

Neutrino Physics and Astrophysics

Neutrino mixing

- EW CC:
$$j_\alpha^W = 2 \sum_{l=e,\mu,\tau} \bar{\nu}_{lL} \gamma_\alpha l_L + 2 \sum_{q=u,c,t} \sum_{q'=d',s',b'} \bar{q}_L \gamma_\alpha q'_L$$

where ν_{lL} , l_L , q_L are left-handed neutrino, lepton

and quark fields and $q'_L = \sum_{q=d,s,b} U_{q'q} q_L$

- In analogy to quark mixing in the lepton sector: $\nu_{lL} = \sum_k U_{lk} \nu_{kL}$ where U is unitary, ν_k is the ν field with mass m_k .

- Since $Q_\nu = 0$ neutrinos can be Dirac or Majorana particles...

Dirac mass term

$$L^D = - \sum_{l'} \bar{\nu}_{l'R} M_{l'l} \nu_{lL} + h.c. = - \bar{\nu}'_R M \nu'_L + h.c.$$

$$\nu'_L = \begin{pmatrix} \nu_{eL} \\ \nu_{\mu L} \\ \nu_{\tau L} \end{pmatrix} \quad \nu'_R = \begin{pmatrix} \nu_{eR} \\ \nu_{\mu R} \\ \nu_{\tau R} \end{pmatrix}$$

- Diagonalisation $M = V m U^+ \implies \mathcal{L}$ in terms of mass eigenstates :

$$L^D = - \bar{\nu}_R m \nu_L - \bar{\nu}_L m \nu_R = - \bar{\nu} m \nu = - \sum_{k=1}^3 m_k \bar{\nu}_k \nu_k$$

$$\begin{aligned} \nu_R &= V^+ \nu'_R \\ \nu_L &= U^+ \nu'_L \end{aligned} \quad \nu = \nu_R + \nu_L = \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Majorana mass term

- Using ν_{lL} and $(\nu_{lL})^c = C\bar{\nu}_{lL}^T$ (Charge conjugation matrix)

- $$L^M = -\frac{1}{2} \sum_{l',l} (\bar{\nu}_{l'L})^c M_{l'l} \nu_{lL} + h.c. = -\frac{1}{2} (\bar{\nu}'_L)^c M \nu'_L + h.c.$$

- M is symmetric $M = (U^+)^T m U^+$

$$L^M = \frac{1}{2} (\nu'_L)^T C^{-1} (U^+)^T m U^+ \nu'_L + h.c. = -\bar{\chi} m \chi = \frac{1}{2} \sum_{k=1}^3 m_k \bar{\chi}_k \chi_k$$

$$\chi = U^+ \nu'_L + (U^+ \nu'_L)^c = \begin{pmatrix} \chi_1 \\ \chi_2 \\ \chi_3 \end{pmatrix}$$

Field with majorana mass m_k

Violates L

General term

- Dirac +Majorana mass terms with L&R-handed fields

$$L^{D-M} = -\frac{1}{2} \left[(\bar{\nu}'_L)^c M_L \nu'_L + (\bar{\nu}'_R M_R (\nu'_R)^c + \bar{\nu}'_R M_D \nu'_L + (\bar{\nu}'_L)^c M_D^T (\nu'_R)^c \right] + h.c.$$

$$L^{D-M} = -\frac{1}{2} (\bar{n}_L)^c M n_L + h.c.$$

$$n_L = \begin{pmatrix} \bar{\nu}'_L \\ (\nu'_R)^c \end{pmatrix}$$

$$M = \begin{pmatrix} M_L & M_D \\ M_D^T & M_R \end{pmatrix}$$

- Diagonalising M we get :

$$L^{D-M} = -\frac{1}{2} \bar{\chi} m \chi = -\frac{1}{2} \sum_{k=1}^6 m_k \bar{\chi}_k \chi_k$$

$$\chi = U^+ n_L + (U^+ n_L)^c = \begin{pmatrix} \chi_1 \\ \vdots \\ \chi_6 \end{pmatrix}$$

↑
Majorana type

More on the general mass term

$$n_L = U \chi_L$$

$$\nu_{lL} = \sum_{k=1}^6 U_{lk} \chi_{kL}$$
$$(\nu_{lR})^c = \sum_{k=1}^6 U_{\bar{l}k} \chi_{kL}$$

1st 3 rows Last 3 rows
 Right handed neutrinos (sterile)

- $\nu_i \longrightarrow \nu_j$ flavour transitions are possible
- Active to sterile neutrinos are also possible !

For one family

- $M = O m' O^T$ (no CP violation) $O = \begin{pmatrix} \sin\theta & -\cos\theta \\ \cos\theta & \sin\theta \end{pmatrix}$

$$\nu_L = \sin\theta \chi_{1L} - \cos\theta \chi_{2L}$$

$$(\nu_R)^c = \cos\theta \chi_{1L} + \sin\theta \chi_{2L}$$

$$m_L = \sin^2\theta m'_1 + \cos^2\theta m'_2$$

$$m_R = \cos^2\theta m'_1 + \sin^2\theta m'_2$$

$$2m_D = \sin 2\theta (m'_1 - m'_2)$$

- M eigenvalues :

$$m'_{1,2} = \frac{1}{2} (m_L + m_R \pm \sqrt{(m_L - m_R)^2 + 4m_D^2})$$

$$\sin 2\theta = \frac{2m_D}{\sqrt{(m_L - m_R)^2 + 4m_D^2}}$$

Seesaw Mechanism

• Limiting case $m_L \approx 0$, $m_R \gg m_D$

$$m_1 \approx m_R, m_2 \approx m_D^2 / m_R$$

$$\theta \approx m_D / m_R$$

$$v_L \approx -\chi_{2L} \quad (v_R)^c \approx \chi_{1L}$$

If $m_D \approx m_{l,q}$ then $m_\nu \approx m_q^2 / m_R$ or m_l^2 / m_R

m_R is assumed GUT scale $\sim 10^{14} \text{ GeV}$

The heavy right-handed Majorana mass generates the small active neutrino mass

$$m'_{1,2} = \frac{1}{2}(m_L + m_R \pm \sqrt{(m_L - m_R)^2 + 4m_D^2})$$

$$\sin 2\theta = \frac{2m_D}{\sqrt{(m_L - m_R)^2 + 4m_D^2}}$$

Oscillations in vacuum

$$|v_l\rangle = \sum_k U_{lk}^* |v_k\rangle$$

$$|v_k(t)\rangle = e^{-iE_k t} |v_k(0)\rangle$$

$$|v_l(t)\rangle = \sum_{l'} \sum_k U_{l'k} e^{-iE_k t} U_{lk}^* |v_{l'}\rangle$$

Transition amplitude: $A_{ll'}(t) = \langle v_{l'} | v_l(t) \rangle = \sum_k U_{l'k} U_{lk}^* e^{-iE_k t}$

$$P(v_l \rightarrow v_{l'}) = |A_{ll'}(t)|^2 = \sum_{kj} U_{lk}^* U_{l'k} U_{lj} U_{l'j}^* e^{-i(E_k - E_j)t}$$

relativistic v : $m \ll E : E_k - E_j \approx \Delta m_{kj}^2 / 2E$

$$P(v_l \rightarrow v_{l'}) = |A_{ll'}(t)|^2 = \sum_{kj} U_{lk}^* U_{l'k} U_{lj} U_{l'j}^* e^{-i(\Delta m_{kj}^2 L / 2E)}$$

Oscillations cont'd

- Measuring oscillations will give us information on the mass differences
- Measurement of symmetry conservation:
 - CP violated : $P(\nu_\alpha \longrightarrow \nu_\beta) \neq P(\bar{\nu}_\alpha \longrightarrow \bar{\nu}_\beta)$
 - T violated : $P(\nu_\alpha \longrightarrow \nu_\beta) \neq P(\nu_\beta \longrightarrow \nu_\alpha)$
 - CPT conserved : $P(\nu_\alpha \longrightarrow \nu_\beta) \neq P(\bar{\nu}_\beta \longrightarrow \bar{\nu}_\alpha)$

Mixing in two families

- Then mass and weak states are connected by means of an unitary transformation, the PMNS mixing matrix, which depends of a single parameter, the mixing angle θ

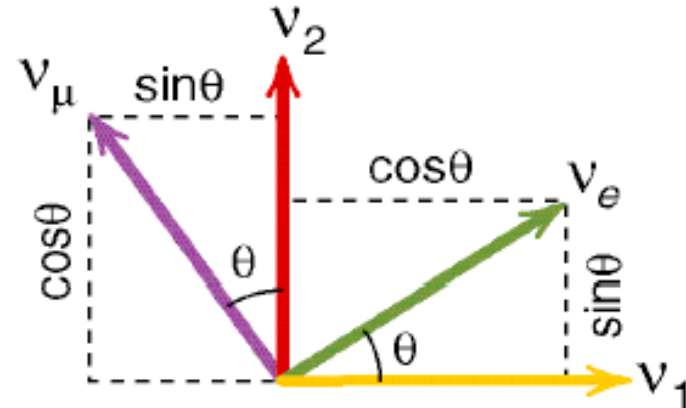
$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

$$\nu_l = \cos\theta \nu_1 - \sin\theta \nu_2$$

$$\nu_l' = \sin\theta \nu_1 + \cos\theta \nu_2$$

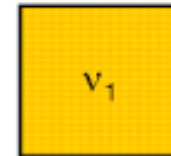
$$P_{\nu_1 \rightarrow \nu_2} = \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E}$$

$$L_\nu = \frac{4\pi E}{\Delta m^2} \approx 2.47 \frac{E(\text{GeV})}{\Delta m^2(\text{eV}^2)} \text{ km}$$

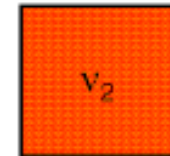


Mass states

First

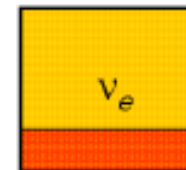


Second

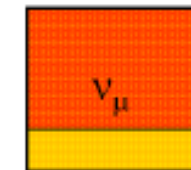


Weak states

First

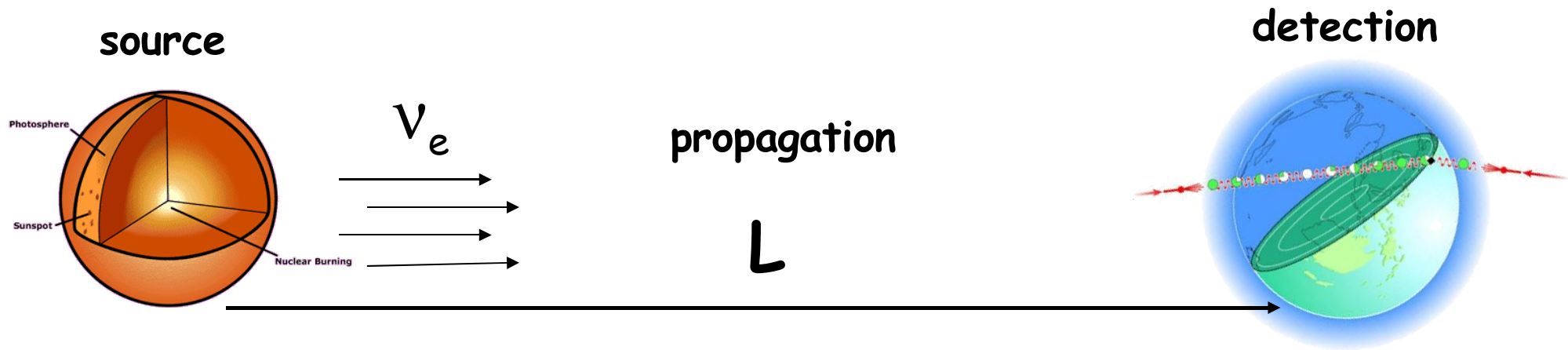


Second



PMNS: Pontecorvo-Maki-Nakagawa-. Sakata

Neutrino oscillations



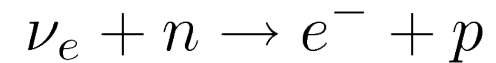
The weak interaction produces neutrinos of a given flavour

The mass eigenstates propagate at different velocities

Detection again via weak interaction

$$|\nu(x_0)\rangle = |\nu_e\rangle = c|\nu_1\rangle + s|\nu_2\rangle$$

$$|\nu(x)\rangle = c|\nu_1\rangle e^{i(Et - \vec{k}_1 \vec{x})} + s|\nu_2\rangle e^{i(Et - \vec{k}_2 \vec{x})}$$

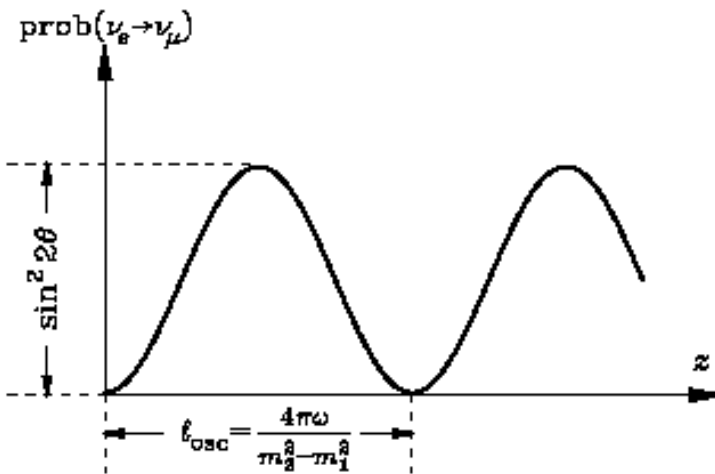


$$P(\nu_e \rightarrow \nu_\mu) = |\langle \nu_\mu | \nu(x) \rangle|^2$$

Oscillation Probability

$$P_{(\nu_e \rightarrow \nu_\mu)}(L) = \sin^2(2\theta) \sin^2 \left(1.27 \frac{\Delta m^2 (eV^2)}{E (GeV)} L (km) \right)$$

$$P_{\nu_e \rightarrow \nu_e}(L) = 1 - P_{\nu_e \rightarrow \nu_\mu}(L)$$



$$L_\nu = \frac{4\pi E}{\Delta m^2} \approx 2.47 \frac{E (GeV)}{\Delta m^2 (eV^2)} km$$

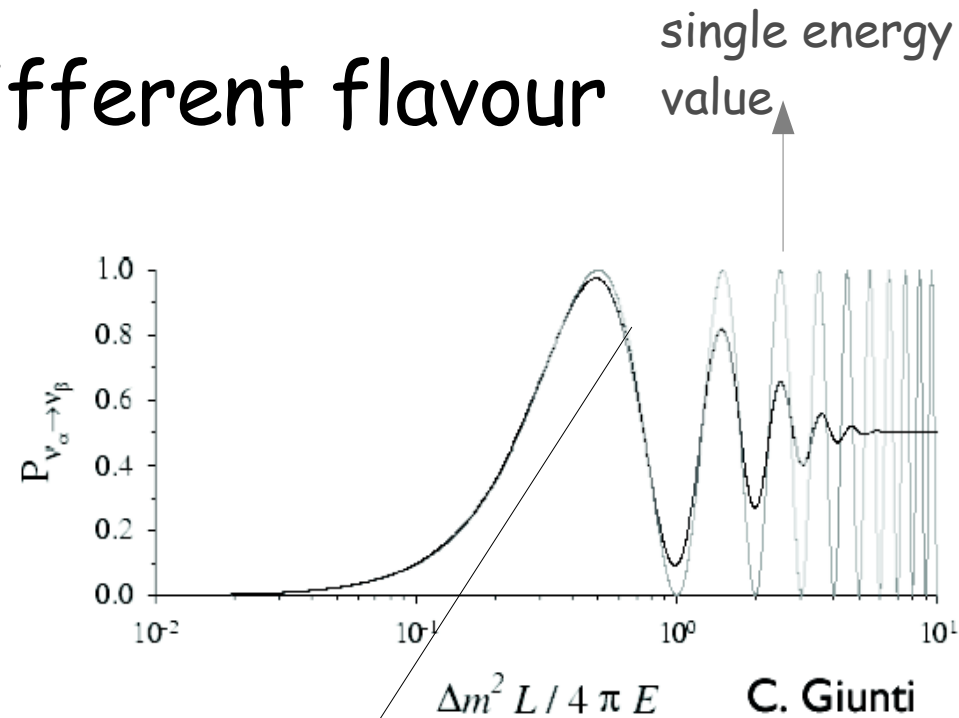
Sensitivity to oscillations

- Disappearance experiments measure survival probability

- Appearance look for a different flavour

- No signal for $\frac{\Delta m^2 L}{2E} \ll 1$

- Averaged out if $\frac{\Delta m^2 L}{2E} \gg 1$



Gaussian E spectrum

Do oscillations solve the solar neutrino problem ?



