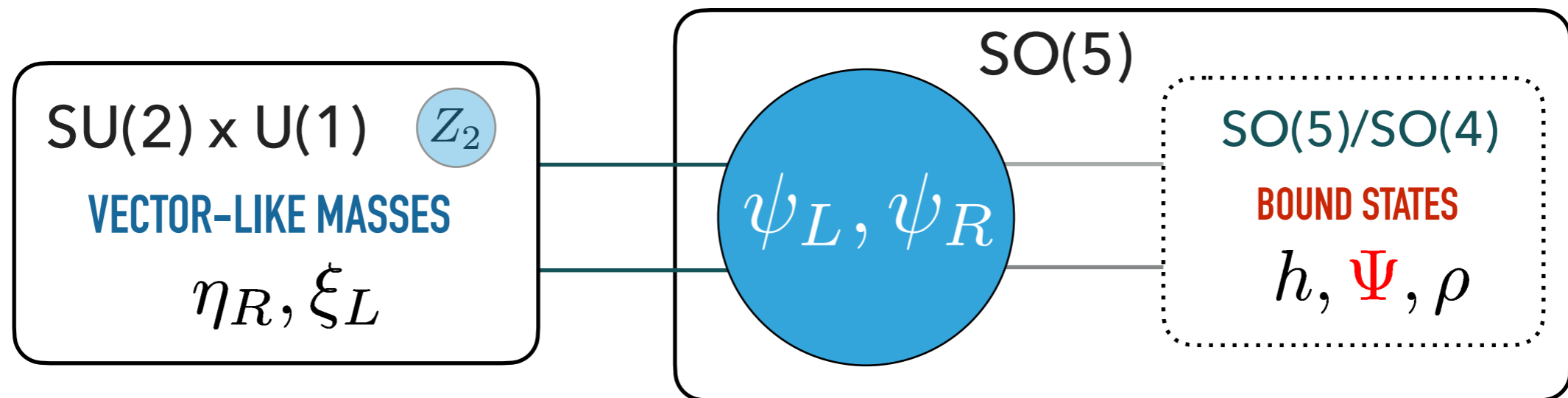


- Breaks correlation between h mass and **top partner mass**.
- Overall tuning still rather large as soft breaking does not solve **double tuning**.

# SOFT BREAKING & MAXIMAL SYMMETRY

SB, Csaki, Goertz 2020

The idea is to enhance the symmetry both on the elementary and composite side to obtain a fully natural spectrum of resonances that is compatible with LHC.



$$\mathcal{L}_{\text{el}} = \bar{\eta}_R M_R \psi_L + \bar{\xi}_L M_L \psi_R$$

$$\mathcal{L}_{\text{linear}} = \lambda_L \bar{\psi}_L U \Psi_R + \lambda_R \bar{\psi}_R U \Psi_L$$

