

# Differential Matrix Element Method

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1st Mini-Workshop on « Theoretical advances in the Matrix Element Method »  
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In Collaboration with  
Olivier Mattelaer.



# Motivations

## ➤ For What ?

- Search for new physics looking at differential cross sections with respect to kinematic variables.
- For topologies that cannot be fully reconstructed using the detector information only (i.e. with neutrinos in final state).

Example: **Search** of new physics in  $t\bar{t}$  dileptonic channel.

- Study the Kinematic of  $t\bar{t}$  system (invariant mass, angular correlation).

## ➤ Why MEM ?

- **Matrix Element Method** maximize the information that you can extract from a sample of events using theoretical constraints.

### Prospect at LHC:

Determination of differential cross sections from  $t\bar{t}$  fully leptonic, using the matrix element method.

O.Mattelaer - A.Pin

IL NUOVO CIMENTO 35C

Presented in this talk

Similar Method also used at Tevatron for  $t\bar{t}$  in the semi-leptonic decay channel.

A search for resonant production of  $t\bar{t}$  pairs in  $4.8 \text{ fb}^{-1}$  of integrated luminosity of  $p\bar{p}$  collisions at  $\sqrt{s} = 1.96 \text{ TeV}$ .

CDF Collaboration

FERMILAB-PUB-11-350-E

## The method: DMEM

## ➤ How ?

The probability equation:

$$P(p_{vis}|\vec{\alpha}) = \frac{1}{\sigma_{\vec{\alpha}}} \int dq_1 dq_2 f(q_1) f(q_2) dp |\mathcal{M}_{\vec{\alpha}}(p)|^2 W(p, p_{vis})$$

where  $\vec{\alpha}$  is fixed as the set of parameters for the standard model, becomes a **probability density function**:

$$\frac{\partial \mathcal{P}(p^{vis})}{\partial m} \Big|_{m_0} = \frac{1}{\sigma} \int dx_1 dx_2 f(x_1) f(x_2) d\Phi |\mathcal{M}(p)|^2 W(p, p^{vis}) \times \delta(m_p - m_0)$$

Where "m" represents an arbitrary variable (invariant mass of tt system)

But too complex to be performed with the  $\delta$  function.  
Evaluated on small intervals  $\rightarrow$  **binned** pdf.

$$\int_{m_0}^{m_0+i} dm^* \frac{\partial \mathcal{P}(p^{vis})}{\partial m} \Big|_{m^*}$$

Practically:

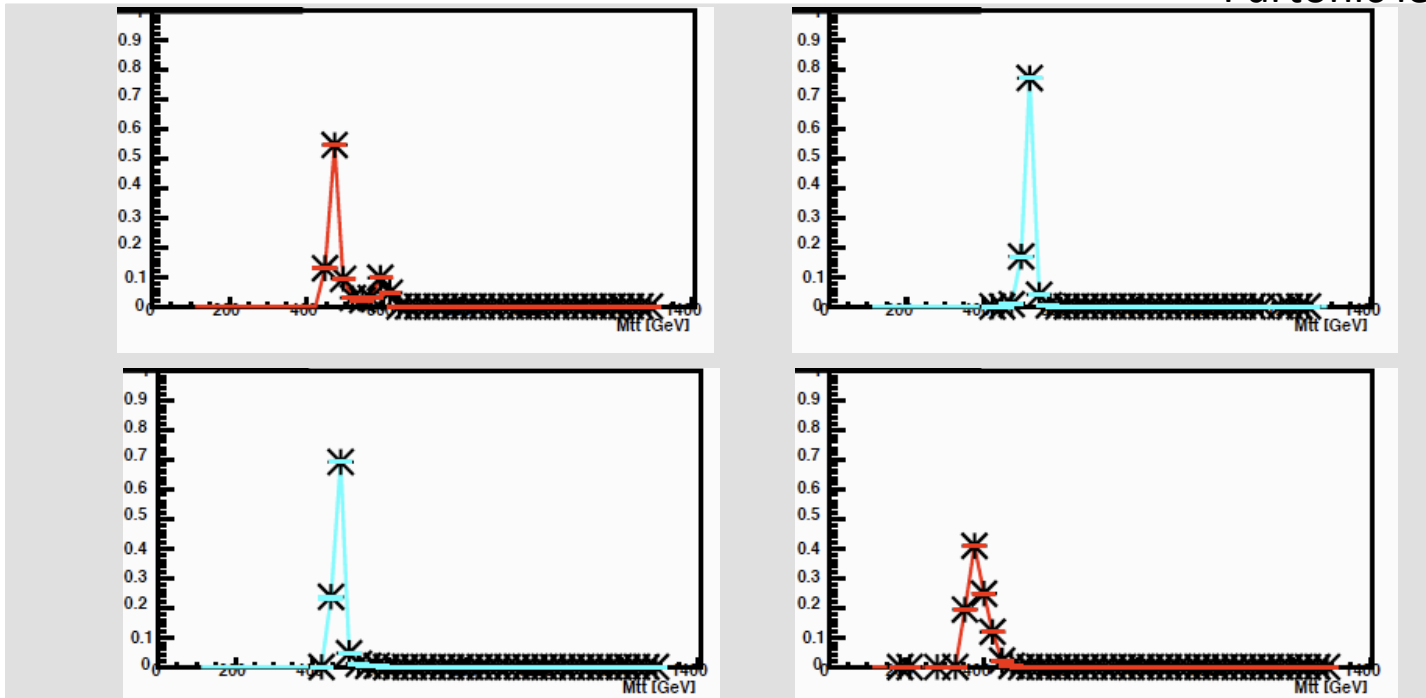
- Quantities of interest are evaluated for each generated partonic state.
- The corresponding bins are incremented by the value of the integrand.
- This way to evaluate on small intervals introduces a binning of the differential variable.