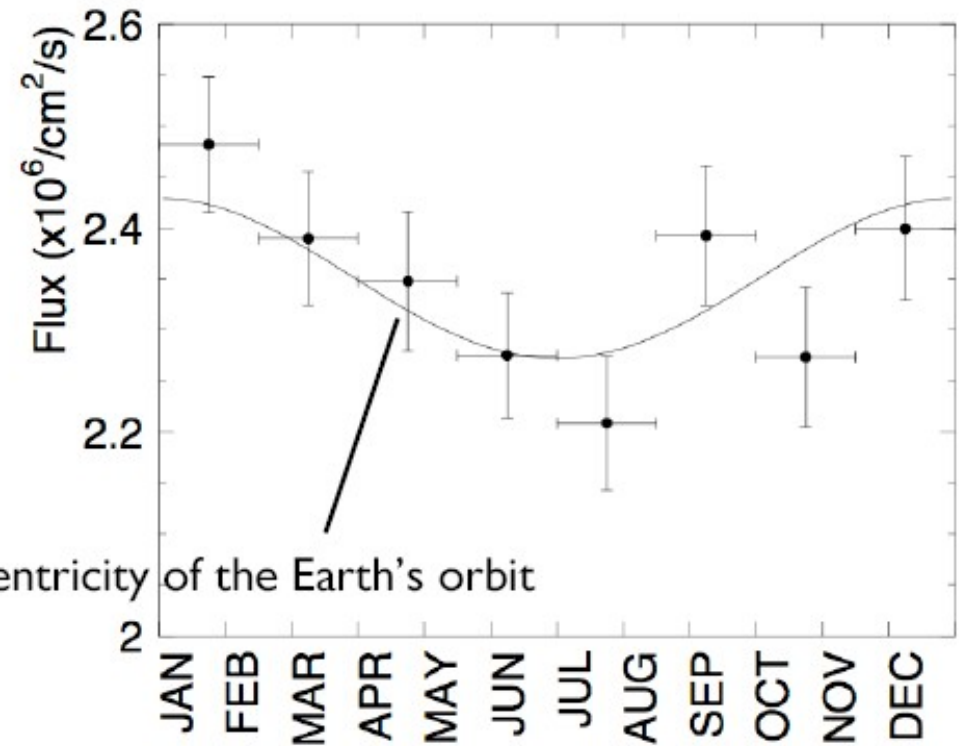
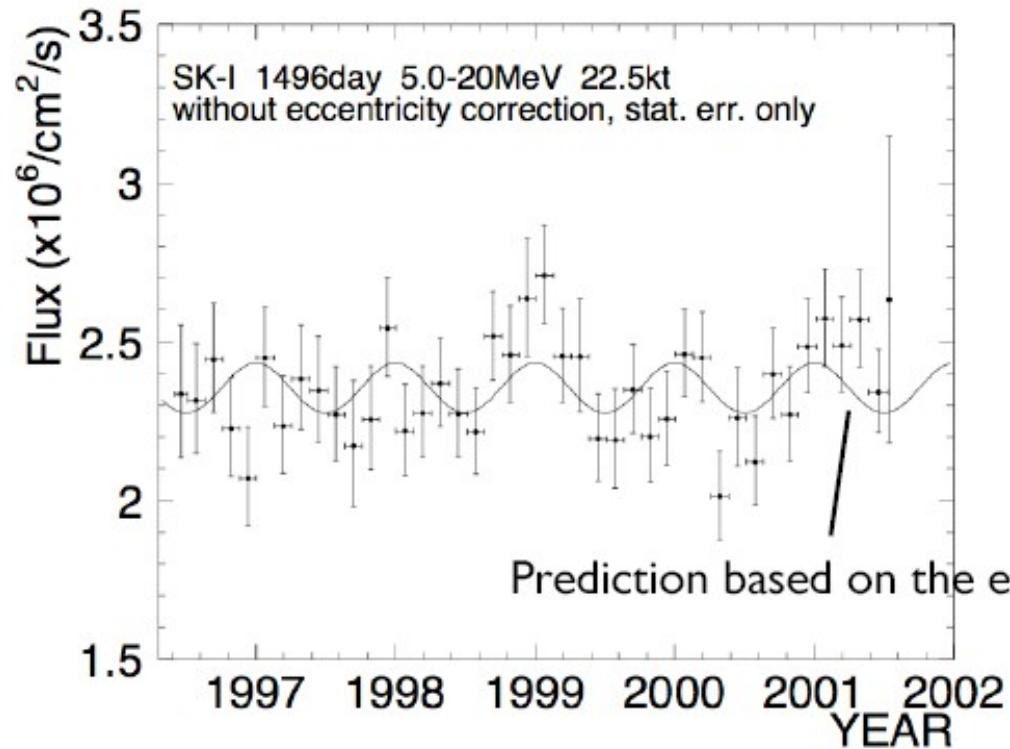
- So far experiments did not measure NC
- If SSM is right NC will reproduce SSM fluxes

- Pontecorvo proposed neutrino oscillations in 1969

$$P_{\nu_e \rightarrow \nu_e}(E, L(t)) = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L(t)}{4E} \right)$$

- With the sun excentricity one should observe seasonal variation n neutrino fluxes

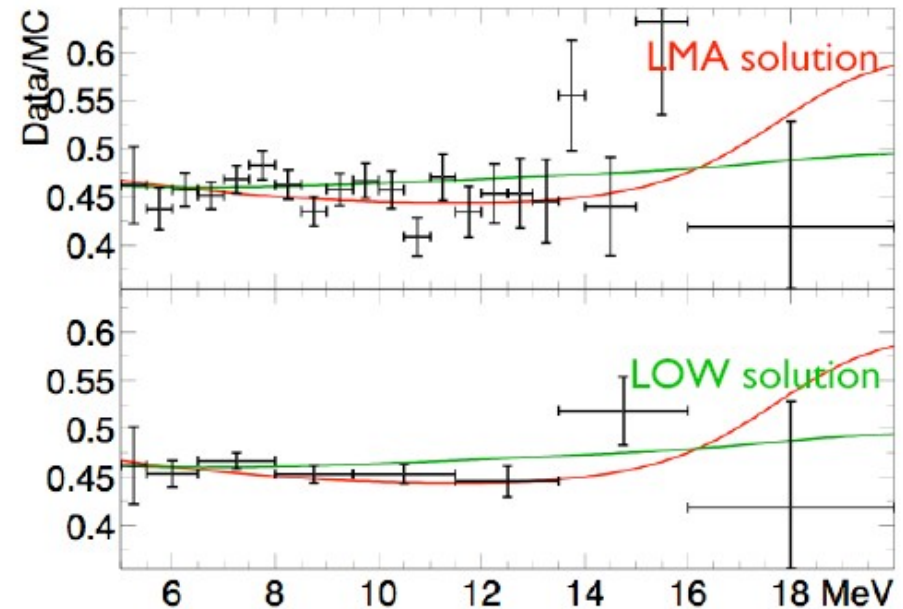
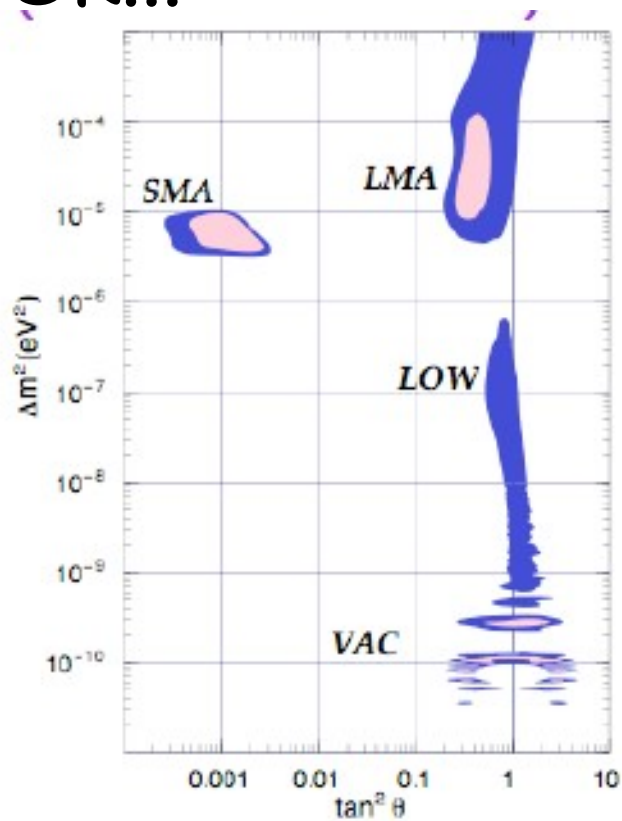
Seasonal variations ?



- The observed variations are compatible with the modulation due to the distance variation
- No extra variation that could be attributed to oscillations

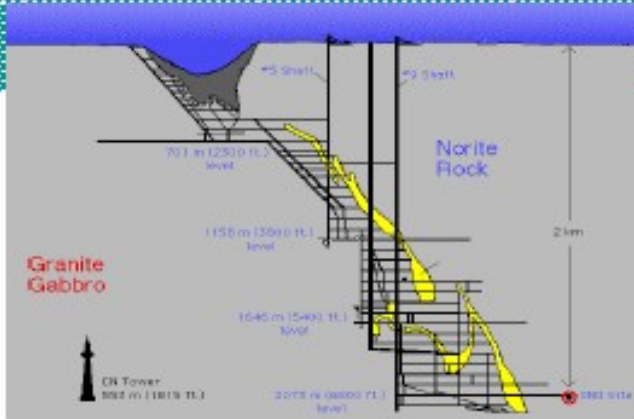
And the E spectrum distortion?

- No distortion of the ${}^8\text{B}$ spectrum is observed in the recoil electron energy in SK...



What about neutral currents ?

Sudbury Neutrino Observatory



1000 tonnes D_2O

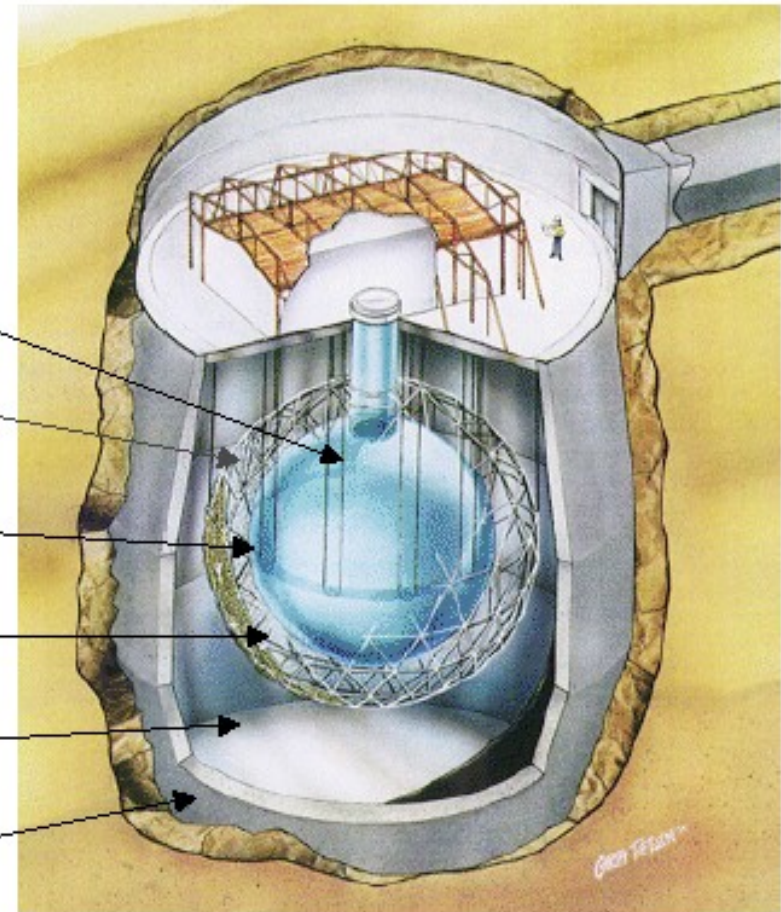
Support Structure for 9500 PMTs, 60% coverage

