A Parton-Level Simulation of DPS

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January 25th, 2019



1 Introduction: double vs. single parton scattering

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¹This work has received funding from the European Union's Horizon 2020 research and innovation programme as part of the Marie Skłodowska-Curie Innovative Training Network MCnetITN3 (grant agreement no. 722104).

Double vs. single parton scattering

• Single parton scattering (SPS):

$$\sigma_A^{\text{SPS}} = \sum_{i,j} \int \mathrm{d}x_1 \mathrm{d}x_2 \,\hat{\sigma}_{ij\to A}(\hat{s} = x_1 x_2 s, Q^2) \, f_i(x_1, Q^2) \, f_j(x_2, Q^2).$$

• $f_i(x, Q^2)$: Parton Distribution Functions (PDFs).



Double vs. single parton scattering

• Double parton scattering (DPS) [1710.04408]:

$$\sigma_{(A,B)}^{\text{DPS}} = \sum_{i,j,k,l} \int \mathrm{d}x_1 \,\mathrm{d}x_2 \,\mathrm{d}x_3 \,\mathrm{d}x_4 \,\hat{\sigma}_{ij\to A}(x_1 x_2 s, Q_A^2) \,\hat{\sigma}_{kl\to B}(x_3 x_4 s, Q_B^2)$$
$$\int \mathrm{d}^2 \boldsymbol{y} \, F_{ik}(x_1, x_3, \boldsymbol{y}, Q_A^2, Q_B^2) F_{jl}(x_2, x_4, \boldsymbol{y}, Q_A^2, Q_B^2).$$

• $F_{ij}(x_1, x_2, y, Q_A^2, Q_B^2)$: dPDFs.



Why do we consider double parton scattering?

$$\sigma^{\mathrm{DPS}}_{(A,B)}/\sigma^{\mathrm{SPS}}_{A+B} \sim \Lambda^2/Q^2$$
. But:

• For bosons with small transverse momenta [1111.0910]:

$$rac{\mathrm{d}\sigma^{\mathrm{DPS}}_{(A,B)}}{\mathrm{d}^2 oldsymbol{q}_A \mathrm{d}^2 oldsymbol{q}_B} \sim rac{\mathrm{d}\sigma^{\mathrm{SPS}}_{A+B}}{\mathrm{d}^2 oldsymbol{q}_A \mathrm{d}^2 oldsymbol{q}_B}$$

• SPS might be suppressed by a high multiplicity of couplings:



Parton shower

• Define the probability $d\mathcal{P}_b = df_b(x, Q^2)/f_b(x, Q^2)$.



• Evolve downwards in Q^2 according to DGLAP equations:

$$df_b(x,Q^2) = \frac{dQ^2}{Q^2} \sum_a P_{a \to bc} \left(\frac{x}{x'}\right) \otimes f_a(x',Q^2)$$

dDGLAP equations

• Homogeneous equal-scale dDGLAP equations [1702.06486]:

$$dF_{ij}(x_1, x_2, \boldsymbol{y}, Q^2) = \frac{dQ^2}{Q^2} \left(\sum_{i'} P_{i' \to i} \left(\frac{x_1}{x_1'} \right) \otimes F_{i'j}(x_1', x_2, \boldsymbol{y}, Q^2) \right)$$
$$+ \sum_{j'} P_{j' \to j} \left(\frac{x_2}{x_2'} \right) \otimes F_{ij'}(x_1, x_2', \boldsymbol{y}, Q^2) \right)$$

• Inhomogeneous term included inside $F_{ij}(x_1, x_2, \boldsymbol{y}, Q^2)$ (1/ \boldsymbol{y}^2 behaviour).



• Algorithm:

- Select two separate hard processes with the DPS cross section. A value for y is also selected.
- 2 Define the branching probability as $d\mathcal{P}_{ij} = dF_{ij}(x_1, x_2, \boldsymbol{y}, Q^2) / F_{ij}(x_1, x_2, \boldsymbol{y}, Q^2)$ [0408302].
- Shower simultaneously the two hard processes with an angular-ordered shower.
- The set of y-dependent dPDFs has been developed in [1702.06486].

• The possibility to have mergings is included in the simulation:



• But far from perfect (kinematics very difficult): still some problems and requires further work!

• DPS: $W^+ \to e^+ \nu_e \oplus W^+ \to \mu^+ \nu_\mu$ (no SPS channel).



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• Double parton scattering must be included to improve the precision of event generators. Combine dPDFs and parton showers.

- Use the **y**-dependent dPDFs $F_{ij}(x_1, x_2, y, Q^2)$.
- Extension to two different scales Q_A^2 and Q_B^2 ?

• MPI models might benefit from a parton shower based on dPDFs.

Thanks for your attention!