# The method

Example:  $t\bar{t}$  invariant mass system for dileptonic events

- **Matrix element** for  $t\bar{t}$  production and decay. (MadGraph)
- Integration performed with **MadWeight**<sup>1</sup>.
- **Distribution** obtained for **each event**:

Partonic level



- Both **jet permutations** are considered: reflected with double peak for some event

These distributions are **normalized** to 1 (**pdf**) and combined as:  $\frac{1}{\sigma} \frac{\partial \sigma}{\partial m} \sum_{event} \frac{1}{\mathcal{P}} \frac{\partial \mathcal{P}}{\partial m}$

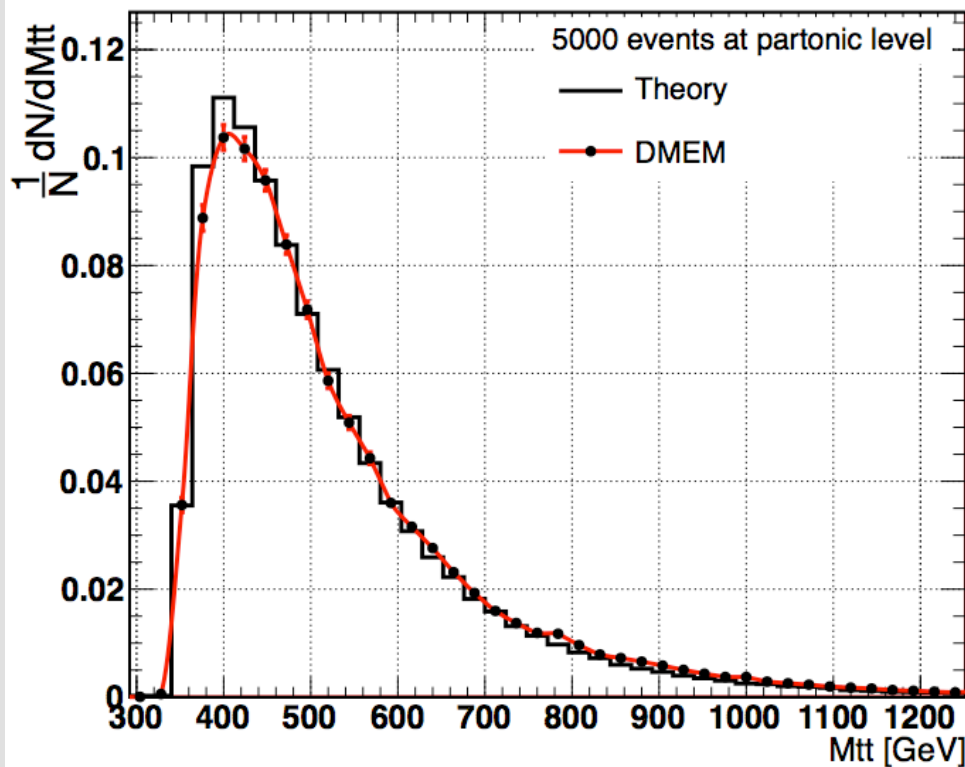
1 : Pierre Artoisenet, Vincent Lemaître, Fabio Maltoni, Olivier Mattelaer, « Automation of the matrix element reweighting method », JHEP 2010

## validation

Comparison with theory **at leading order** for :