12 m Diameter Acrylic Vessel

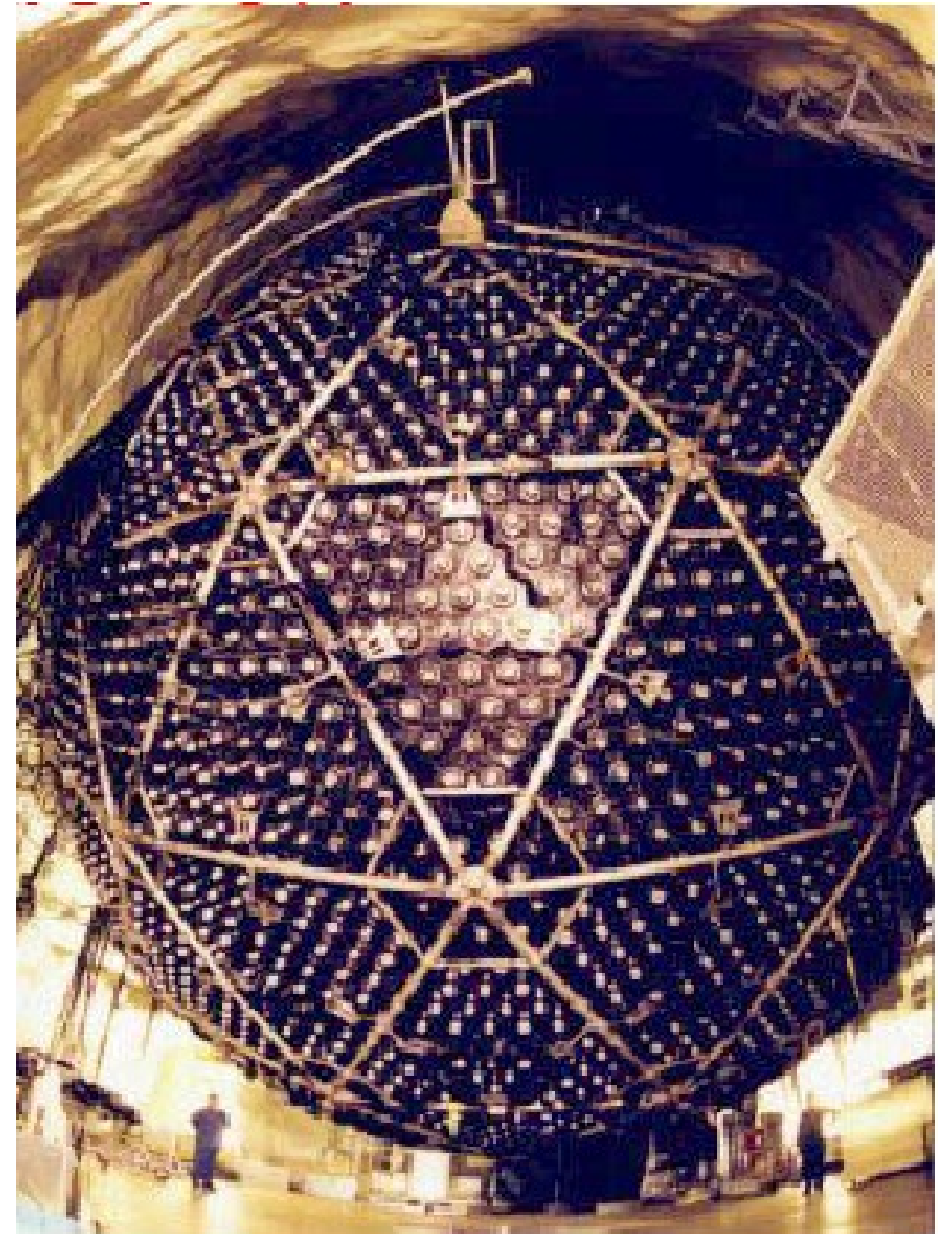
1700 tonnes Inner Shielding H_2O

5300 tonnes Outer Shield H_2O

Urylon Liner and Radon Seal

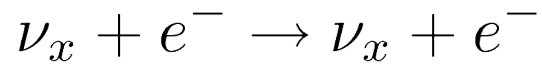


SNO detector



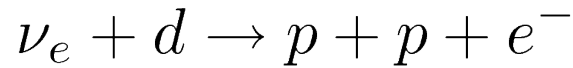
Signals in SNO

ES



Strong directional sensitivity

CC

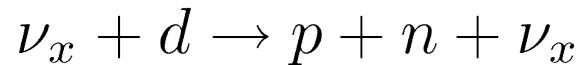


Good measurement of ν_e spectrum

Weak directional sensitivity

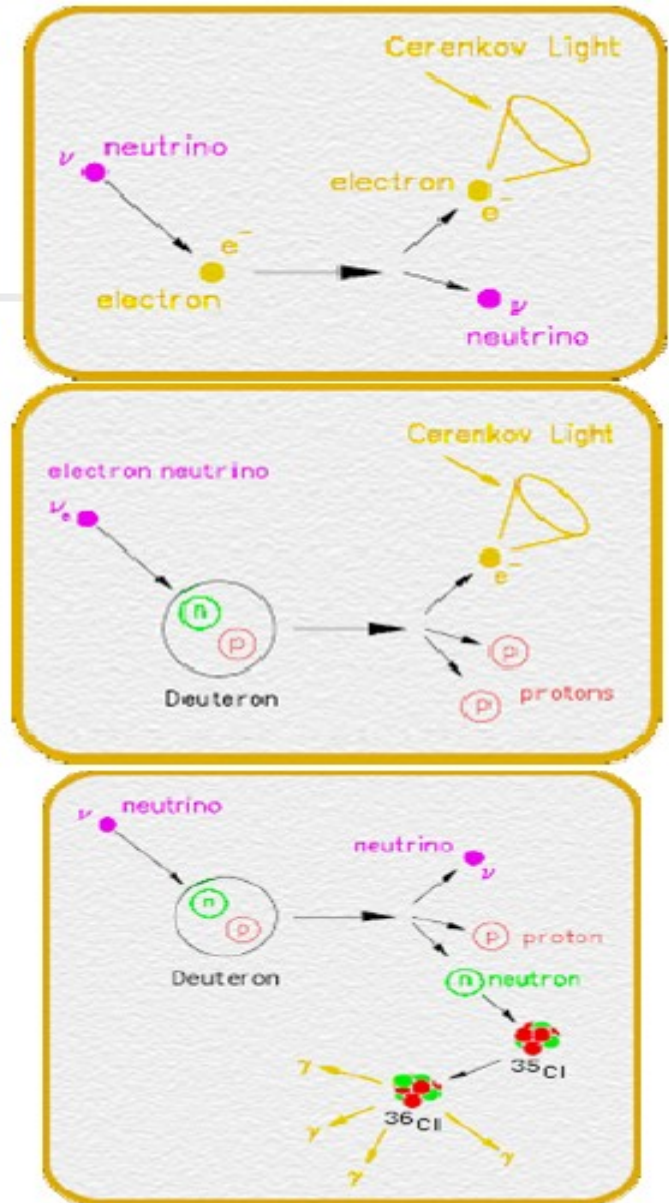
ν_e only

NC

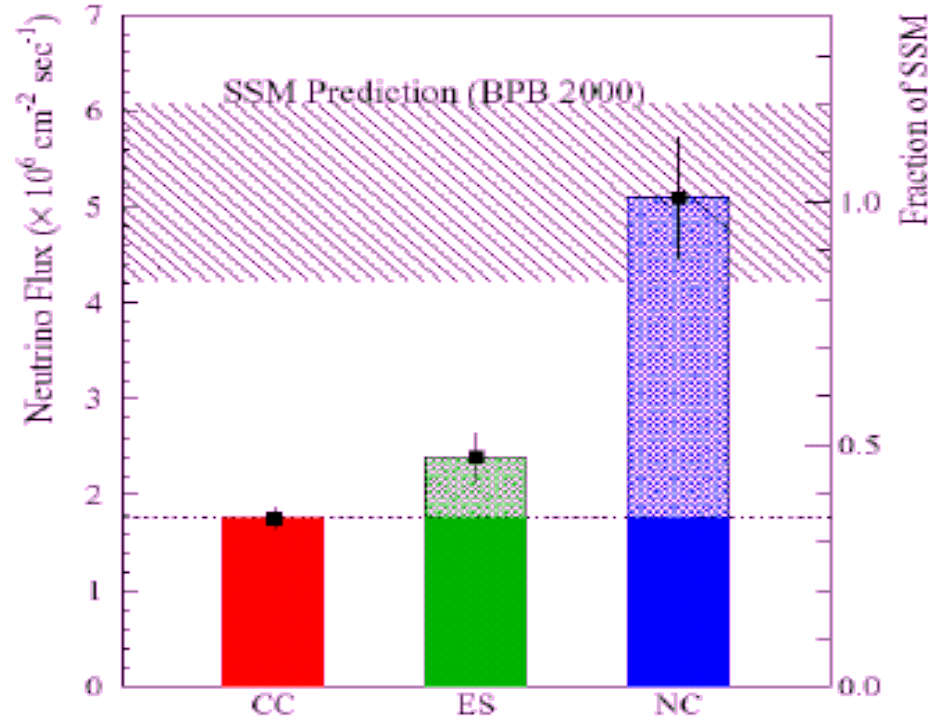
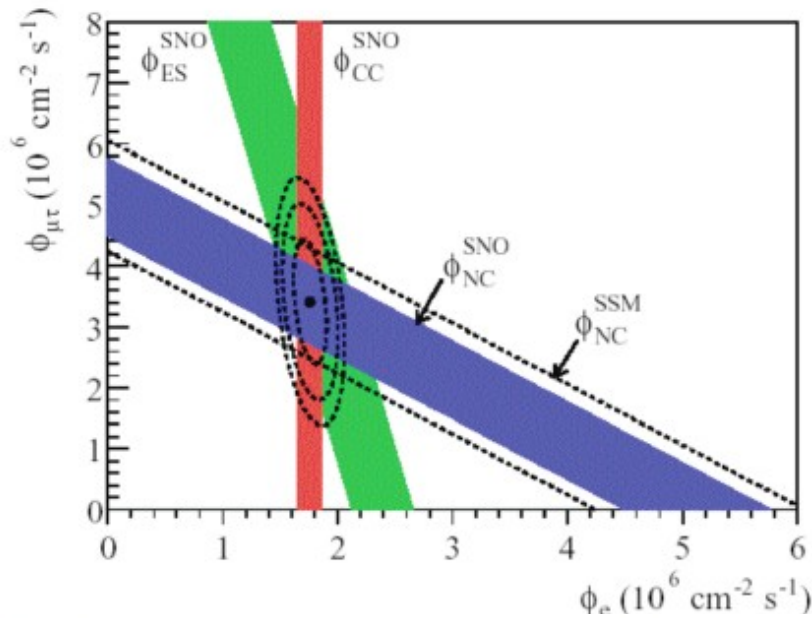
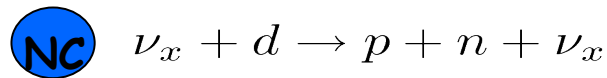
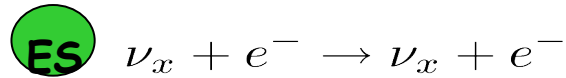
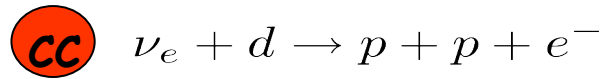


Measure total ${}^8\text{B}$ flux from the sun

Equal cross section for all types



SNO observations



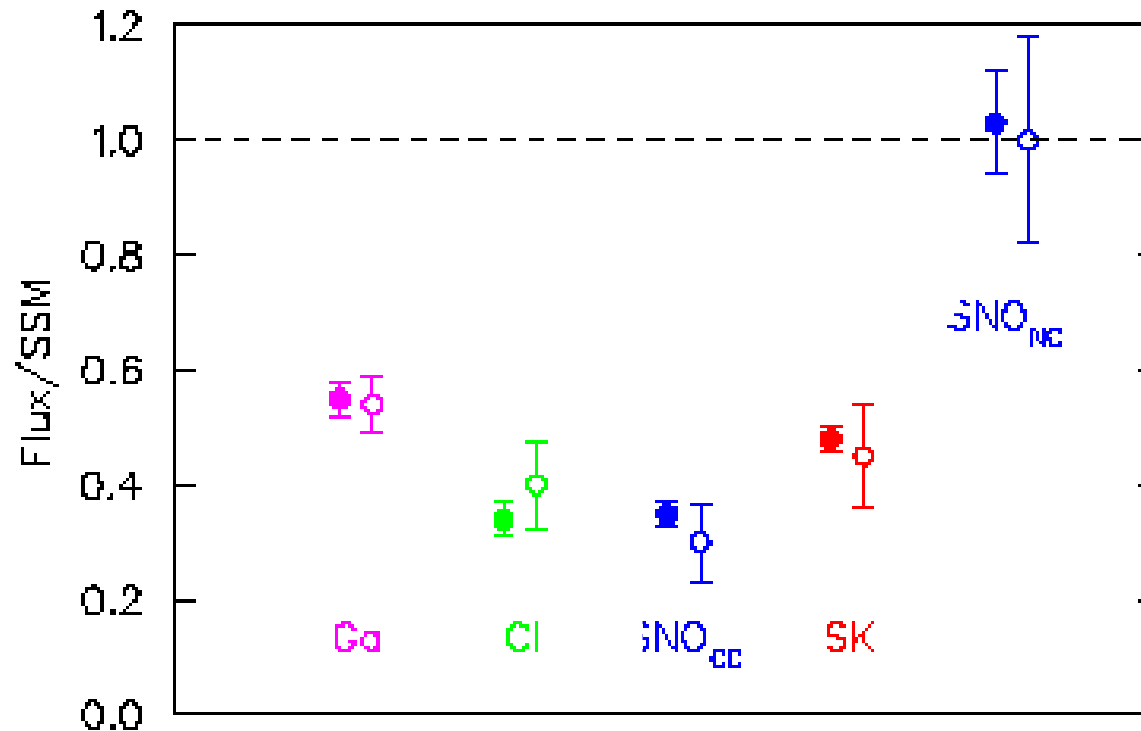
$$\Phi_{CC}^{SNO} = (1.68 \pm 0.06_{-0.09}^{+0.06}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{NC}^{SNO} = (4.94 \pm 0.21_{-0.34}^{+0.38}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{ES}^{SNO} = (2.35 \pm 0.22 \pm 0.15) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

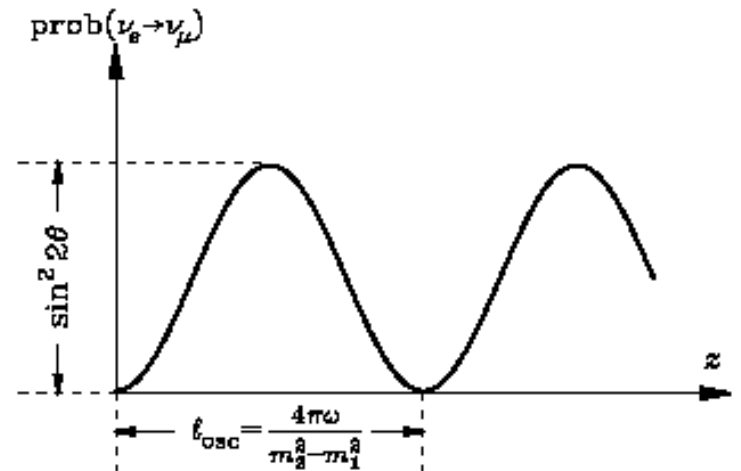
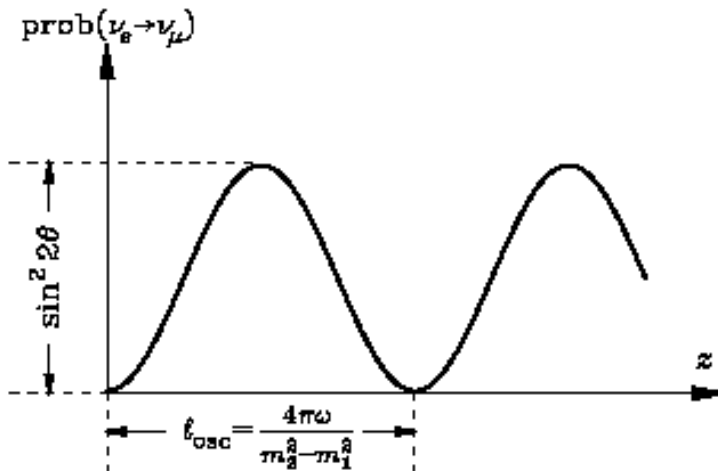
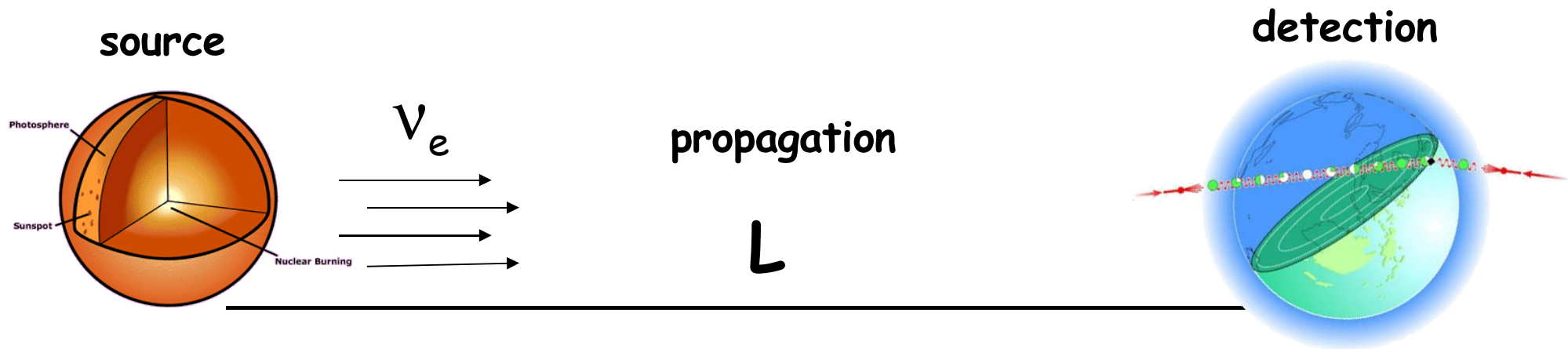
$$\frac{\Phi_{CC}^{SNO}}{\Phi_{NC}^{SNO}} = 0.340 \pm 0.023_{-0.031}^{+0.029}$$

The solar neutrino problem



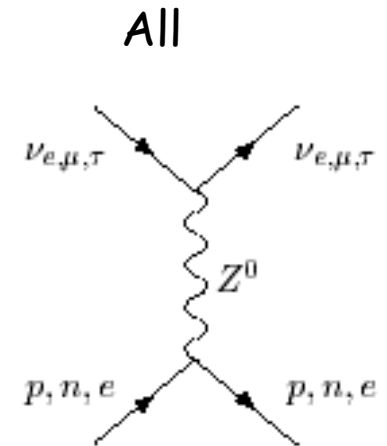
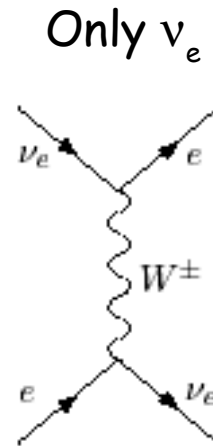
So the sun is shining the expected number of neutrinos but many of them are ν_{μ} and/or ν_{τ} ! Not only Davis, but also Bahcall was right!

Fine-tuning oscillations ?



Neutrino oscillations in Matter

ν_e, ν_μ, ν_τ interact with e, p and n of matter via NC interactions (Z). Only ν_e interact via (CC) with the electrons of the medium



- Neutrinos are subject to a potential linked due to their interaction with the medium

$$V_{CC} = \sqrt{2}G_F N_e \quad V_{NC} = -\frac{1}{2}\sqrt{2}G_F N_n$$

- $V_e = V_{CC} + V_{NC}$
- $V_\mu = V_\tau = V_{NC}$

Hamiltonian in matter

$$H_m = \begin{pmatrix} E_1 \cos^2 \theta + E_2 \sin^2 \theta + C + \sqrt{2}G_F\rho_e & -(E_2 - E_1) \sin \theta \cos \theta \\ -(E_2 - E_1) \sin \theta \cos \theta & E_2 \cos^2 \theta + E_1 \sin^2 \theta + C \end{pmatrix}$$

$$H_m = (E_1 \cos^2 \theta + E_2 \sin^2 \theta + C) \cdot \mathbf{I} + \begin{pmatrix} \sqrt{2}G_F\rho_e & -\frac{1}{2}(E_2 - E_1) \sin 2\theta \\ -\frac{1}{2}(E_2 - E_1) \sin 2\theta & (E_2 - E_1) \cos 2\theta \end{pmatrix}$$

To diagonalize H_m one needs θ_m such that

$$\tan 2\theta_m = \frac{-(E_2 - E_1) \sin 2\theta}{\sqrt{2}G_F\rho_e - (E_2 - E_1) \cos 2\theta}$$

$$\sin^2 2\theta_m = \frac{\sin^2 2\theta}{1 - 2 \cdot \frac{2\sqrt{2}\rho_e G_F E}{\Delta m^2} \cos 2\theta + \left(\frac{2\sqrt{2}\rho_e G_F E}{\Delta m^2}\right)^2}$$

$$|\nu_e \rangle = \cos \theta_m |\nu_1 \rangle_m - \sin \theta_m |\nu_2 \rangle_m$$

$$|\nu_\mu \rangle = \sin \theta_m |\nu_1 \rangle_m + \cos \theta_m |\nu_2 \rangle_m$$

Maximal for $\theta_m = \pi/4$

Oscillations in matter

- Oscillation probability change in matter. There can be a resonant enhancement of the oscillation probability. The Mikheyev-Smirnov-Wolfenstein (MSW) effect.

$$\rho_e = \rho_R = \frac{\Delta m^2 \cos 2\theta}{2\sqrt{2}G_F E}$$

Only for $\Delta m^2 > 0$
and neutrinos or
 $\Delta m^2 < 0$ and anti-
neutrinos !!

$P_{\text{osc}}^{\text{matter}}$ can be large (≈ 1) even if mixing angle in vacuum is small.

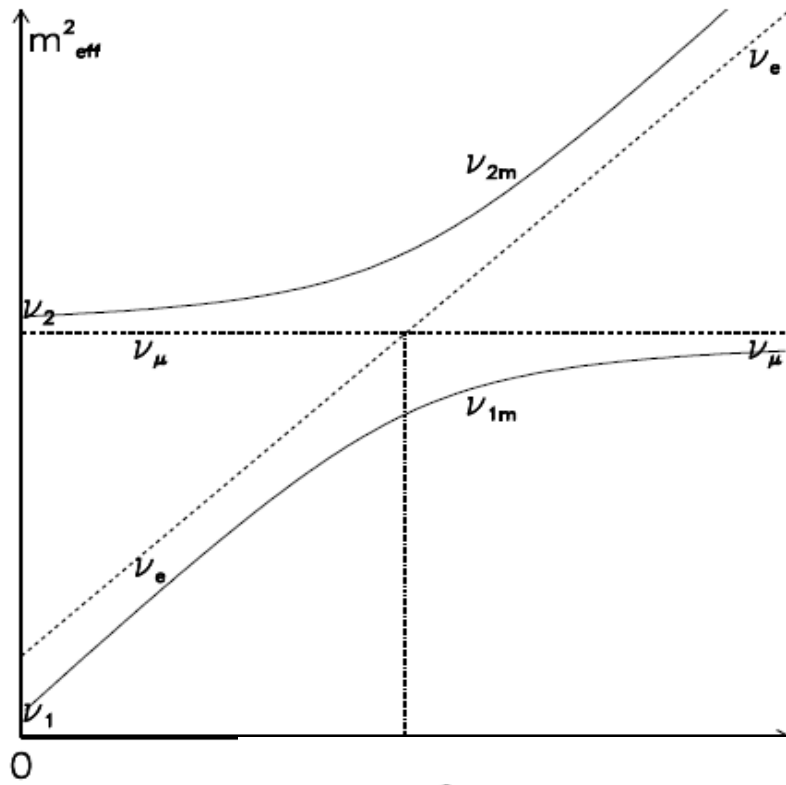
- In practice this implies that (if MSW is at work) ν_e can oscillate to ν_μ, ν_τ BEFORE exiting the sun

$$L_0 = \frac{2\pi}{\sqrt{2}\rho_e G_F} \quad \sin^2 2\theta_m = \frac{\sin^2 2\theta}{1 - 2 \cdot \frac{L_v}{L_0} \cos 2\theta + \left(\frac{L_v}{L_0}\right)^2}$$

Oscillation length in matter:

$$L_m = \frac{L_v}{\sqrt{1 - 2\frac{L_v}{L_0} \cos 2\theta + \left(\frac{L_v}{L_0}\right)^2}}$$