$$\mathcal{L}_{\text{mass}} = M \bar{\Psi}_L V \Psi_R$$

UV-BRANE LOCALIZED SPINORS

$$\eta_R = (w_R, s_R) \quad \xi_L = (w'_L, v_L)$$

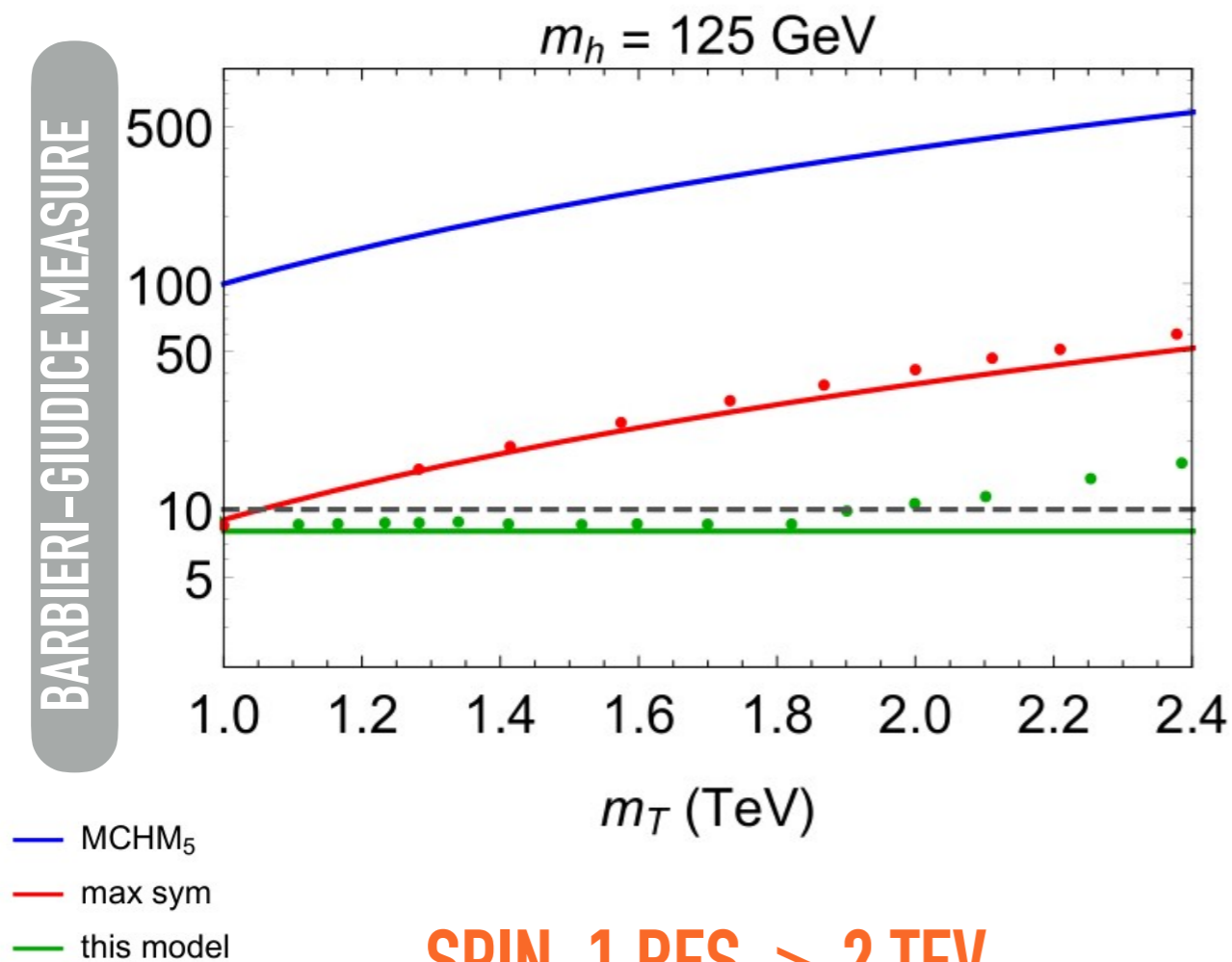
$SO(5)$ -SYMMETRIC PARTIAL COMP.

\*Successful combination requires simple modification of the minimal embedding for the VL fermions

$SO(5)'$  MAXIMAL SYMMETRY

# SOFT BREAKING & MAXIMAL SYMMETRY

**Natural spectrum** above the LHC bounds compatible with a **light h boson**.



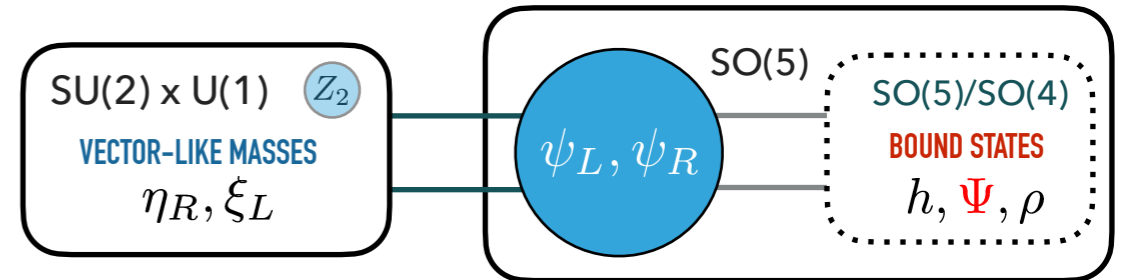
**SPIN-1 RES. > 2 TEV**  
( > 3 TEV: 15)

- Trigonometric parity broken in a controlled way: right misalignment no longer requires cancellation against gauge sector.
- Fine-tuning at the **10%** already implied by LEP and **almost flat** along  $m_T$ .
- Soft breaking makes the h boson mass compatible with heavy partners by reducing  $\beta$  instead of raising  $f$ .
- Maximal symmetry provides the connection  $\alpha \leftrightarrow \beta$  due to trig. parity and removes double tuning.



# UNIVERSAL BOUNDARY CONDITIONS

All the features that we have employed have a simple interpretation in the holographic 5D setup.



$$S_{UV} = \int d^4x \left\{ -i\eta_R \sigma^\mu \partial_\mu \bar{\eta}_R - i\bar{\xi}_L \bar{\sigma}^\mu \partial_\mu \xi_L + \frac{1}{\sqrt{R}} \chi_l(R) M_R^\dagger \eta_R + \frac{1}{\sqrt{R}} \psi_r(R) M_L^\dagger \xi_L + \text{h.c.} \right\}$$