- $M_{t\bar{t}}$  : sensitivity to  $X \rightarrow t\bar{t}$  .
- $\text{Cos}(\theta_{t\bar{t}}^*)$  : sensitivity to the spin of  $X$  .
- selected events :
  - 2 isolated muons  $p_t > 20$  GeV and  $|\eta| < 2.4$  .
  - **Exactly 2** jets  $p_t > 30$  GeV and  $|\eta| < 2.4$  and b-tagged.
  - MET > 30 GeV.

$$\sqrt{s} = 14 \text{TeV}$$



## Partonic level

Perfect detector

transfer function :

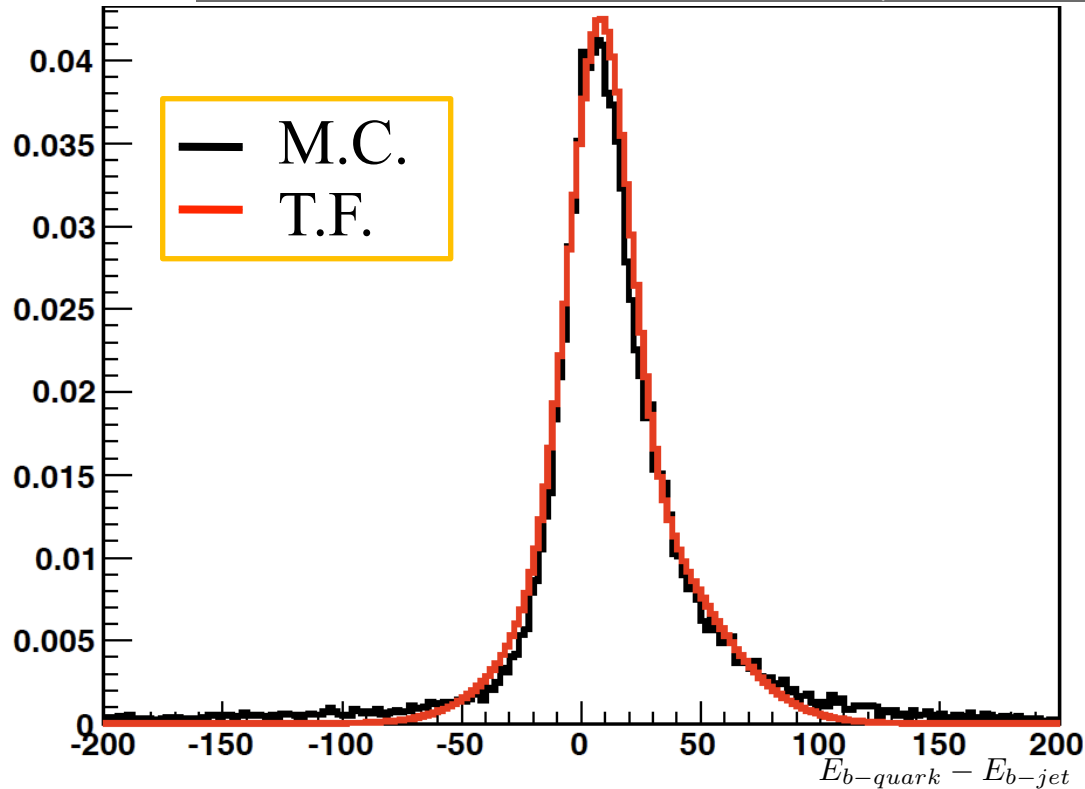
$$W = \delta \text{ function}$$

- Theory estimated from  $l\bar{l}b\bar{b}v$  final state.
- DMEM applied on  $l\bar{l}b\bar{b} + \text{MeT}$  final state.
- The neutrino momenta are in fact fixed by the mass constraints.

## realistic situation

- Parton shower: Pythia (add ISR/FSR)  
No correction used.
- Fast detector simulation response with Delphes<sup>2</sup>
- Transfer function on jet energy:

$$W(E_j, E_{part}) = \frac{1}{\sqrt{2}(P_2 + P_3 \cdot P_5)} \cdot \left( e^{-\frac{[(E_{part} - E_j) - P_1]^2}{2 \cdot P_2^2}} + P_3 \cdot e^{-\frac{[(E_{part} - E_j) - P_4]^2}{2 \cdot P_5^2}} \right)$$