Adiabatic condition

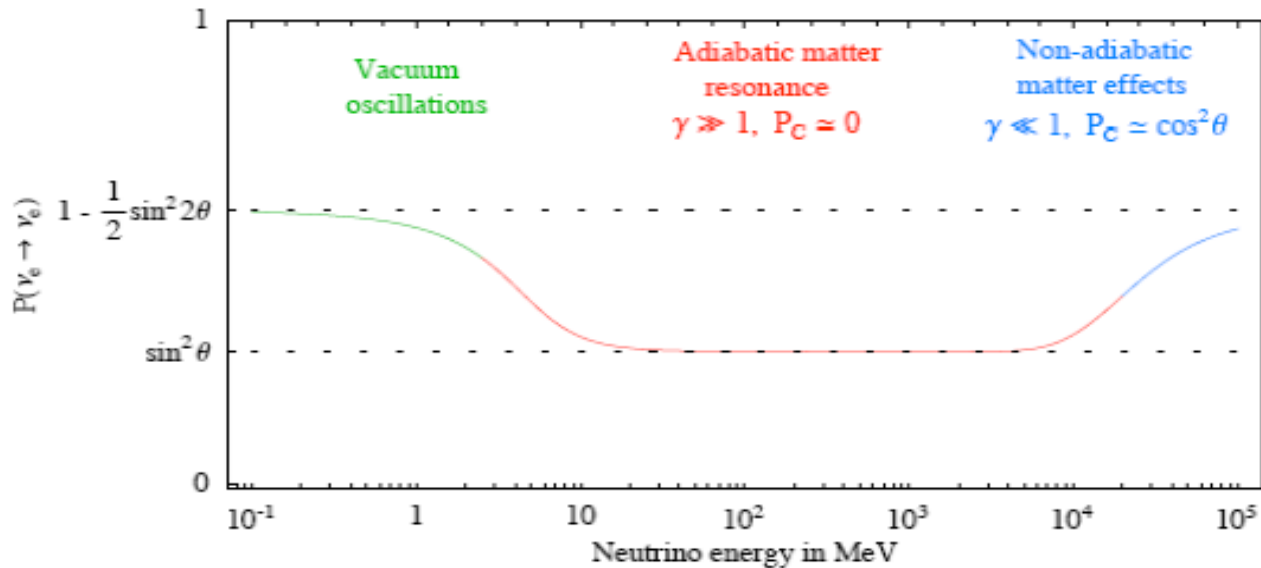


Fulfilled if the density layer corresponding to the resonance is thicker than an oscillation length

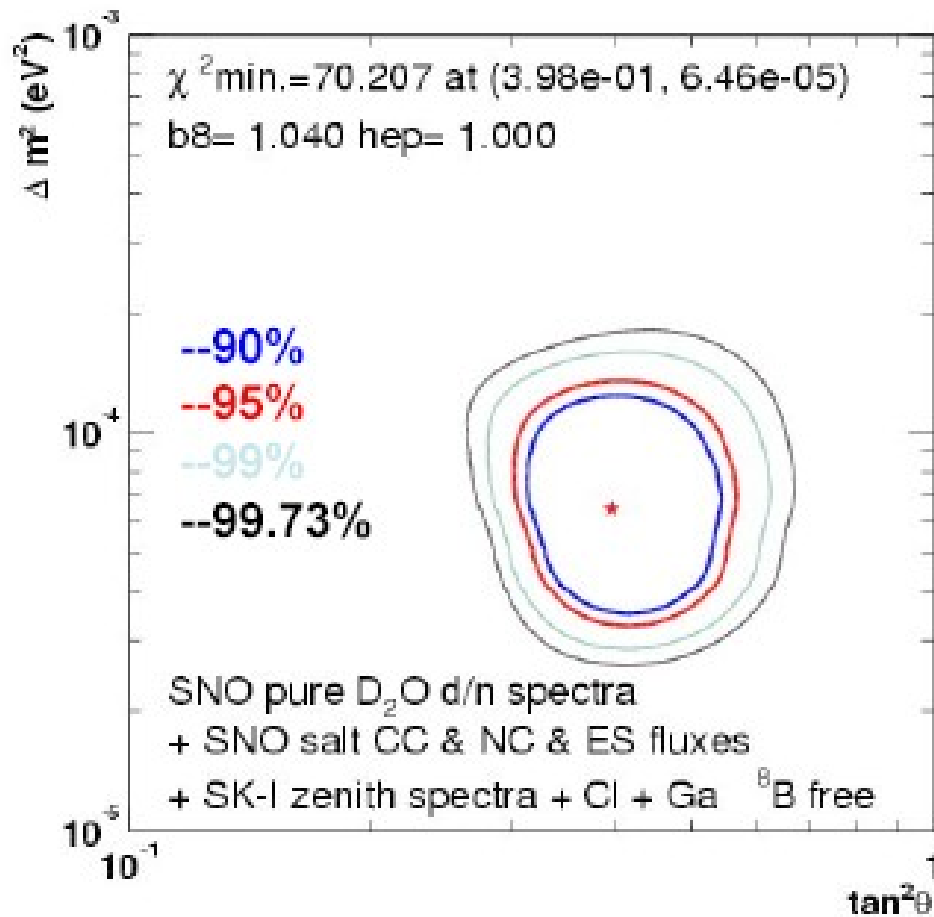
$$\Delta\rho_R = \rho_R \tan 2\theta$$

$$\left(\frac{d\rho}{dr}\right)^{-1} \Delta\rho_R > L_m$$

$$\frac{d\rho}{dr} < \frac{(\Delta m^2)^2 \sin^2 2\theta}{8\pi\sqrt{2}G_F E^2}$$



Solar oscillations



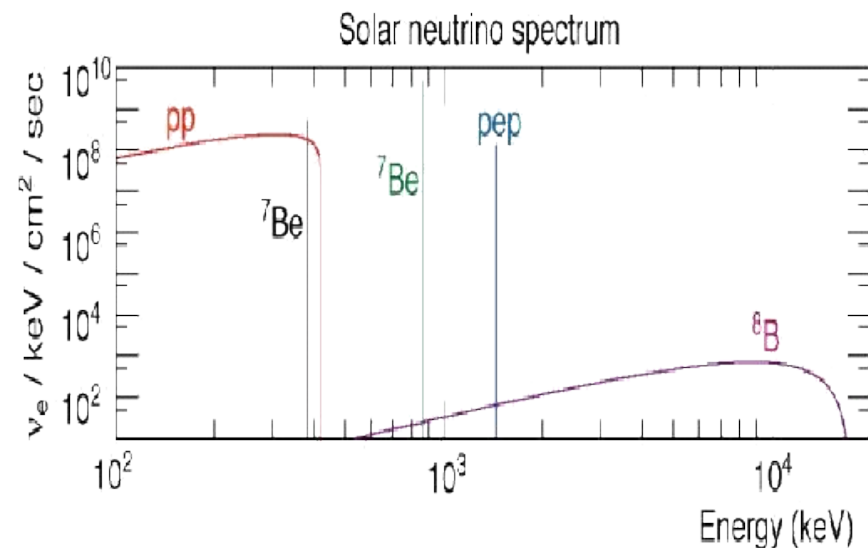
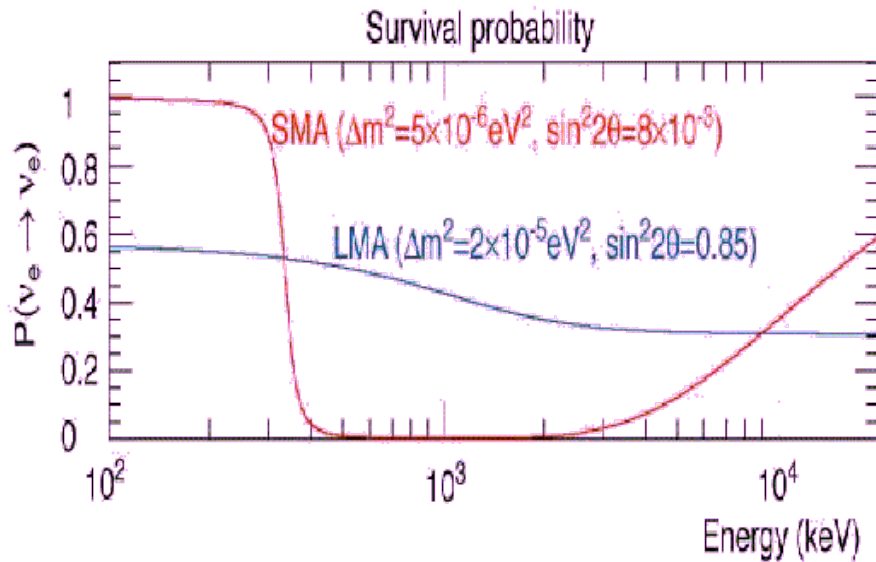
Neutrinos produced at the sun (ν_e) oscillate to other neutrinos via matter-enhanced MSW.

$$\Delta m^2 = 8 \times 10^{-5} \text{ eV}^2$$

$$\theta \approx 30^\circ$$

Solar neutrino oscillations

Matter effect on ν_e from Sun to Earth

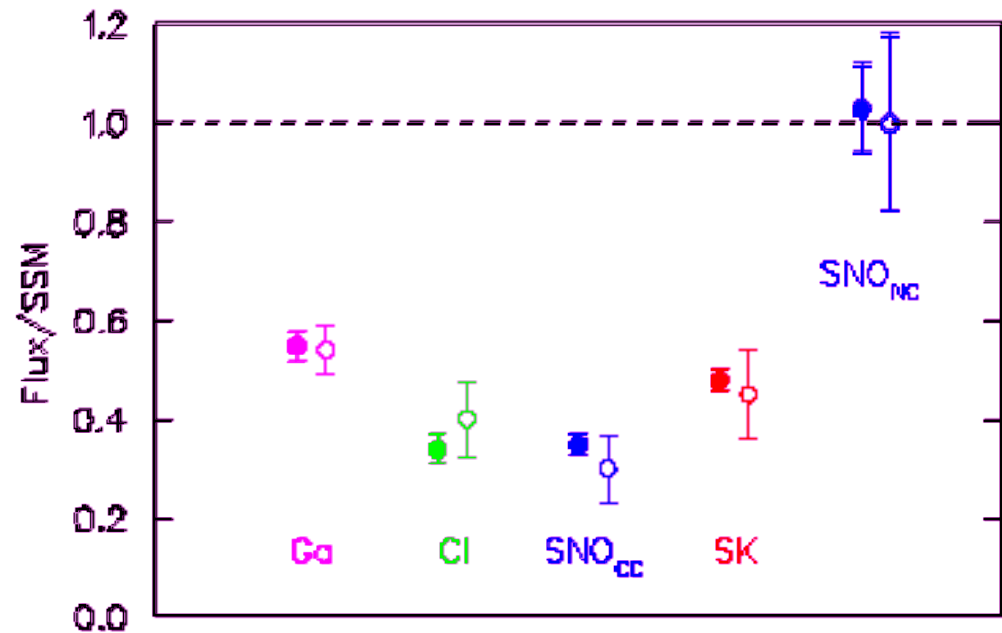


The LMA solar solution

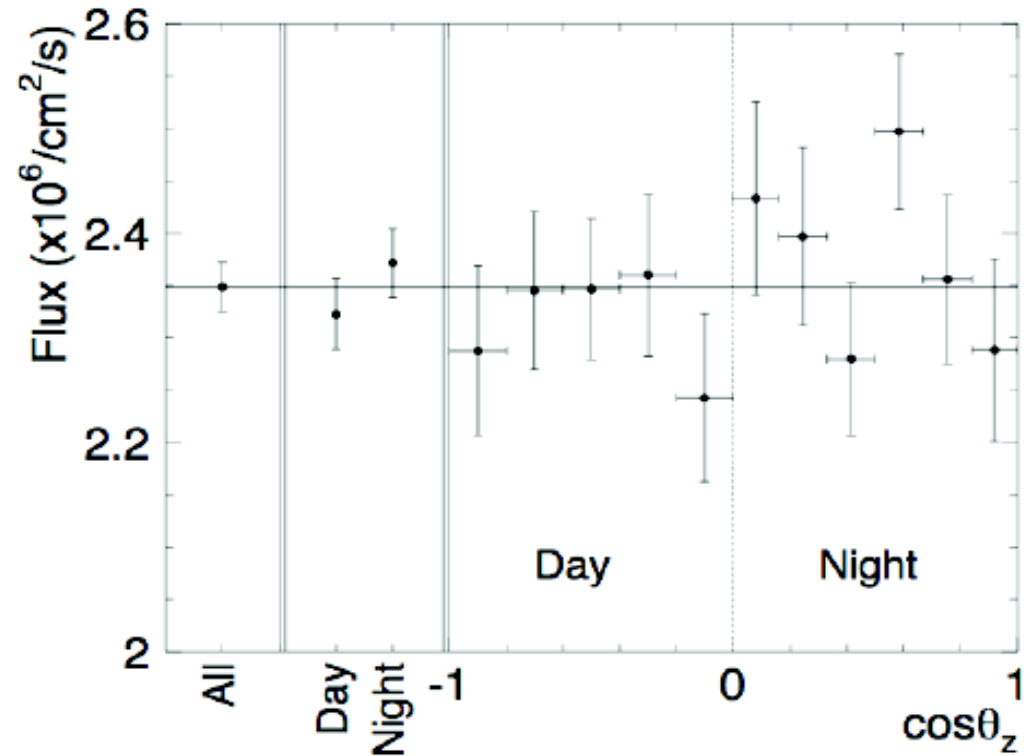
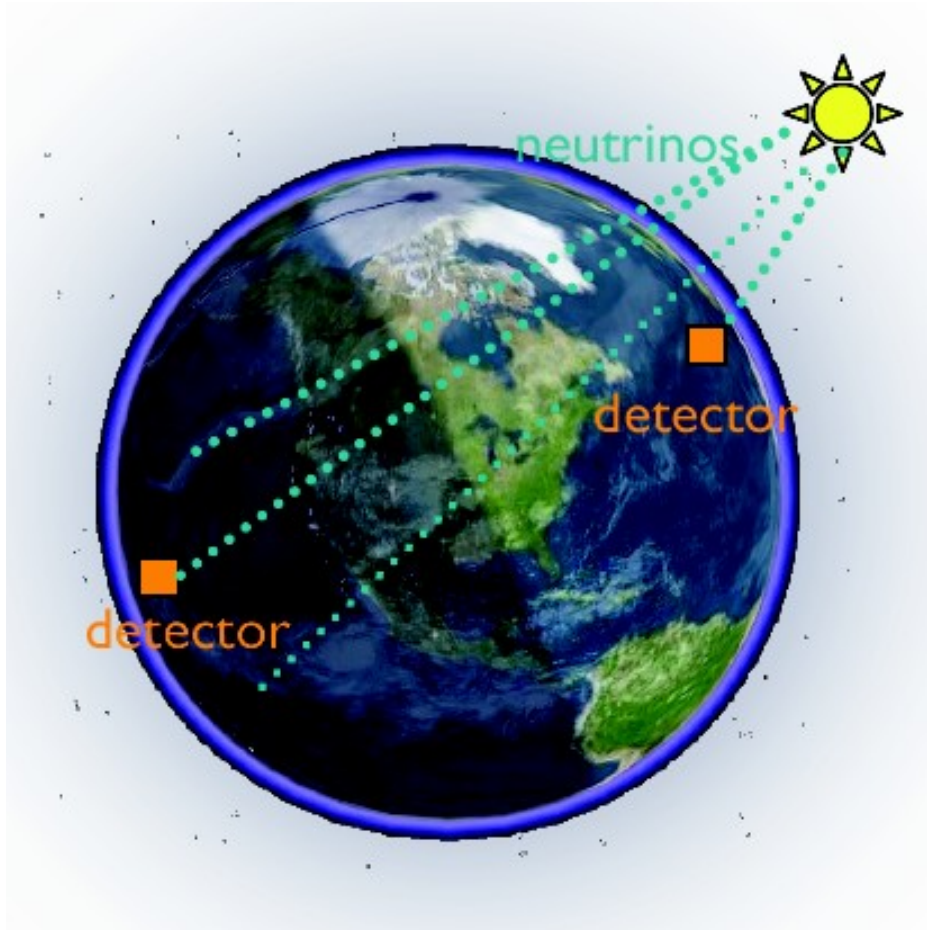
+