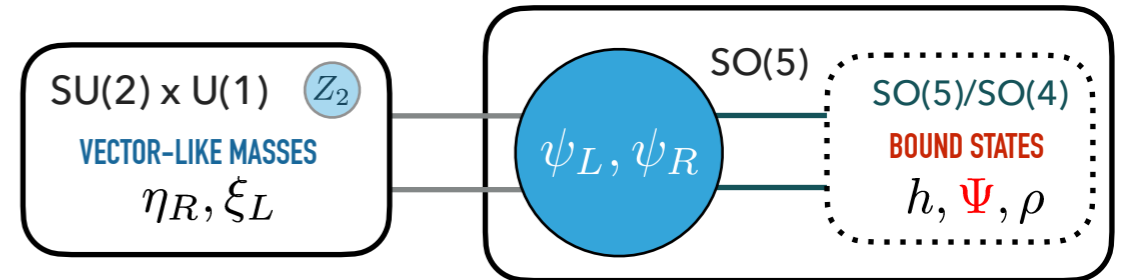
1. Complete SO(5) multiplets are the fundamental objects one starts with in 5D.
  - ▶ The spectrum of zero-modes (SM fermions) looks in fact incomplete because of static and specific boundary conditions.
  - ▶ Soft breaking means universal boundary conditions made dynamical by UV-localized action.

$$\Psi_{l,r} = \begin{pmatrix} \chi \\ \bar{\psi} \end{pmatrix}$$

$$\left( \begin{matrix} [-, +] & [+ , +] \\ [-, +] & [+ , +] \end{matrix} \right) \oplus [-, +] \rightarrow [+ , +]$$

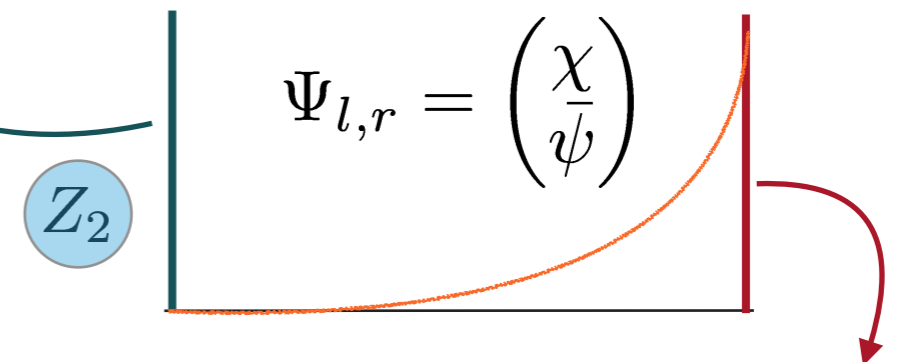
# UNIVERSAL BOUNDARY CONDITIONS

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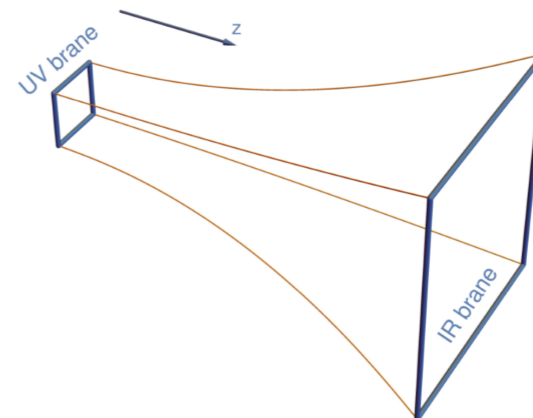
$$S_{UV} = \int d^4x \left\{ -i\eta_R \sigma^\mu \partial_\mu \bar{\eta}_R - i\bar{\xi}_L \bar{\sigma}^\mu \partial_\mu \xi_L + \frac{1}{\sqrt{R}} \chi_l(R) M_R^\dagger \eta_R + \frac{1}{\sqrt{R}} \psi_r(R) M_L^\dagger \xi_L + \text{h.c.} \right\}$$

2. Maximal symmetry is implemented by requiring the IR-localized action to respect  $SO(5)'$ .
3. Similarly, the discrete symmetry is imposed on the UV brane and only broken in the IR.
4. The mass of the 4D vector-like fermions can be TeV-scale due to wave-function suppression: automatically at work for third generation quarks.



$$\Psi_{l,r} = \begin{pmatrix} \chi \\ \bar{\psi} \end{pmatrix}$$

IR-localized terms are **SO(5)'** invariant



# UNIVERSAL BOUNDARY CONDITIONS

$$\eta_R = (w_R \textcircled{s_R}) \quad \xi_L = (w'_L, v_L)$$

- If the brane-masses on the UV are too large, boundary conditions are no longer dynamical (decoupling): brane-localized spinors as Lagrange multipliers. [Contino et al.'04](#)

$$S_{UV} = \int d^4x \left\{ -i s_R \sigma^\mu(x) \partial_\mu \bar{s}_R(x) + \frac{1}{\sqrt{R}} s_L(x, R) \mu_s s_R(x) + \text{h.c.} \right\} \quad \mu_s \sim \mathcal{O}(1)$$

- We can investigate the dynamical-to-static transition as a function of brane mass for the simplest case in which only the singlet state is active.

$$\text{UV brane: } \bar{s}_R(x) \quad \text{Bulk: } \Psi_l^1[+, +] = \begin{pmatrix} s_L(x, z) \\ \bar{\sigma}_R(x, z) \end{pmatrix} \quad \text{IR brane: empty}$$