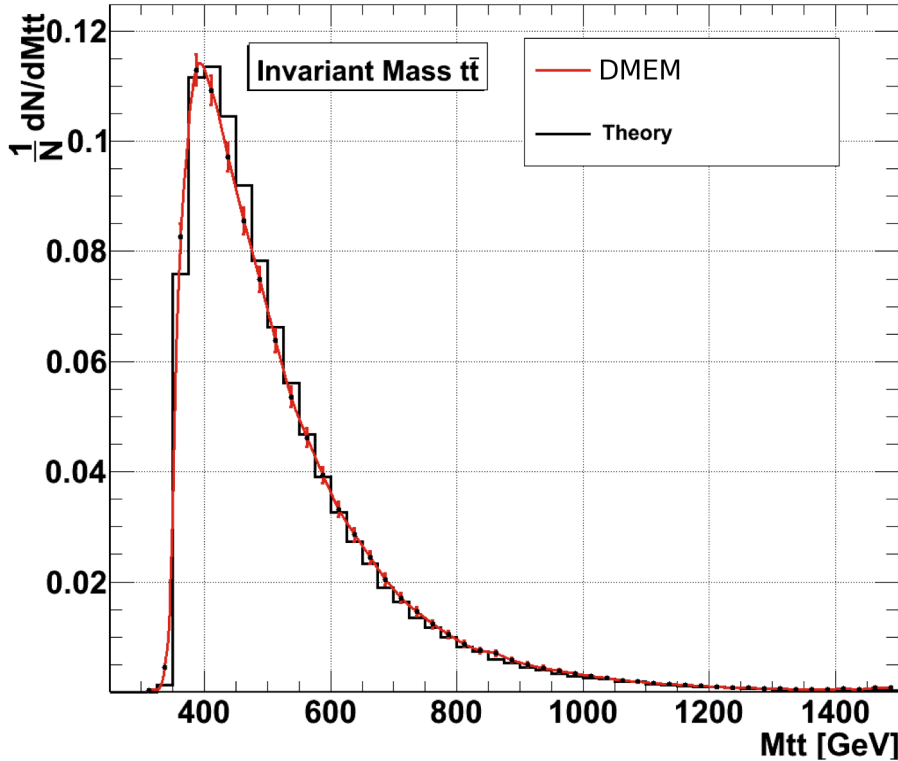


- 150.000 pairs of jets/partons
- 10 parameters :

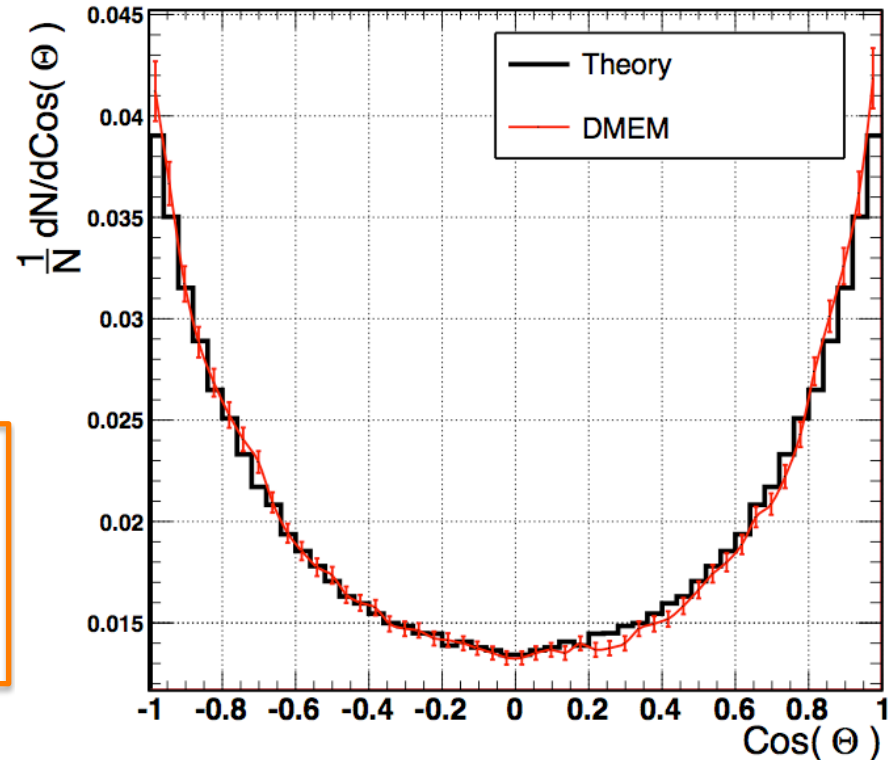
$$P_i = a_{i0} + a_{i1} \cdot E$$

2 : S. Ovin and X.Rouby, « Delphes, a framework for fast simulation of a generic collider experiment » ,

realistic situation: Validation



- Good agreement with the theory.
- No bias due to the transfer function



Reconstruction of other variables  
 as  $\text{Cos}(\theta_{t\bar{t}}^*)$   
 (top-diffusion angle in the  $t\bar{t}$  rest frame )