matter effects

explain beautifully
all solar neutrino experiments

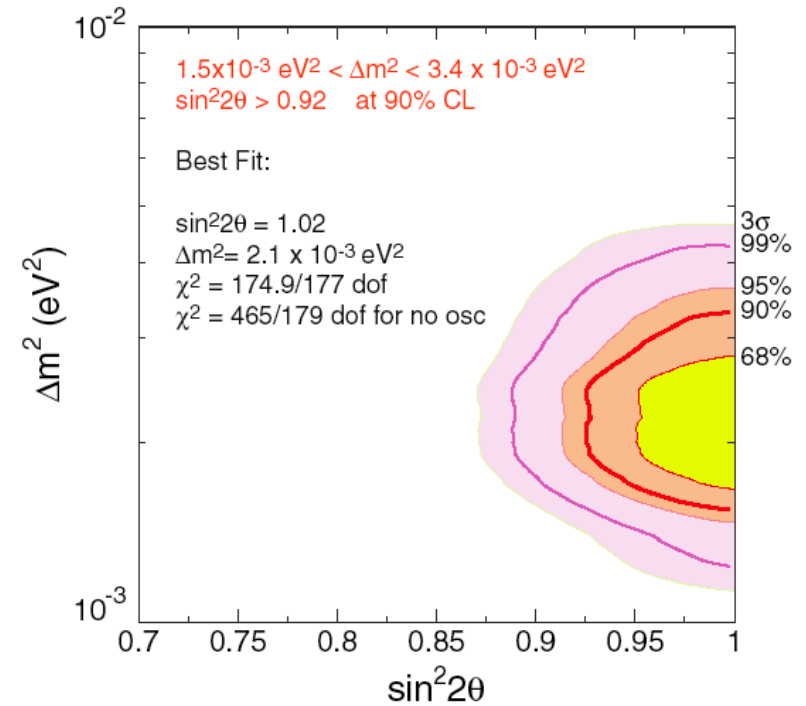
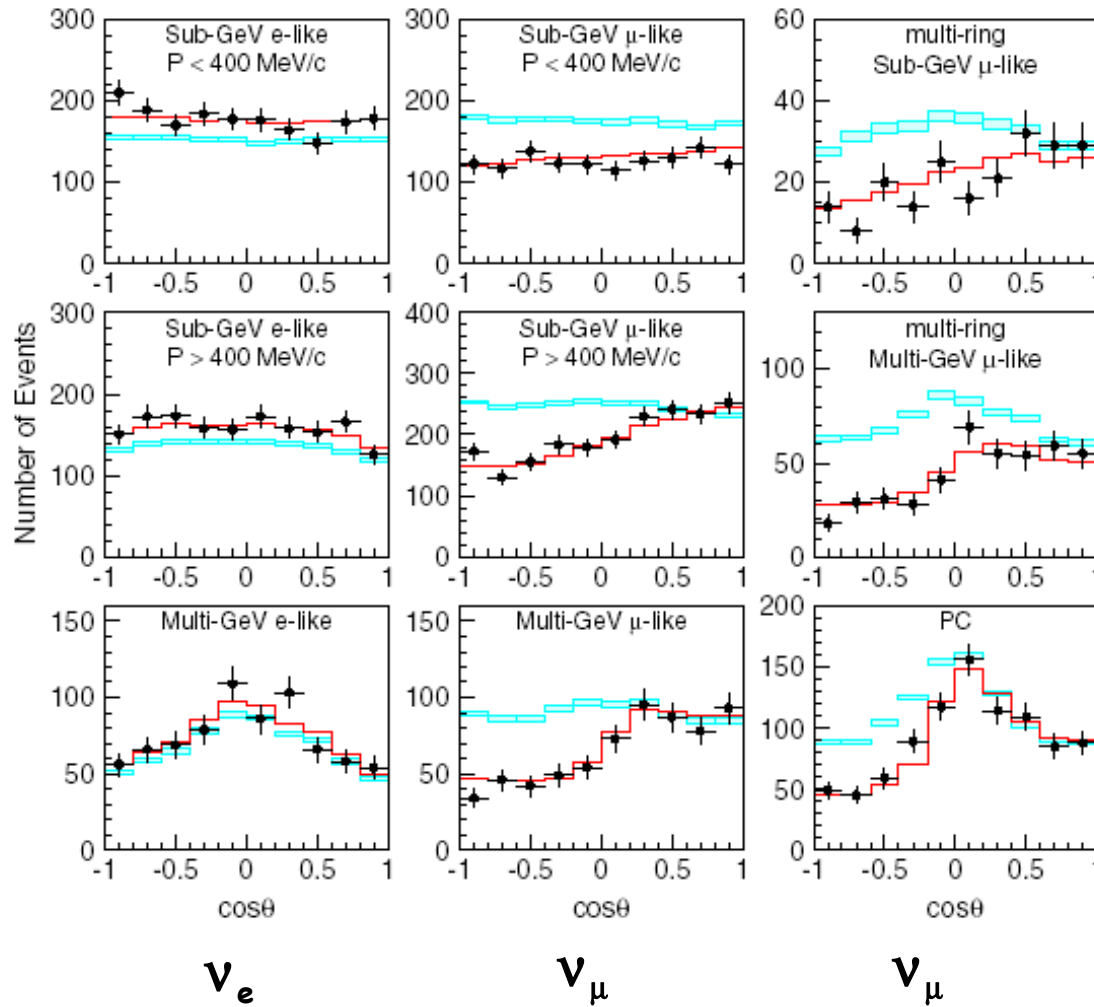


Neutrino regeneration in the Earth ?



- SK sees no significant day-night effect

Atmospheric ν oscillations



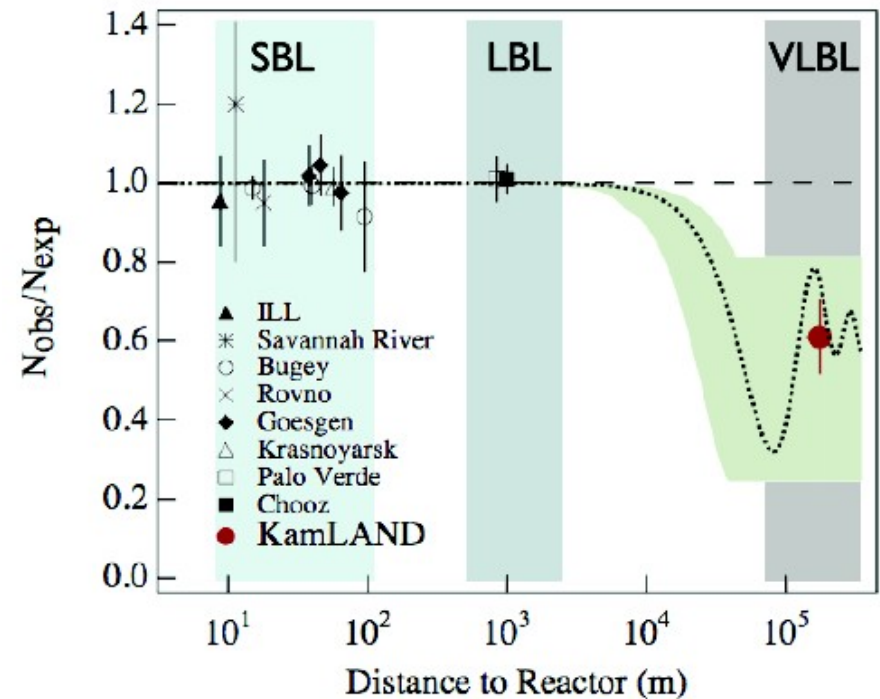
$\nu_\mu \rightarrow \nu_\tau$ oscillations

$$\Delta m^2 = 2.1 \cdot 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta \approx 1$$

Reactor experiments

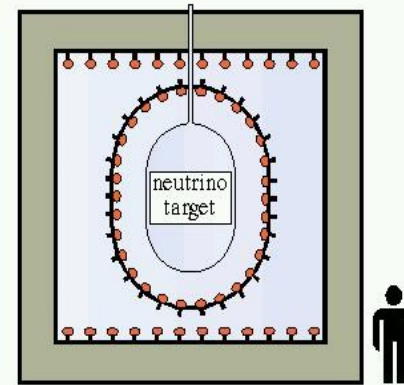
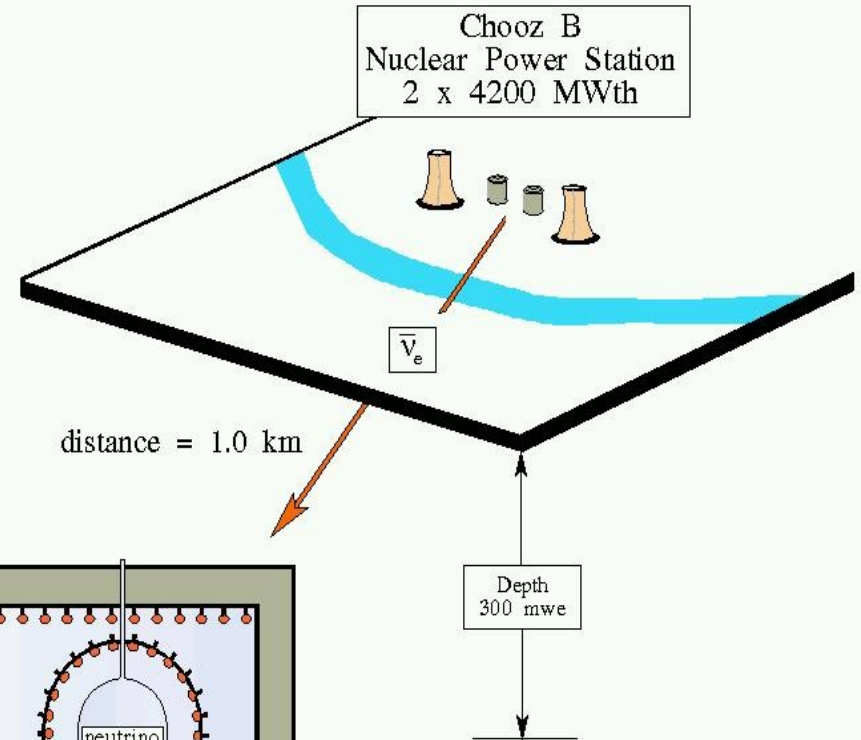
- SBL 10-100m from the reactor : exclusion regions
- LBL ~1 km CHOOZ, sensitive to Atmospheric neutrino parameter space
- VLBL 100km KamLAND evidence for disappearance



LBL experiments



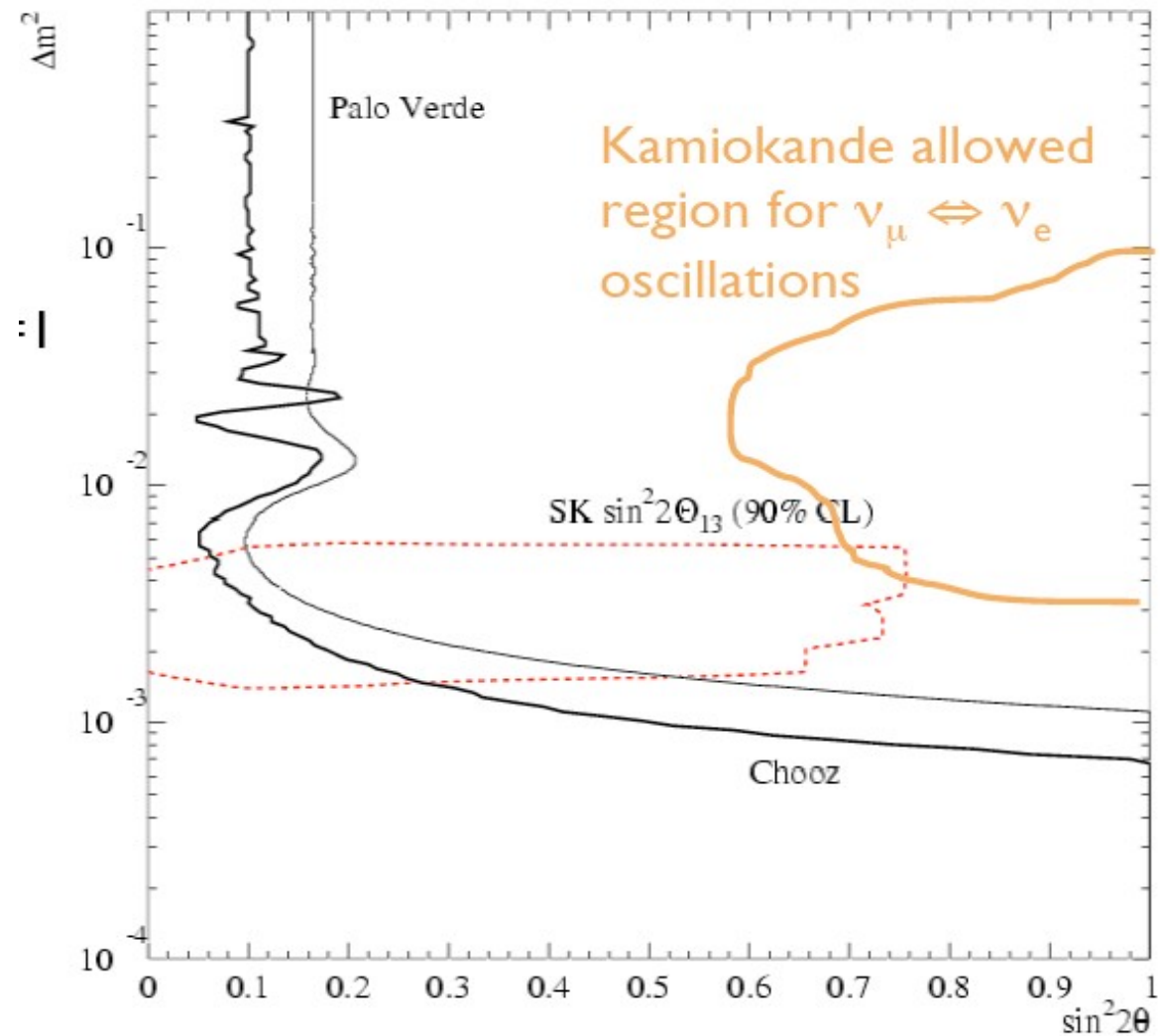
- Liquid scintillator +Gd
- Coincidence from e^+ capture and n-capture (8MeV gamma)



Chooz Underground Neutrino Laboratory
Ardennes, France

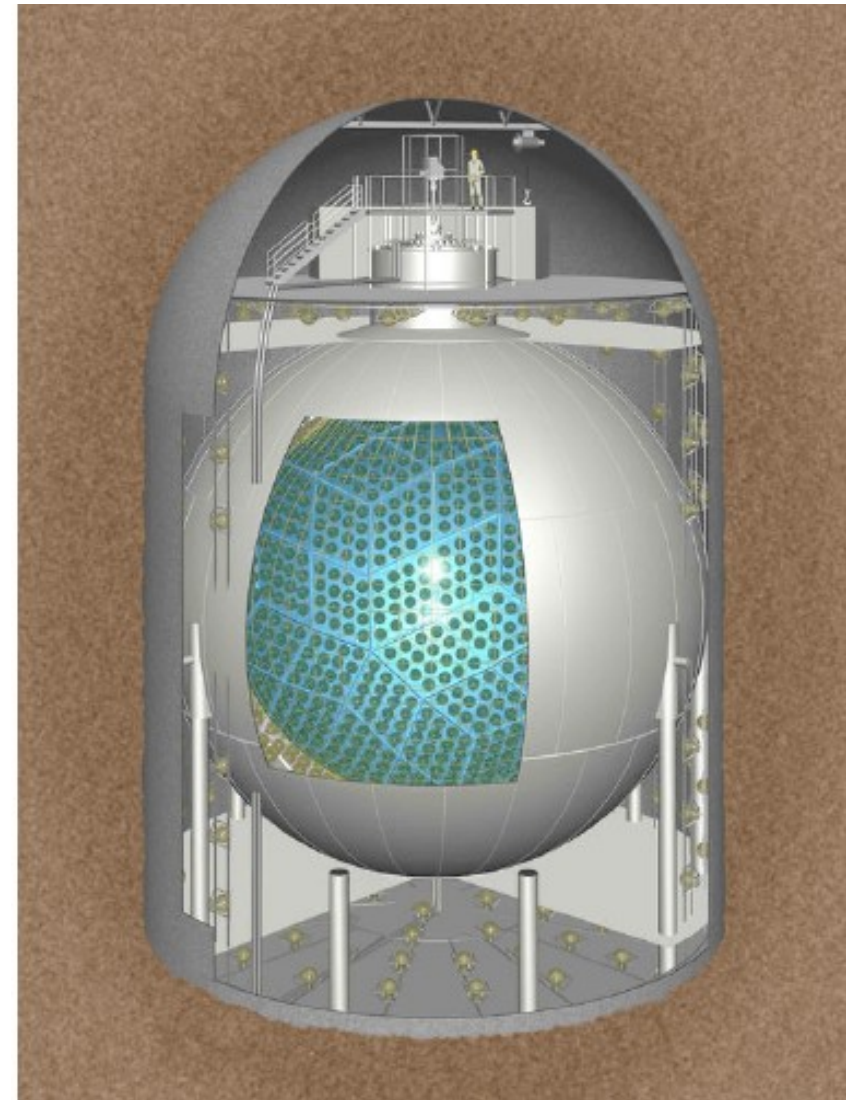
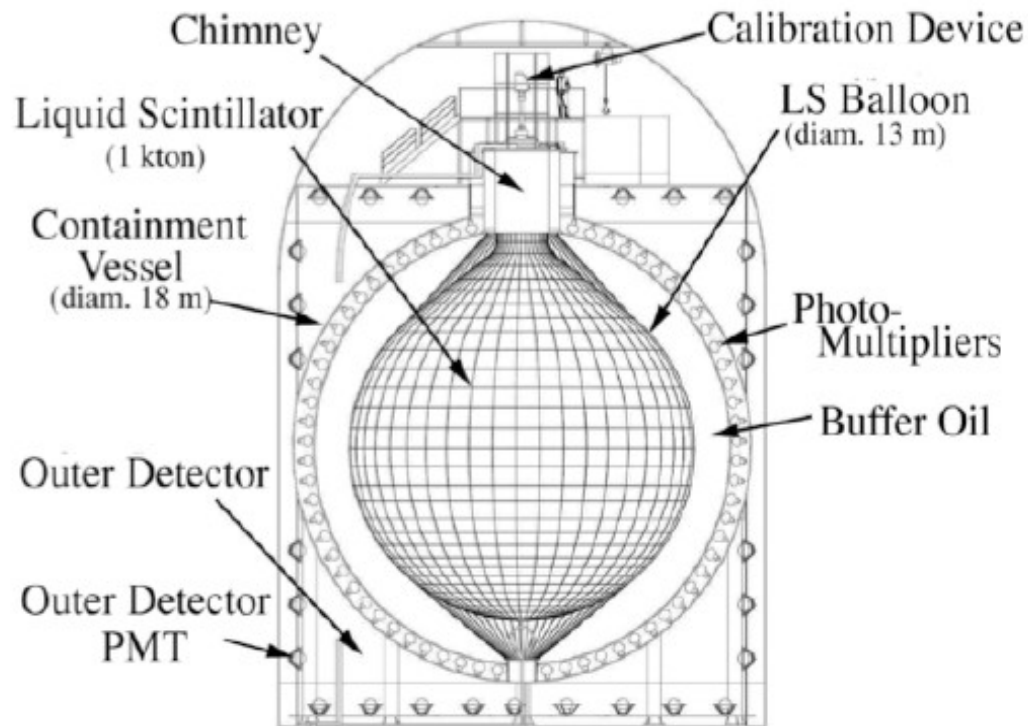
Chooz and Palo Verde

- No disappearance observed
- Excludes the region allowed by SK atmospheric neutrino anomaly



KamLAND

- Measuring $\overline{\nu}_e$ from several reactors in Japan
- 1200m³ of scintillator