- Kaluza-Klein decomposition & normalization of the profiles:

$$\bar{s}_R(x) = \sum_n e_n \bar{\psi}_n(x) \quad s_L(x, z) = \sum_n g_n(z) \chi_n(x) \quad \bar{\sigma}_R(x, z) = \sum_n f_n(z) \bar{\psi}_n(x)$$

$$\left( e_n^2 + \int_R^{R'} dz a(z)^4 g_n(z)^2 = 1 \right) \quad \int_R^{R'} dz a(z)^4 f_n(z)^2 = 1$$

# UNIVERSAL BOUNDARY CONDITIONS

$$\eta_R = (w_R \circledast s_R) \quad \xi_L = (w'_L, v_L)$$

- The [+,+] boundary condition is perturbed by the presence of the UV action:

Csaki'03..  $f_n(R') = 0, \quad f_n(R) = 0 \quad \rightarrow \quad f_n(R) - \frac{\mu_s^2}{m_n R} g_n(R) = 0$

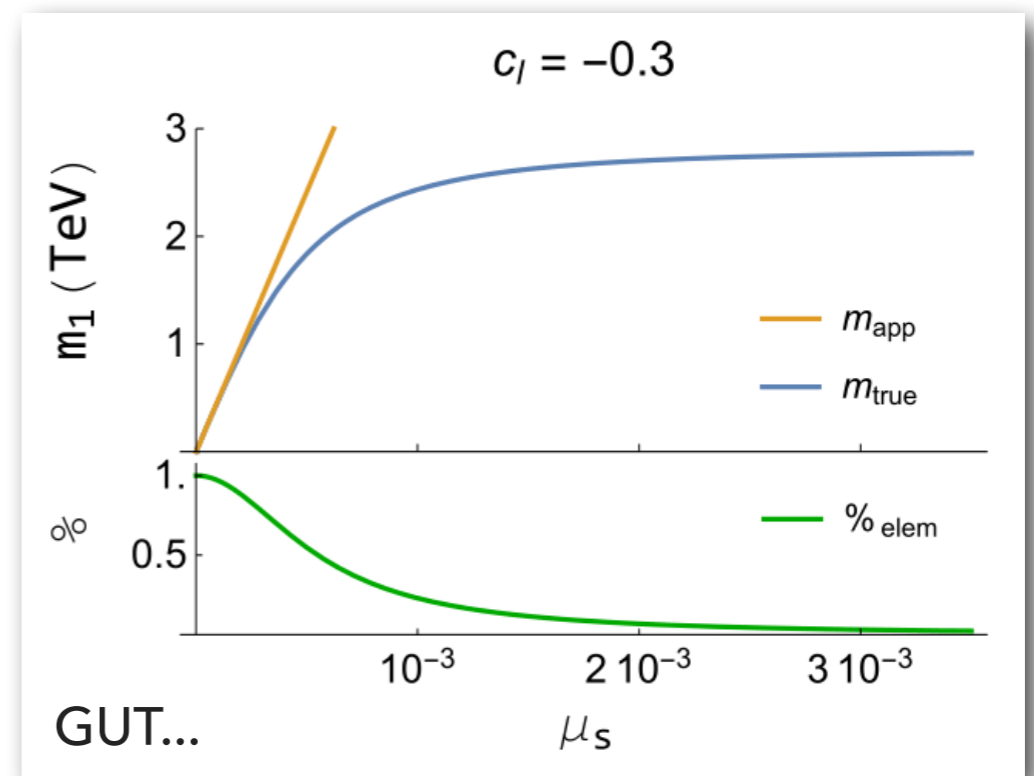
- Mass of the first Kaluza-Klein excitation:

$$m_1^2 \sim \begin{cases} (2c_l - 1)\mu_s^2 R^{-2} & \text{blue circle} \\ (1 - 4c_l^2)\mu_s^2 R'^{-2} \left(\frac{R}{R'}\right)^{-1-2c_l} & \text{red circle} \end{cases}$$

- ▶ Would-be zero mode UV localized: light partially-elementary KK is unnatural.