Kamland location & flux

Many reactors contribute to the antineutrino flux at KamLAND

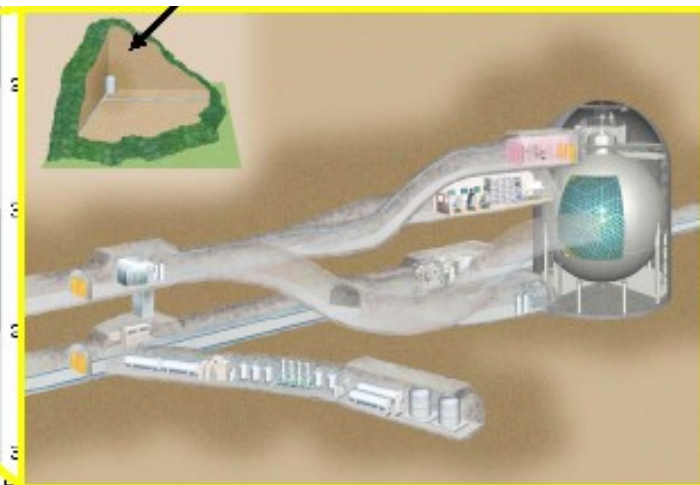


Site	Dist (km)	Cores (#)	P_{therm} (GW)	Flux ($\text{cm}^{-2} \text{s}^{-1}$)	Rate noosc* ($\text{yr}^{-1} \text{kt}^{-1}$)	
Japan	Kashiwazaki	160	7	24.3	$4.1 \cdot 10^5$	254.0
	Ohj	179	4	13.7	$1.9 \cdot 10^5$	114.3
	Takahama	191	4	10.2	$1.2 \cdot 10^5$	74.3
	Tsuruga	138	2	4.5	$1.0 \cdot 10^5$	62.5
	Hamaoka	214	4	10.6	$1.0 \cdot 10^5$	62.0
	Mihama	146	3	4.9	$1.0 \cdot 10^5$	62.0
	Sika	88	1	1.6	$9.0 \cdot 10^4$	55.2
	Fukushima1	349	6	14.2	$5.1 \cdot 10^4$	31.1
	Fukushima2	345	4	13.2	$4.8 \cdot 10^4$	29.5
	Tokai2	295	1	3.3	$1.6 \cdot 10^4$	10.1
	Onagawa	431	3	6.5	$1.5 \cdot 10^4$	9.3
	Simane	401	2	3.8	$1.0 \cdot 10^4$	6.3
	Ikata	561	3	6.0	$8.3 \cdot 10^3$	5.1
	Genkai	755	4	10.1	$7.8 \cdot 10^3$	4.8
Sendai	830	2	5.3	$3.4 \cdot 10^3$	2.1	
Tomari	783	2	3.3	$2.3 \cdot 10^3$	1.4	
South Korea	Ulchin	712	4	11.5	$9.9 \cdot 10^3$	6.1
	Yonggwang	986	6	17.4	$7.8 \cdot 10^3$	4.8
	Kori	735	4	9.2	$7.5 \cdot 10^3$	4.6
	Wolsong	709	4	8.2	$7.1 \cdot 10^3$	4.3
Total Nominal	-	70	181.7	$1.3 \cdot 10^6$	803.8	

* $E_{\nu} > 3.4 \text{ MeV}$
($E_{\text{prompt}} > 2.6 \text{ MeV}$)

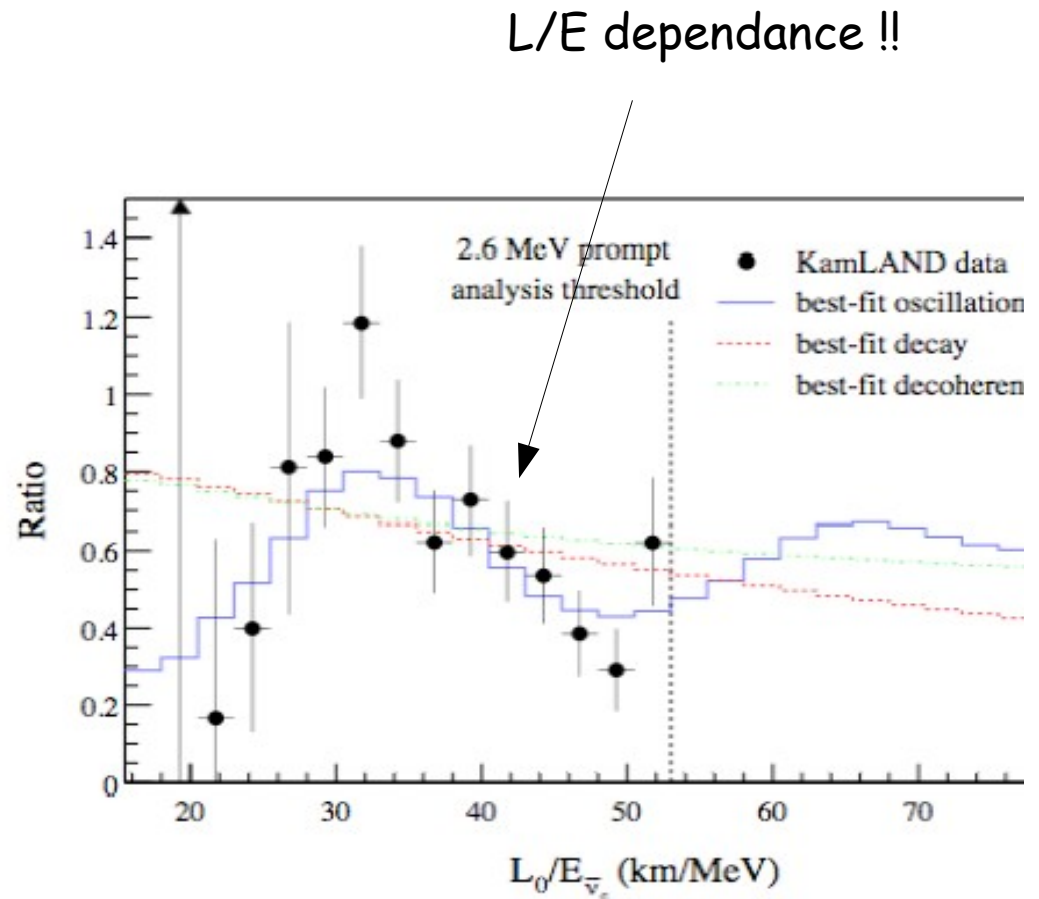
Detailed power and fuel
Composition calculation used

From electrical
power
Japanese average
fuel used



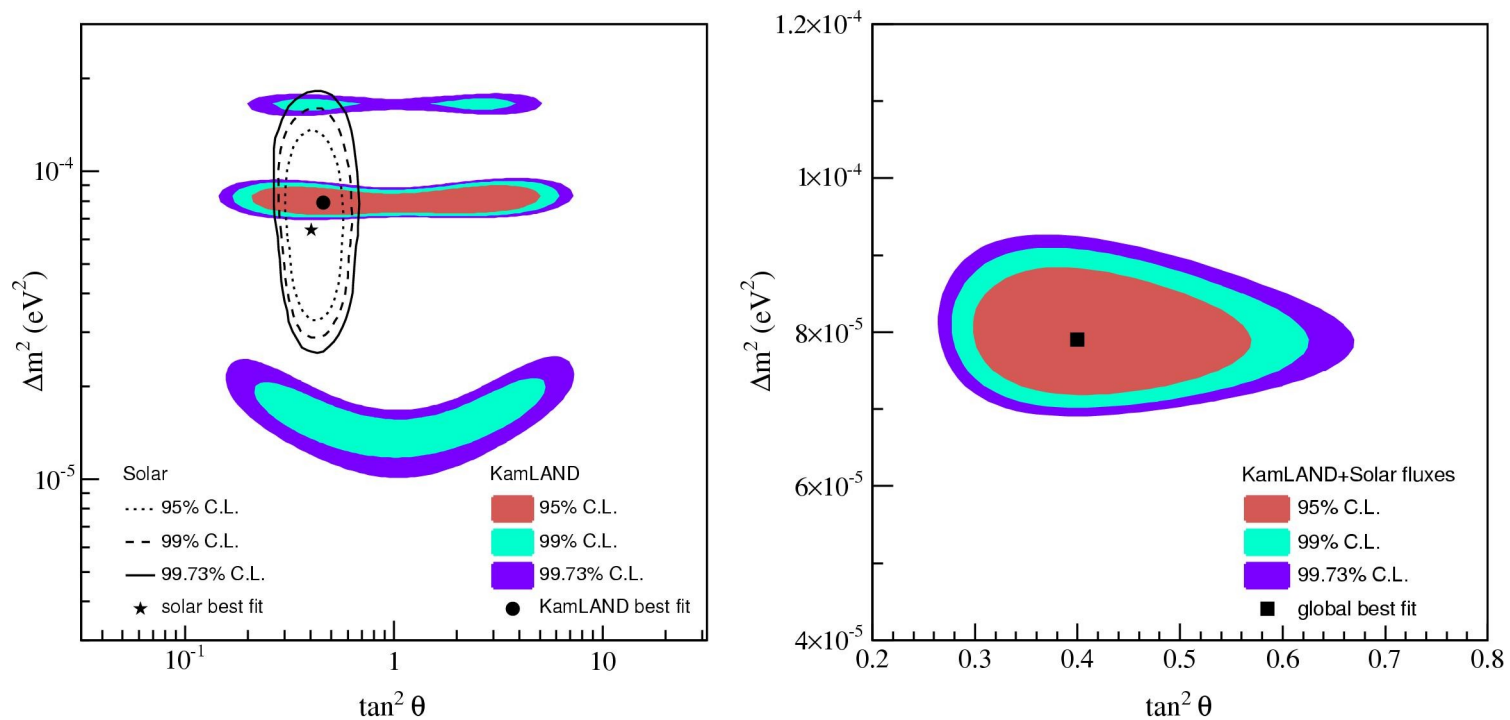
KamLAND results

- Disappearance of ν_e observed
- Designed to check the Large Mixing Angle solar neutrino solution
- $R=0.658\pm 0.044\pm 0.047$

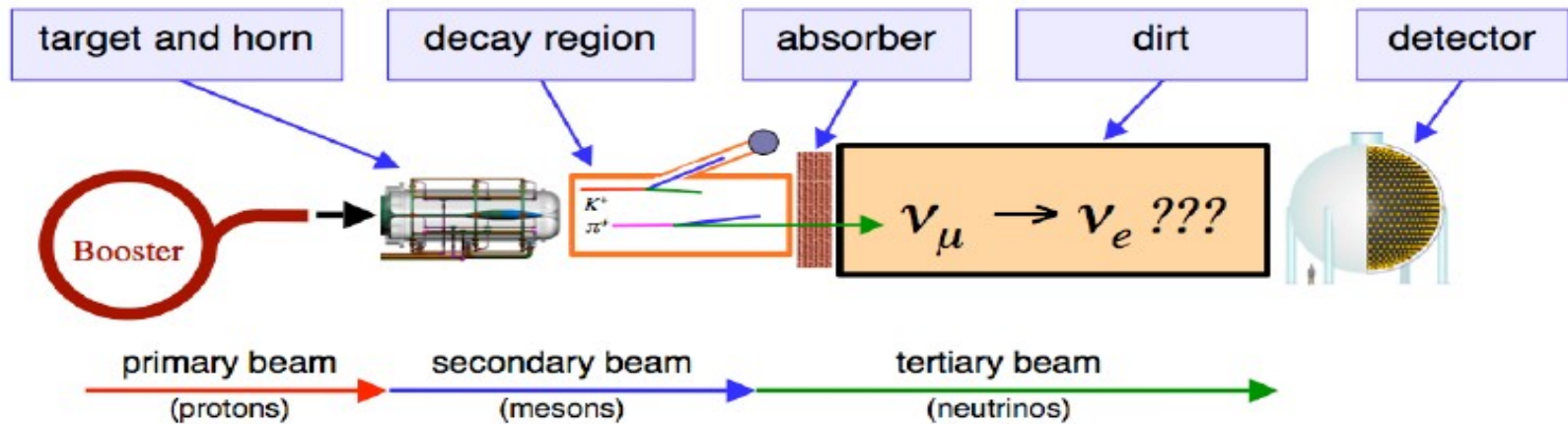


KamLAND confirms solar oscillations

- LMA solution confirmed!



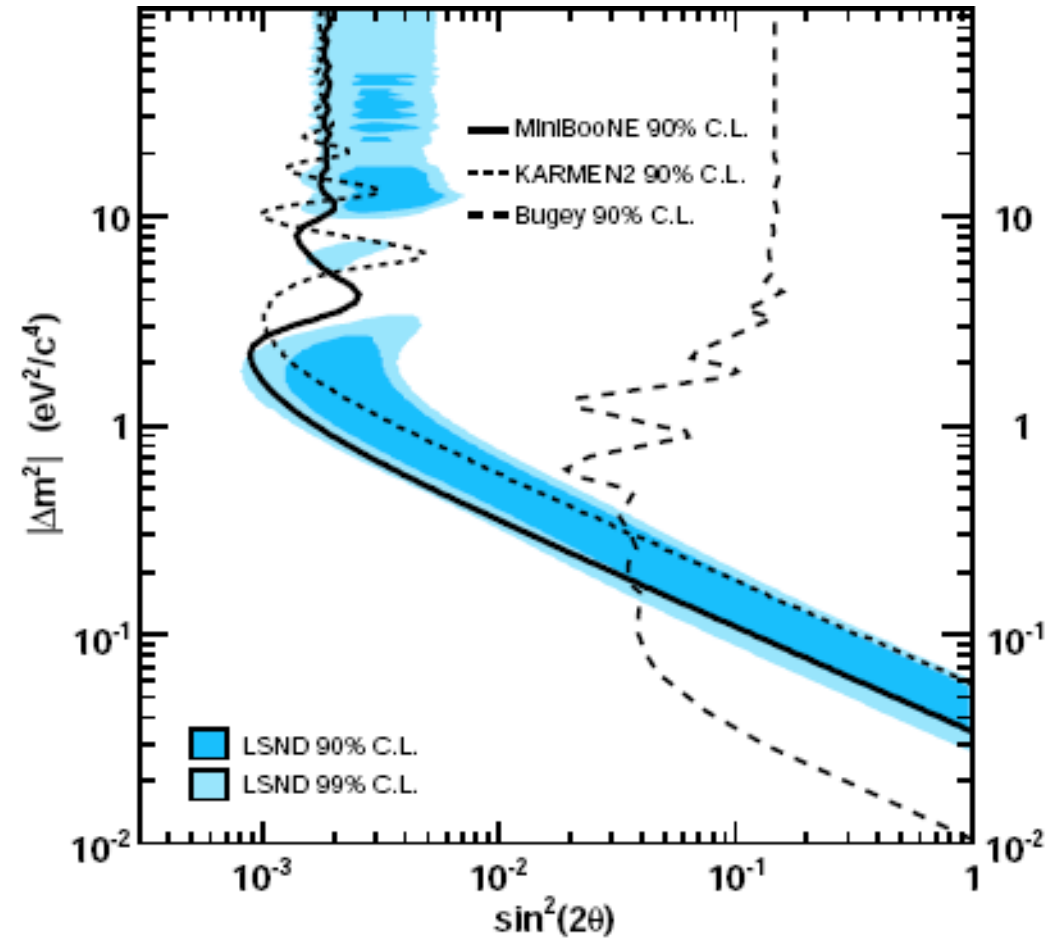
Accelerator experiments



- Neutrinos produced by the decay of pions, kaons and muons from a proton beam onto a target
 - Pion decay in flight: mostly muon neutrinos (OR anti-neutrinos) with energies $\sim GeV$ or more; e.g. SBL: CHORUS, NOMAD, CHARM, LSND; LBL: MINOS, OPERA, ICARUS, T2K
 - Muon decay at rest: muon anti-neutrinos of low energy from muon decay, with energy \sim tens MeV; e.g. KARMEN, LSND
 - Beam dump: protons of very high energy are completely stopped by a target; muon and electron neutrinos with energy $\sim 100 GeV$

$$\nu_{\mu} \longleftrightarrow \nu_e \text{ SBL}$$

- Only LSND claims a signal in $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$ and weaker in $\nu_{\mu} \rightarrow \nu_e$
- $L=30\text{m}$ $E\sim 30\text{MeV}$
- Not confirmed by other experiments





MiniBoone

- Concept of sterile neutrino:

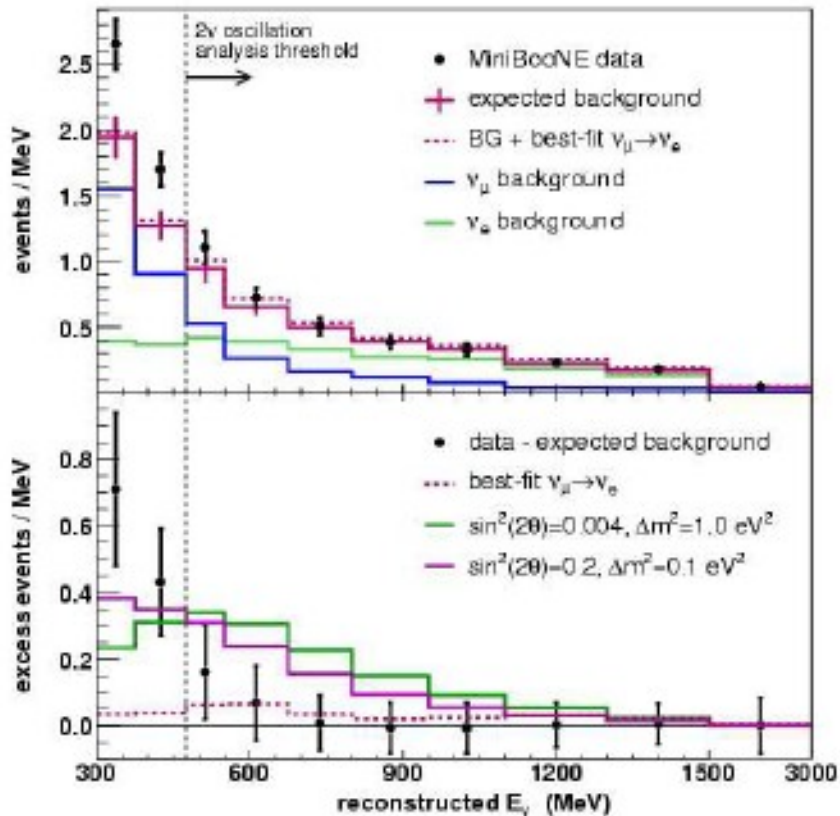
- non-interacting light particle

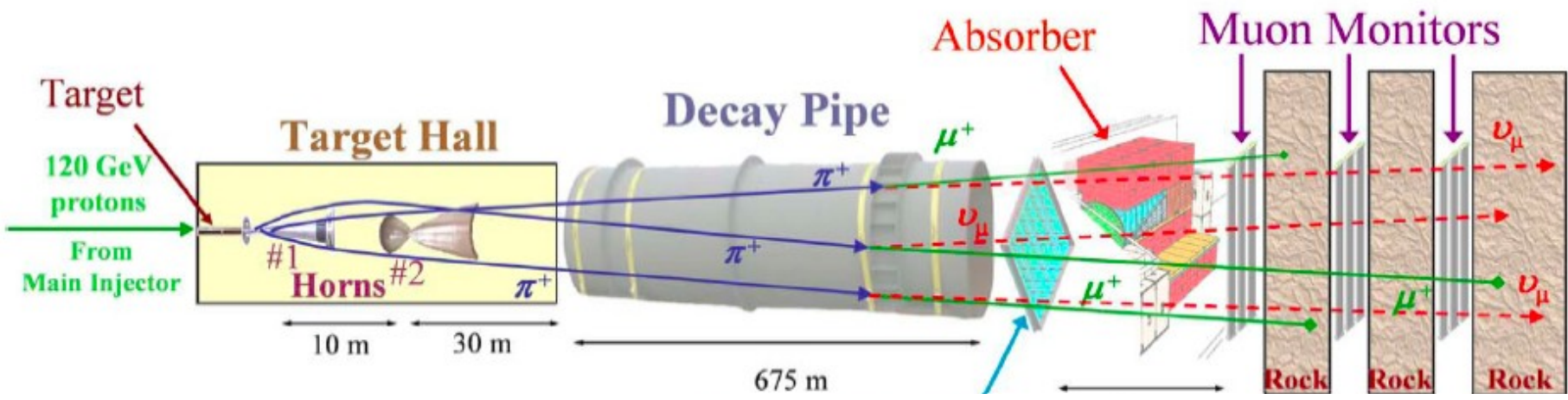
- Singlet in the $SU(2) \times U(1)$ group

- mixed with active neutrinos

$L=500\text{m}$ $E=500\text{MeV}$

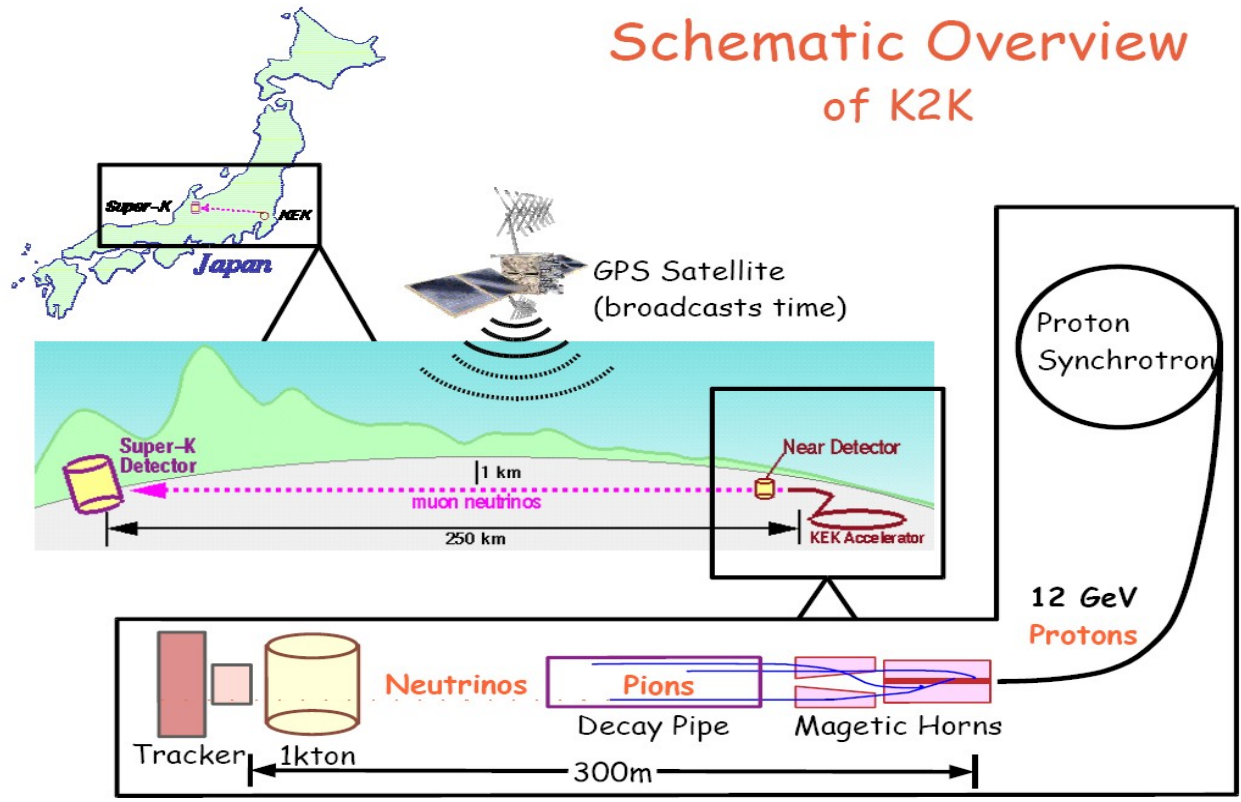
Now running anti- ν mode



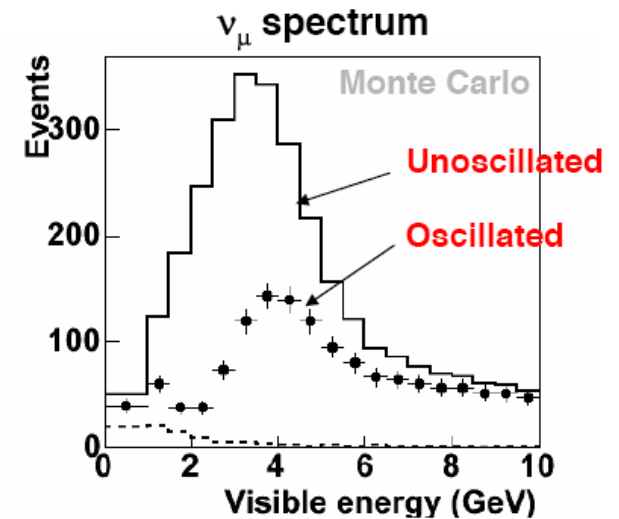
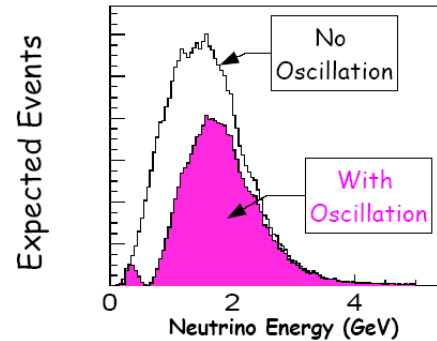
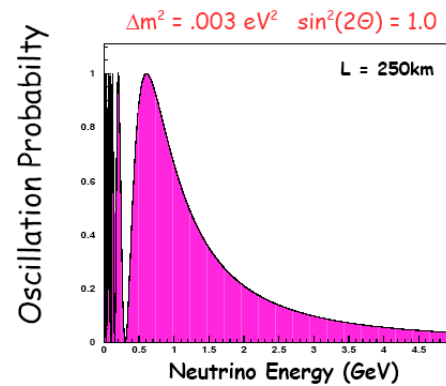
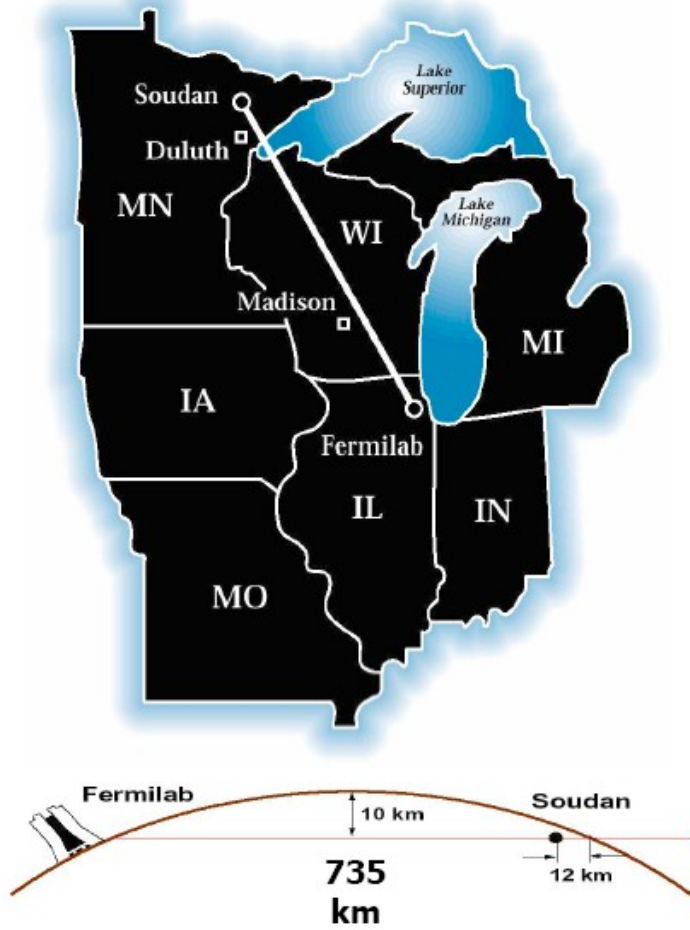


Schematic Overview of K2K

Minos & K2K:



K2K/Minos: confirm atmospheric oscillation with a controlled beam



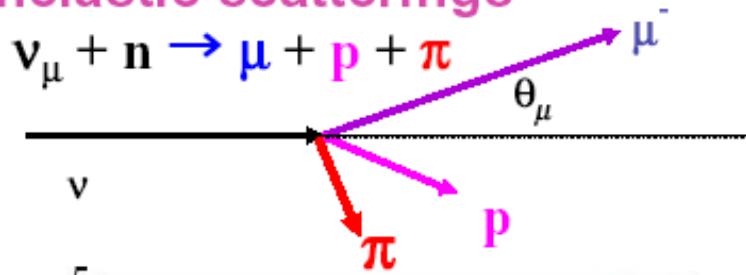
$$E_{K2K} \sim 1 \text{ GeV} \Rightarrow L \sim 250 \text{ Km}$$

$$E_{\text{Numi}} \sim 3 \text{ GeV} \Rightarrow L \sim 750 \text{ Km}$$

Cross sections and energy reconstruction

Numi/MINOS

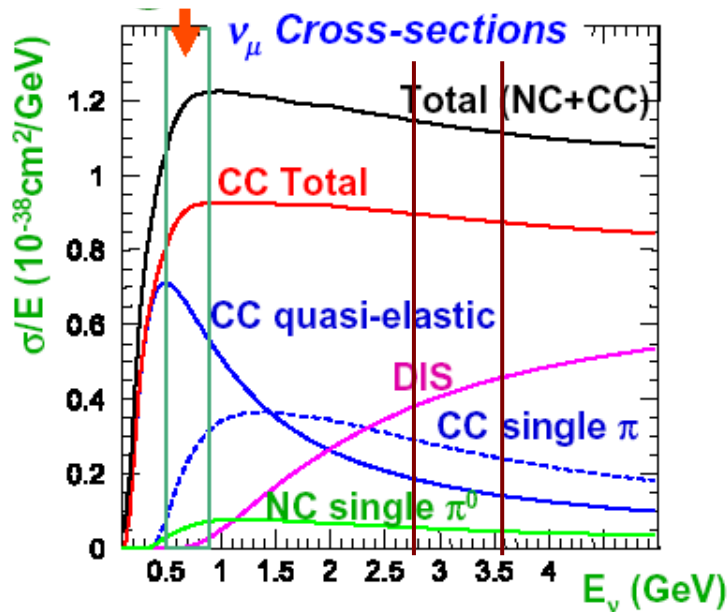
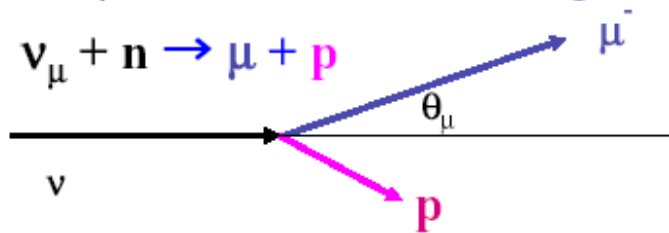
Inelastic scatterings



Beam $E \sim 120 \text{ GeV}$

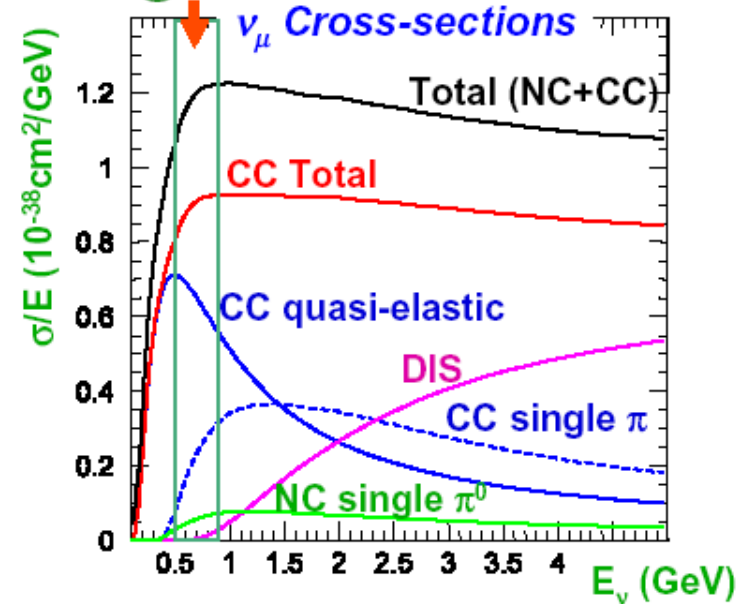
K2K

CC quasi elastic scatterings



Oscillation maximum @ 750 km

Oscillation maximum @ 295 km



Detectors

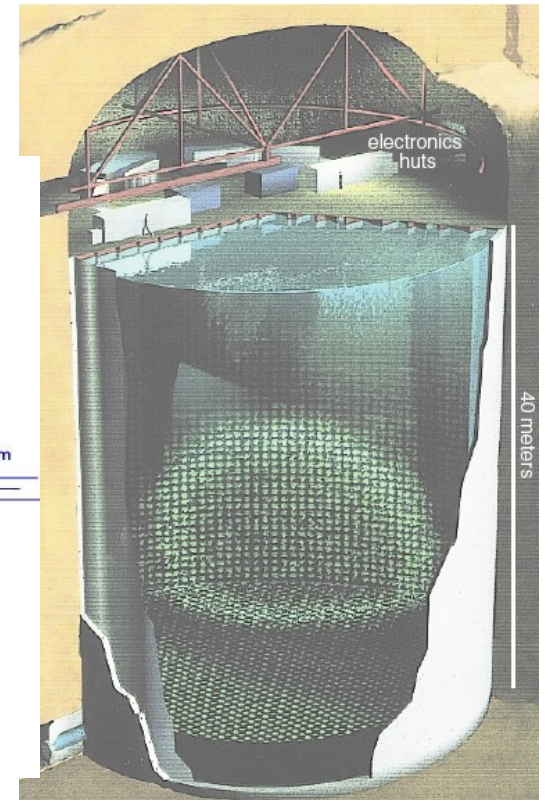
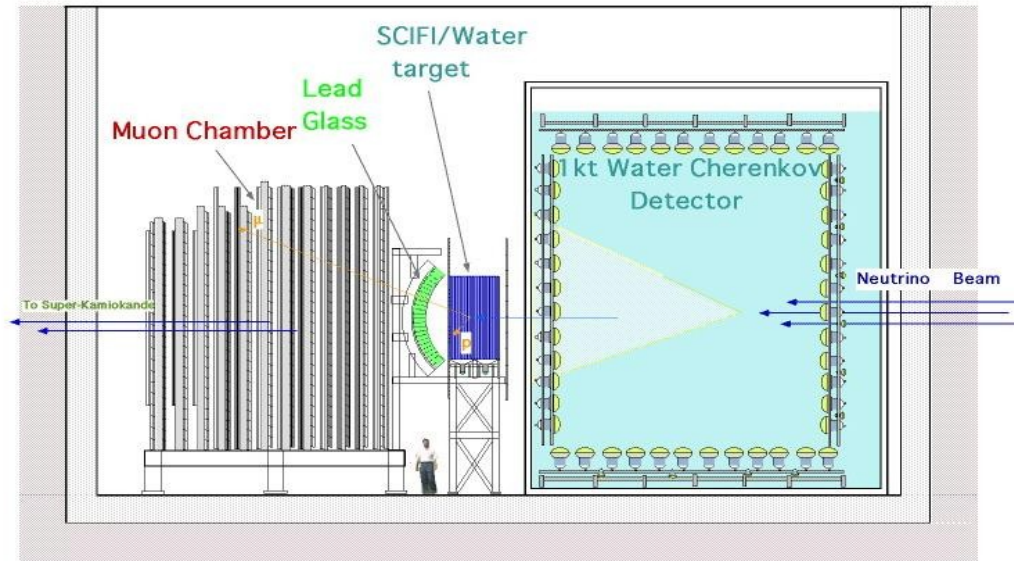
Far Detector