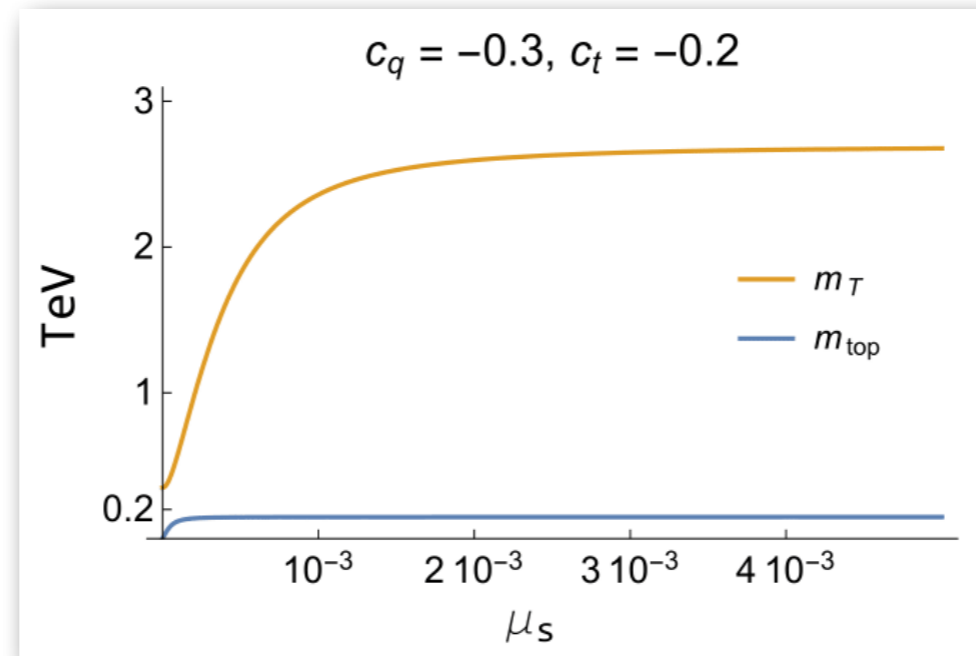
▶ Deep IR localization: TeV-scale KK with large overlap with UV-localized spinors.

- ▶ Still too large brane masses: would-be zero mode migrates towards higher KK states and [-,+ ] is effectively recovered (light custodian).



# UNIVERSAL BOUNDARY CONDITIONS

$$\eta_R = (w_R, s_R) \quad \xi_L = (w'_L, v_L)$$



- Wave-function suppression can produce partially-elementary KK states in case of deep IR localization: **third generation quarks!**
- The **top mass** can be reproduced in presence of partially-elementary KK states confirming the results of the 4D effective theory.
- The actual 5D calculation of the  $h$  potential is ongoing.

SB, Bollig, Goertz, in prep.

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# CONCLUSION

- we have presented a new realization of composite h boson in which partial compositeness respects the global symmetry
- this removes the correlation between the h mass and the top partner masses, allowing for a light h boson with heavy top partners without raising the compositeness scale
- main source of tuning is not irreducible and can be largely cut down whenever other ingredients are added
- we have presented the combination of soft breaking with maximal symmetry which turns out to be a perfect match (double tuning, misalignment, fully softened potential)
- enhancing the symmetry on both the elementary and composite sides allows for a natural model to emerge: spectrum of resonances above 2 TeV is now compatible with minimal 10% tuning already implied by LEP

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# CONCLUSION

- all the ingredients of the 4D effective theory can be naturally realized in the 5D picture corroborating our results
- soft breaking corresponds to universal and dynamical boundary conditions that replace the static and specific ones in the original realization
- a partially-elementary KK state appears at low-energy in case of deep IR localization: automatic for third generation quarks (which in fact create the issue of top partners in the first place...)

**THANK YOU!**

# PARTIAL COMPOSITENESS

- Linear couplings between SM quarks and composite operators:

$$\mathcal{L} = \lambda_L \bar{q}_L^i \mathcal{O}_R^i + \lambda_R \bar{q}_R^i \mathcal{O}_L^i + \text{h.c.}$$

- Large hierarchies in the masses from RG-evolution with strong dynamics:

$$m_q \sim v \left( \frac{\Lambda}{\Lambda_{UV}} \right)^{\gamma_L + \gamma_R}$$

- ▶ Very sensitive depending on the sign
- ▶ Linear couplings allow large masses without reintroducing the HP

- Anomalous dimensions have simple interpretation in terms of bulk masses of the 5D field in which the chirality  $q$  is embedded:

$$\gamma = [\mathcal{O}] - 5/2 = c - 1/2$$

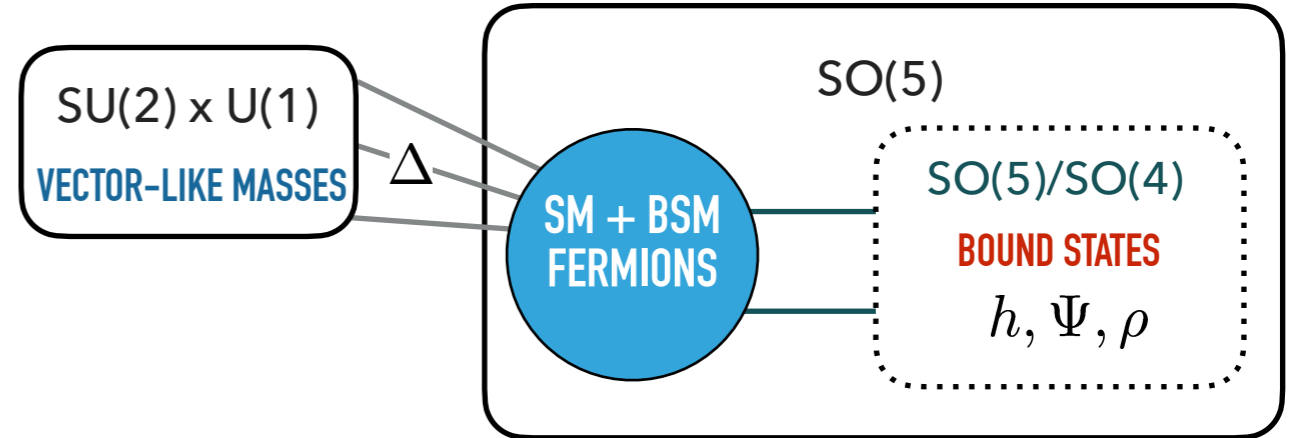
\*Purely 4D models generically predict additional pNGBs, partial compositeness only works for top quark (the strong dynamics has to condense). [Ferretti, Karateev'13](#)