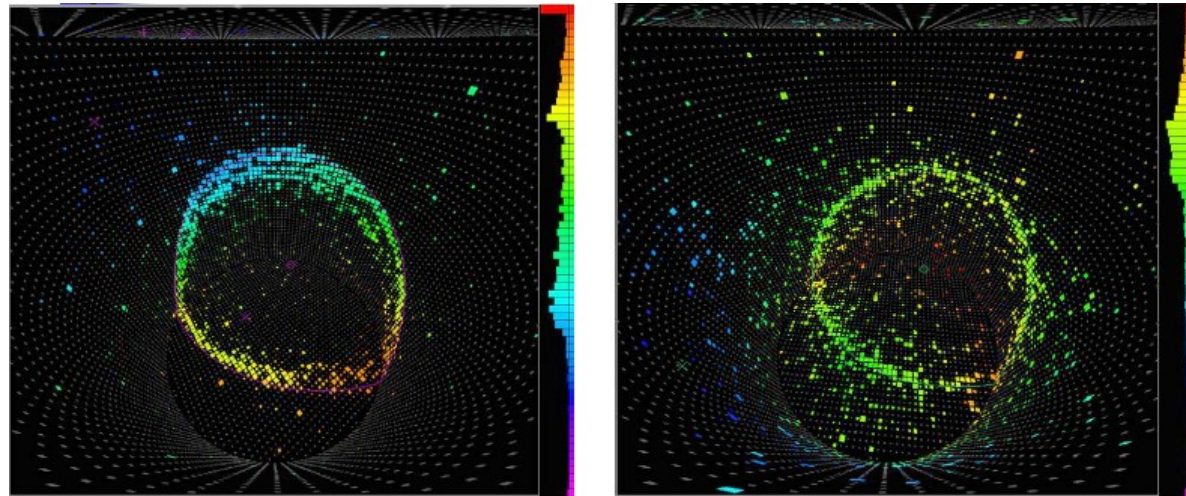
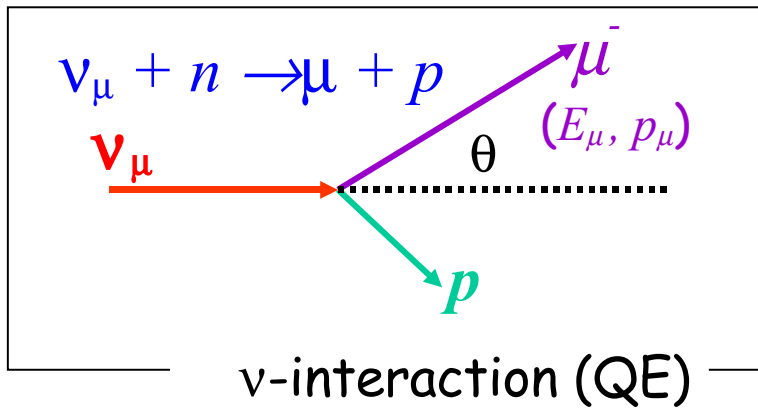


Near Detector

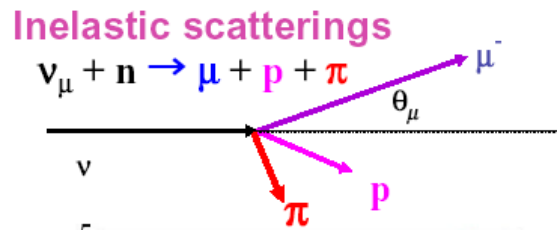


Two different technologies:
Water & Iron

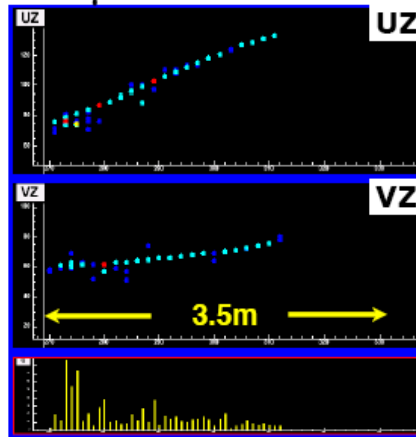




Neutrinos in water & iron

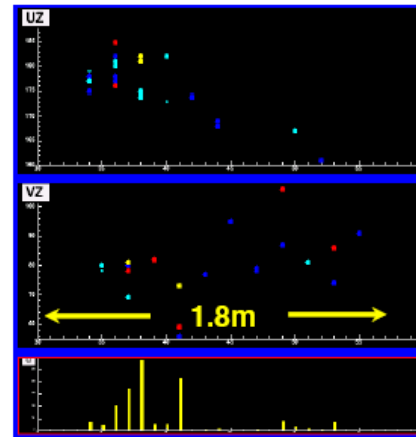


ν_μ CC Event



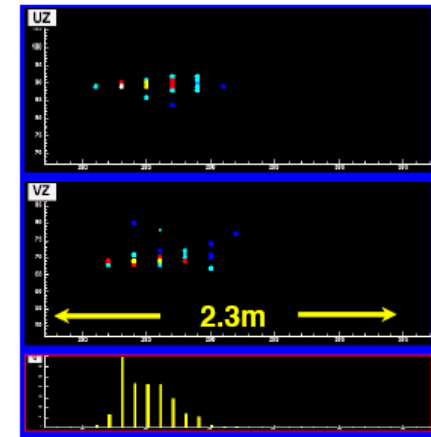
• long μ track + hadronic activity at vertex

NC Event



• short event, often diffuse

ν_e CC Event



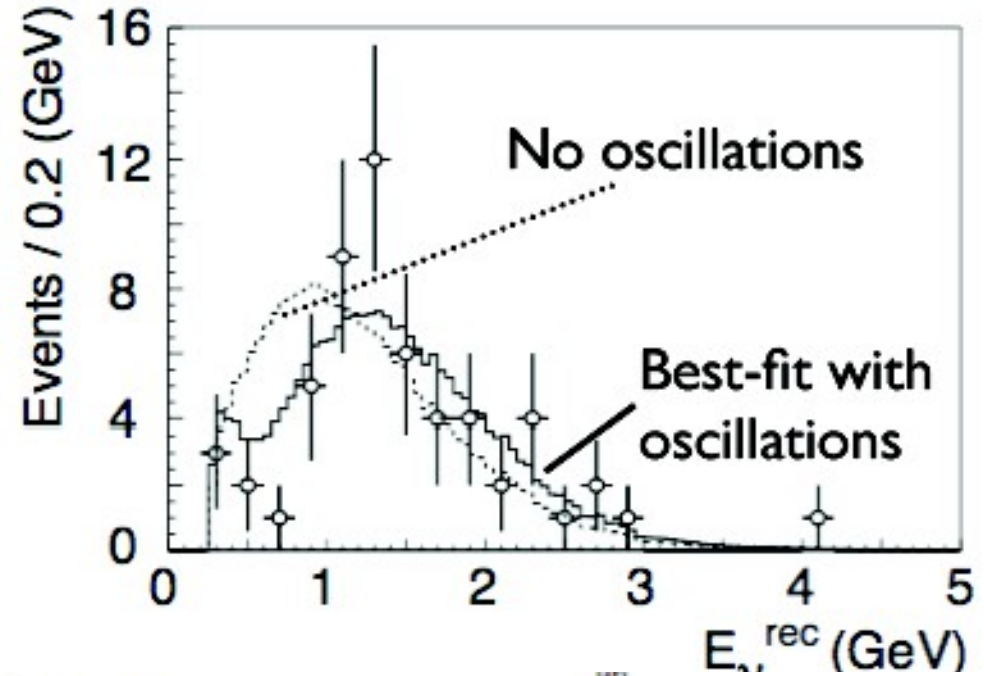
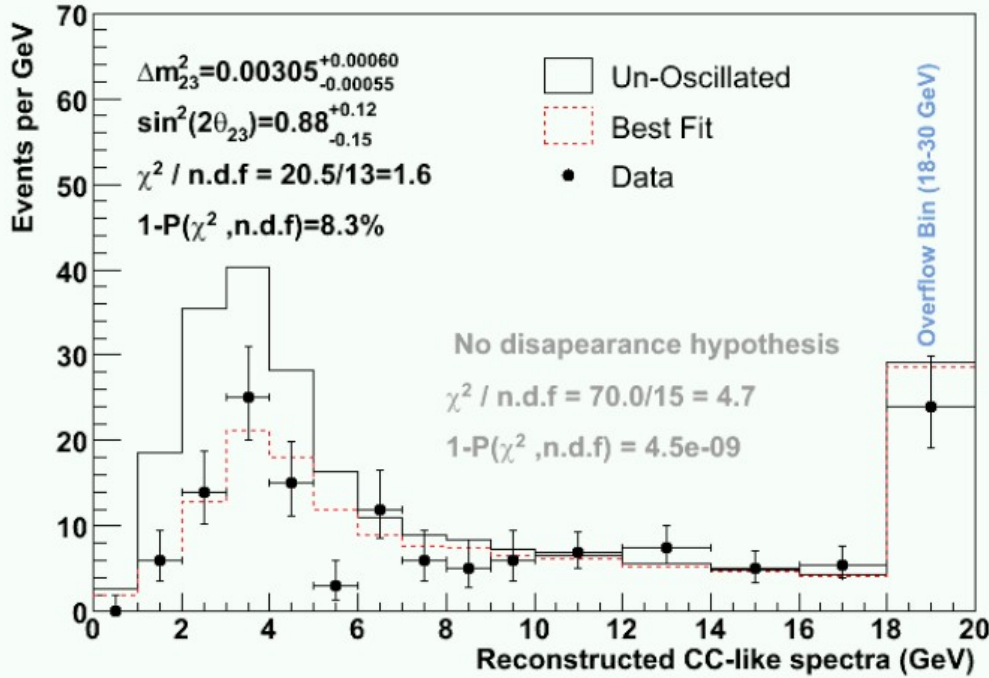
• short, with typical EM shower profile

$$E_\nu = E_{\text{shower}} + P_\mu$$

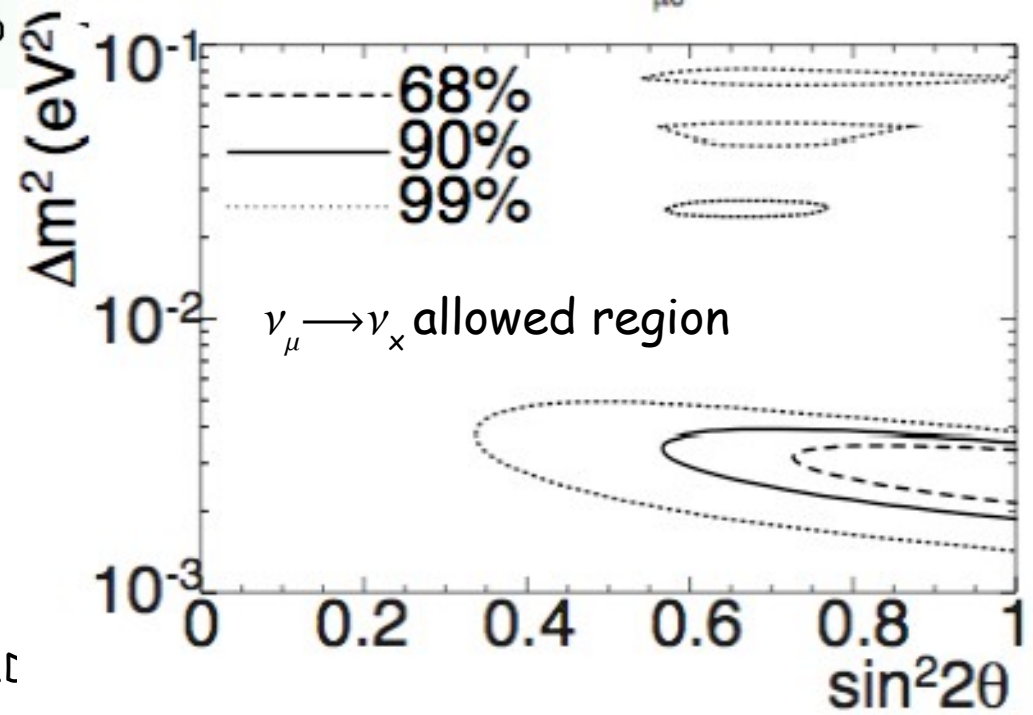
55% NE 6% range, 10% curvature

Minos/K2K results

Oscillation Results for 0.93E20 p.o.t

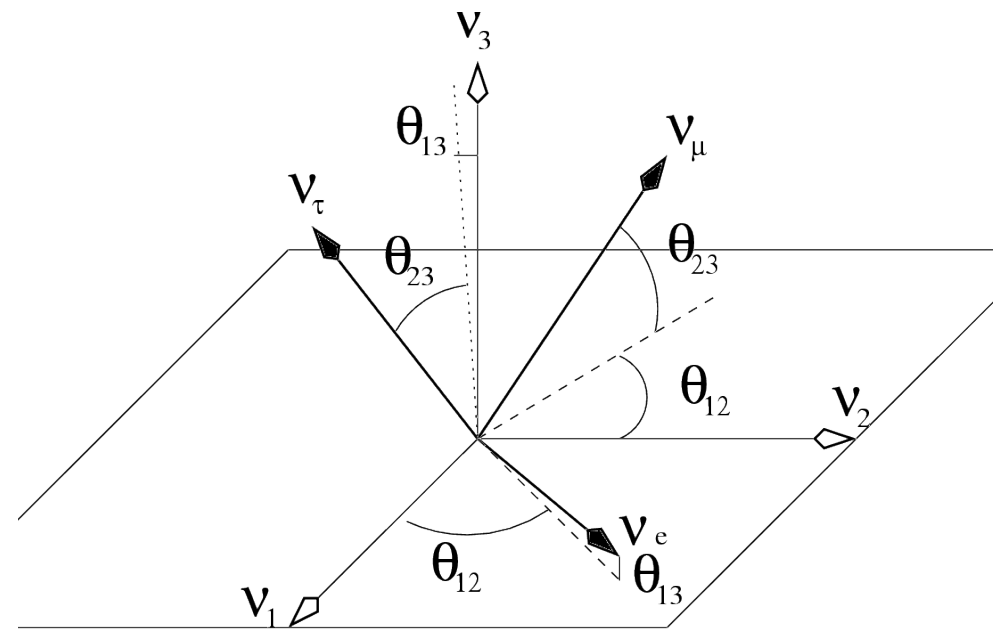
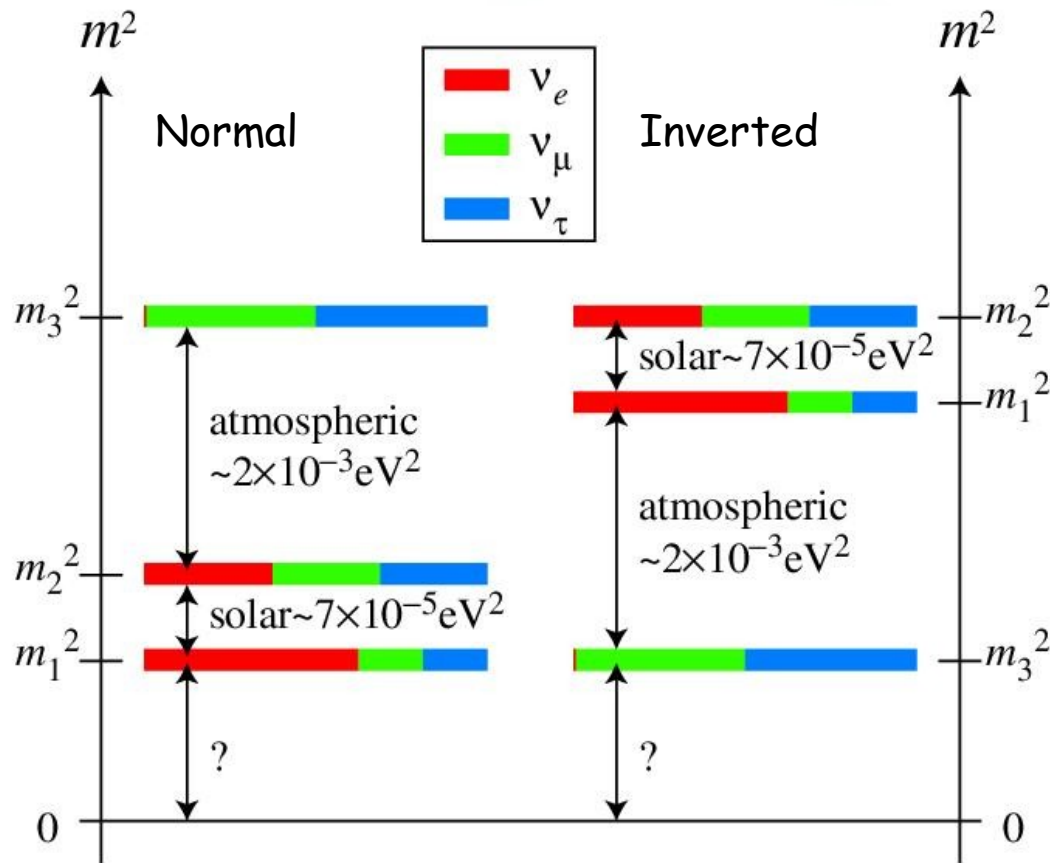


ATMOSPHERIC
OSCILLATION
CONFIRMED!



Oscillations revisited

Oscillation parameter	central value	99% CL range
solar mass splitting	$\Delta m_{12}^2 = (8.0 \pm 0.3) 10^{-5} \text{ eV}^2$	$(7.2 \div 8.9) 10^{-5} \text{ eV}^2$
atmospheric mass splitting	$ \Delta m_{23}^2 = (2.5 \pm 0.2) 10^{-3} \text{ eV}^2$	$(2.1 \div 3.1) 10^{-3} \text{ eV}^2$
solar mixing angle	$\tan^2 \theta_{12} = 0.45 \pm 0.05$	$30^\circ < \theta_{12} < 38^\circ$
atmospheric mixing angle	$\sin^2 2\theta_{23} = 1.02 \pm 0.04$	$36^\circ < \theta_{23} < 54^\circ$
'CHOOZ' mixing angle	$\sin^2 2\theta_{13} = 0 \pm 0.05$	$\theta_{13} < 10^\circ$



The neutrino mixing matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \mathbf{U} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

If $\delta \neq 0, \pi, 2\pi \dots$ then weak interactions violate CP symmetry in the lepton sector (as in the quark sector)

atmospheric

CP violation phase

solar

$$\mathbf{U} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13} e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Links atmospheric & solar sectors