# A SOFT COMPOSITE BEH

SB, Goertz 2019

## MINIMAL EMBEDDING: s,v,w



- The SM fermions are completed to full SO(5) irreps:

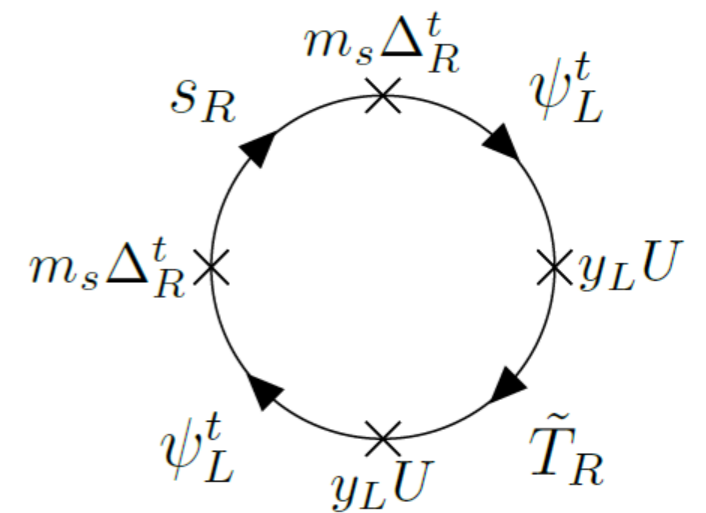
$$\Delta_L^\dagger q_L = \begin{pmatrix} q_L \\ 0 \\ 0 \end{pmatrix} \rightarrow \psi_L = \begin{pmatrix} q_L \\ w_L \\ s_L \end{pmatrix} \quad \Delta_R^\dagger t_R = \begin{pmatrix} 0 \\ 0 \\ t_R \end{pmatrix} \rightarrow \psi_R = \begin{pmatrix} v_R \\ w_R \\ t_R \end{pmatrix}$$

$$\mathcal{L}_{\text{linear}} = \lambda_L \bar{\psi}_L U \Psi_R + \lambda_R \bar{\psi}_R U \Psi_L + \text{h.c.}$$

- Explicit breaking moved from partial compositeness to elementary sector:

$$\begin{aligned} \mathcal{L}_{\text{el}} &= m_v \bar{v}v + m_w \bar{w}w + m_s \bar{s}s \\ &= m_v \bar{v}_L \Delta_L \psi_R + m_w \bar{\psi}_L \Gamma_w \psi_R + m_s \bar{s}_R \Delta_R \psi_L \end{aligned}$$

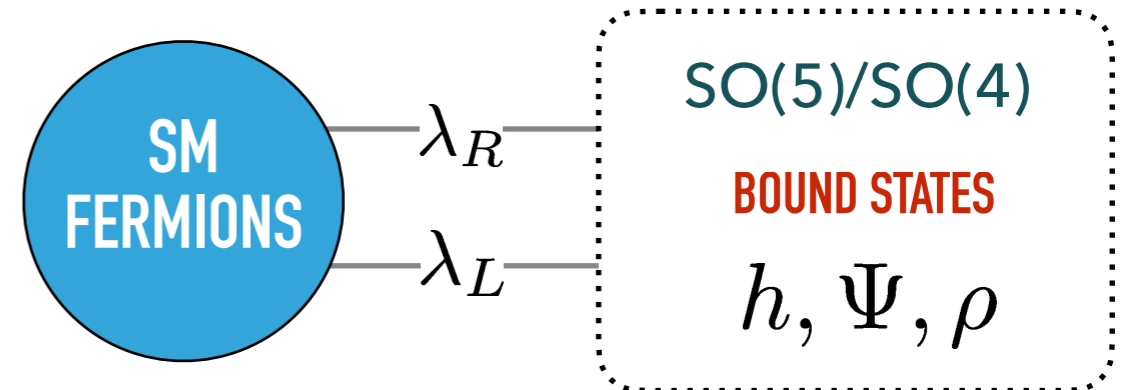
- Soft breaking changes the UV sensitivity: max divergence is log.



Note: the potential (especially in 5D) is anyways finite

# TUNING

## STANDARD MCHM5



- The **LO** potential contains only one trigonometric function: **trivial extrema** (no ewsb, or *technicolor*):

$$V_{\text{LO}} \simeq \frac{3}{16\pi^2} (g_* f)^2 f^2 \lambda_{L,R}^2 \text{Tr}(\Sigma \Gamma_{L,R}) \propto \sin^2(h/f) \quad \Sigma = U^2 V$$

- Extra (double) tuning in order to **balance LO** and **NLO** potential:

$$|V_{\text{NLO}}| \simeq \frac{\lambda_{L,R}^2}{g_*^2} \cdot |V_{\text{LO}}| \quad \longrightarrow \quad \Delta_5 \simeq \frac{f^2}{v^2} \left(\frac{g_*}{\lambda}\right)^2 \sim 90 \left(\frac{m_T}{1 \text{ TeV}}\right)^2$$

$$m_h \sim \frac{m_T}{f} m_t$$

$$\text{MCHM5: } V_{\text{LO}} \simeq \frac{3}{16\pi^2} (g_* f)^2 f^2 \lambda_{L,R}^2 \text{Tr}(\Sigma \Gamma_{L,R}) \propto \sin^2(h/f)$$

# TUNING

$$V^\dagger T^a V = T^a, \quad V^\dagger T^{\hat{a}} V = -T^{\hat{a}}$$

**MAXIMAL SYMMETRY** is a symmetry of the strong sector that can emerge under certain assumptions.

Csaki et al.'17,'18

- Imposing maximal symmetry further constrains the structure of the LO potential, in particular **forbidding linear terms** in  $\Sigma$ :

$$V_{\text{LO}} \simeq \frac{3}{16\pi^2} f^4 \lambda_L^2 \lambda_R^2 \text{Tr}(\Sigma \Gamma_L \Sigma \Gamma_R) \propto \sin^2(h/f) \cos^2(h/f)$$

- There is **unbroken Higgs parity** as long as fermions are concerned:

$$\sin^2(h/f) \leftrightarrow -\cos^2(h/f) \Rightarrow \xi \equiv \frac{v^2}{f^2} = 0.5$$

- Gauge contribution can however be important as well, and helps misalign the vacuum in the right way:

$$\Delta_{\text{max sym}} \simeq \frac{f^2}{v^2} = 9 \left( \frac{m_T}{1 \text{ TeV}} \right)^2 \quad \text{DOUBLE TUNING IS REMOVED!}$$

# SOFT BREAKING AND MAXIMAL SYMMETRY

- The idea is to enhance the symmetry both on the elementary and composite side to obtain a fully natural spectrum of resonances that is compatible with LHC.

## FIRST ATTEMPT

Take simplest embedding  $(s,v,w) + SO(5)'$  on the composite sector:

$$V_{\text{LO}} \simeq \frac{3}{16\pi^2} f^2 \lambda_L \lambda_R m_w M \text{Tr}(\Sigma \Gamma_w) \propto \sin^2(h/f)$$

$$\mathcal{L}_{\text{elem}} = \dots + m_w \bar{\psi}_L \Gamma_w \psi_R$$

$$\psi_L = \begin{pmatrix} q_L \\ w_L \\ s_L \end{pmatrix} \quad \psi_R = \begin{pmatrix} v_R \\ w_R \\ t_R \end{pmatrix}$$

Linear term allowed by all the symmetries: **trigonometric parity** is **badly broken** and double tuning is reintroduced.

# SOFT BREAKING AND MAXIMAL SYMMETRY

## SUCCESSFUL COMBINATION SB, Csaki, Goertz 2020

- It requires a simple modification of the minimal embedding: "splitting" w

$$\psi_L = \begin{pmatrix} q_L \\ w_L \\ s_L \end{pmatrix} \quad \psi_R = \begin{pmatrix} v_R \\ w'_R \\ t_R \end{pmatrix}$$

- In general, the multiplets in which the different SM chiralities are embedded should not couple directly (trivially true without soft breaking):

$$\mathcal{L}_{\text{el}} = m_w \bar{w}_R \Delta_w \psi_L + m'_w \bar{w}'_L \Delta_w \psi_R + m_v \bar{v}_L \Delta_v \psi_R + m_s \bar{s}_R \Delta_s \psi_L + \text{h.c.}$$

- The chiralities that enter neither of the SO(5) multiplets can be grouped:

$$\mathbb{Z}_2 \quad \mathcal{L}_{\text{el}} = \bar{\eta}_R M_R \psi_L + \bar{\xi}_L M_L \psi_R + \text{h.c.} \quad \eta_R = (w_R, s_R) \quad \xi_L = (w'_L, v_L)$$

# SOFT BREAKING AND MAXIMAL SYMMETRY

## SUCCESSFUL COMBINATION

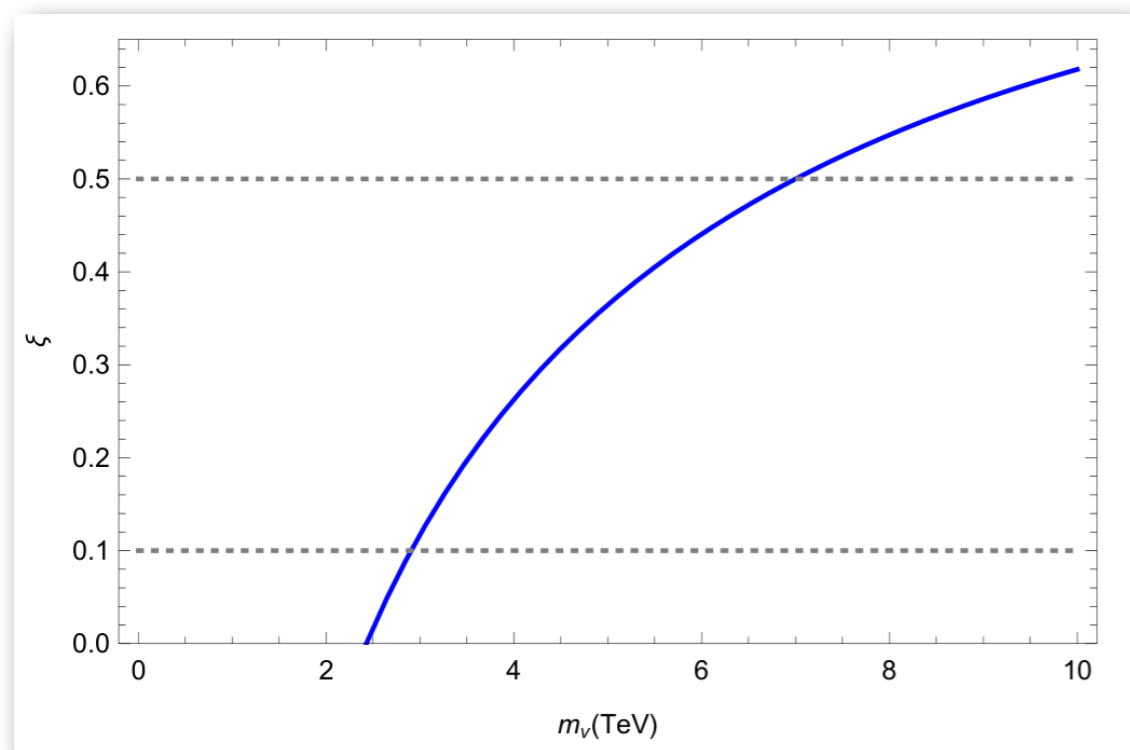
$$\Gamma_L = M_L^\dagger M_L$$

$$\Gamma_R = M_R^\dagger M_R$$

- We can again estimate the LO order potential by means of spurion analysis:

$$V_{\text{LO}} \simeq \frac{3}{16\pi^2} \lambda_L^2 \lambda_R^2 f^4 \sum_{i,j=1}^{\infty} \text{Tr}(\Sigma \Gamma_L^i \Sigma \Gamma_R^j) \propto c_2 \sin^2(h/f) + c_4 \sin^4(h/f)$$

the sum just reconstructs massive VL propagators

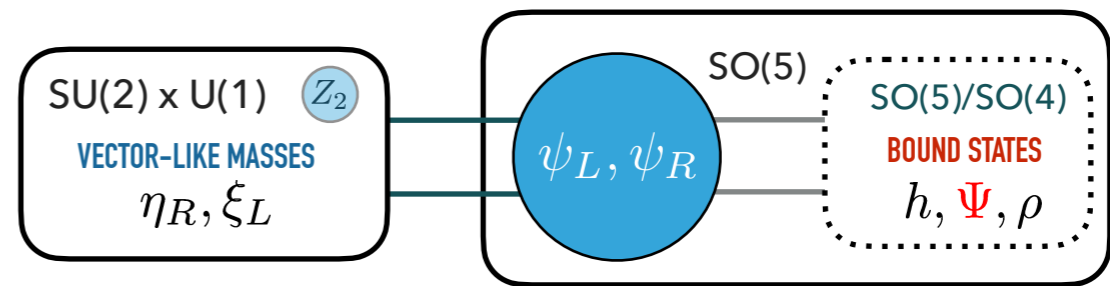


- ▶ **Double tuning** is solved.
- ▶ Trigonometric parity broken in a **controlled way**:
 
$$\xi = 0.5 \Leftrightarrow (m_v^2 - m_w'^2) m_w^2 = 0$$
- ▶ The vacuum **can be misaligned** already within the fermion sector.

# SMALL SUMMARY II

Soft breaking and maximal symmetry turn out to be a perfect match pushing the tuning back to the 10% of the pre-LHC.

## ESSENTIALS OF THE SETUP



1. Soft breaking:  $SO(5)$ -symmetric partial compositeness requires the elementary fermions to appear as complete  $SO(5)$  multiplets.
2. Maximal symmetry: the composite resonances come as complete  $SO(5)$  multiplets as well and the symmetry is enlarged to  $SO(5)'$ .
3. Discrete parity in the elementary sector.
4. The vector-like masses of BSM fermions are at the TeV scale to avoid decoupling ("coincidence problem"?).