Prospect at LHC :  $(pp)\sqrt{s} = 14$  TeV

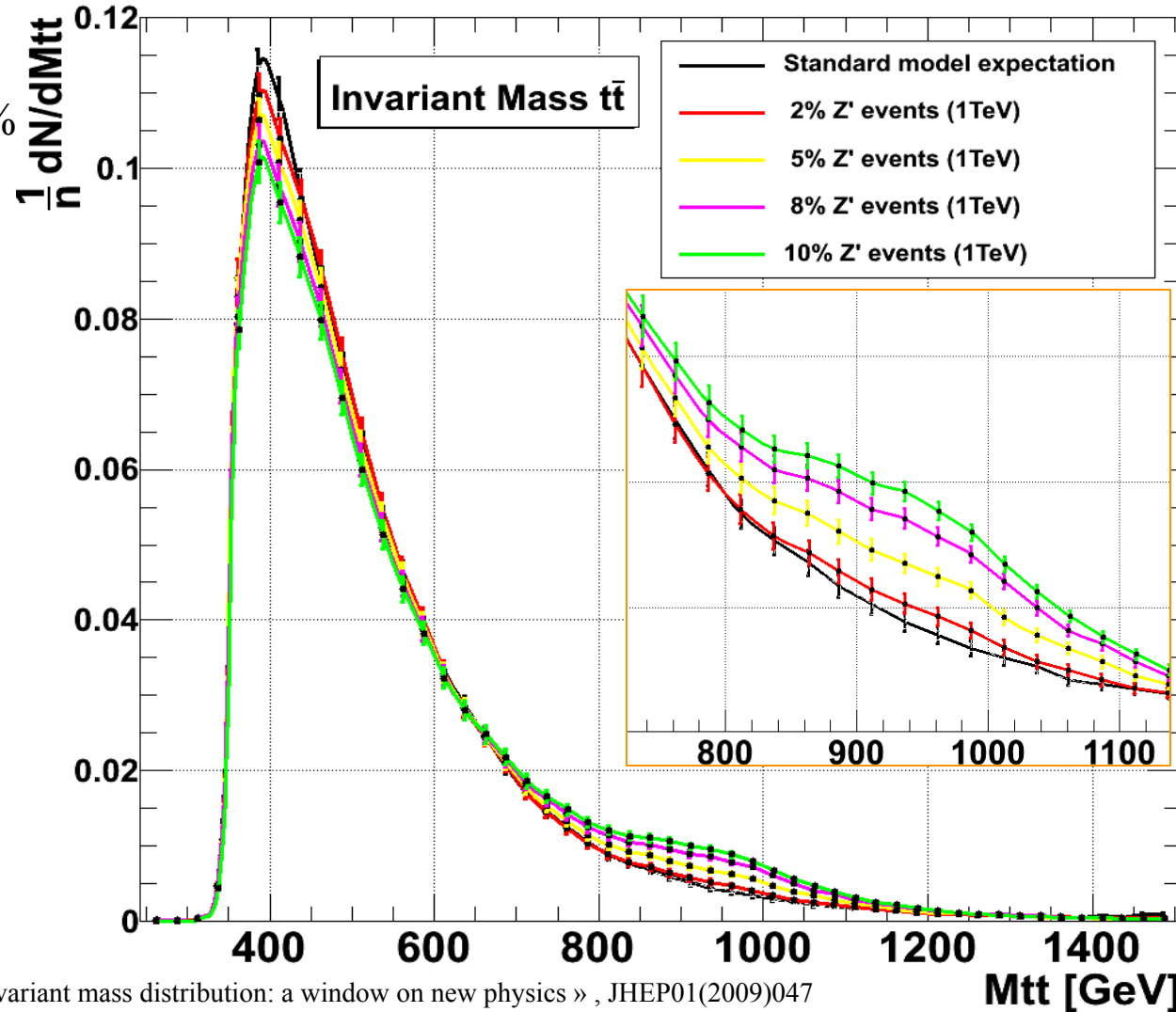
**ONLY** standard model  $t\bar{t}$  dileptonic Matrix Element is used.

Deviation from the standard model introducing a resonance decaying in  $t\bar{t}$ .

- Spin 1 particle ( $Z'$ )<sup>3</sup>.
- 1 TeV
- Various  $\frac{N_{Z'}}{N_{tot}}$  : 2%, 5%, 8% 10%

Compatibility with the S.M.

$N_{Z'}/N_{tot}$	NOT S.M. C.L.
2%	72 %
3%	95.6 %
5%	> 99.998%
8%	> 99.998%
10%	> 99.998%

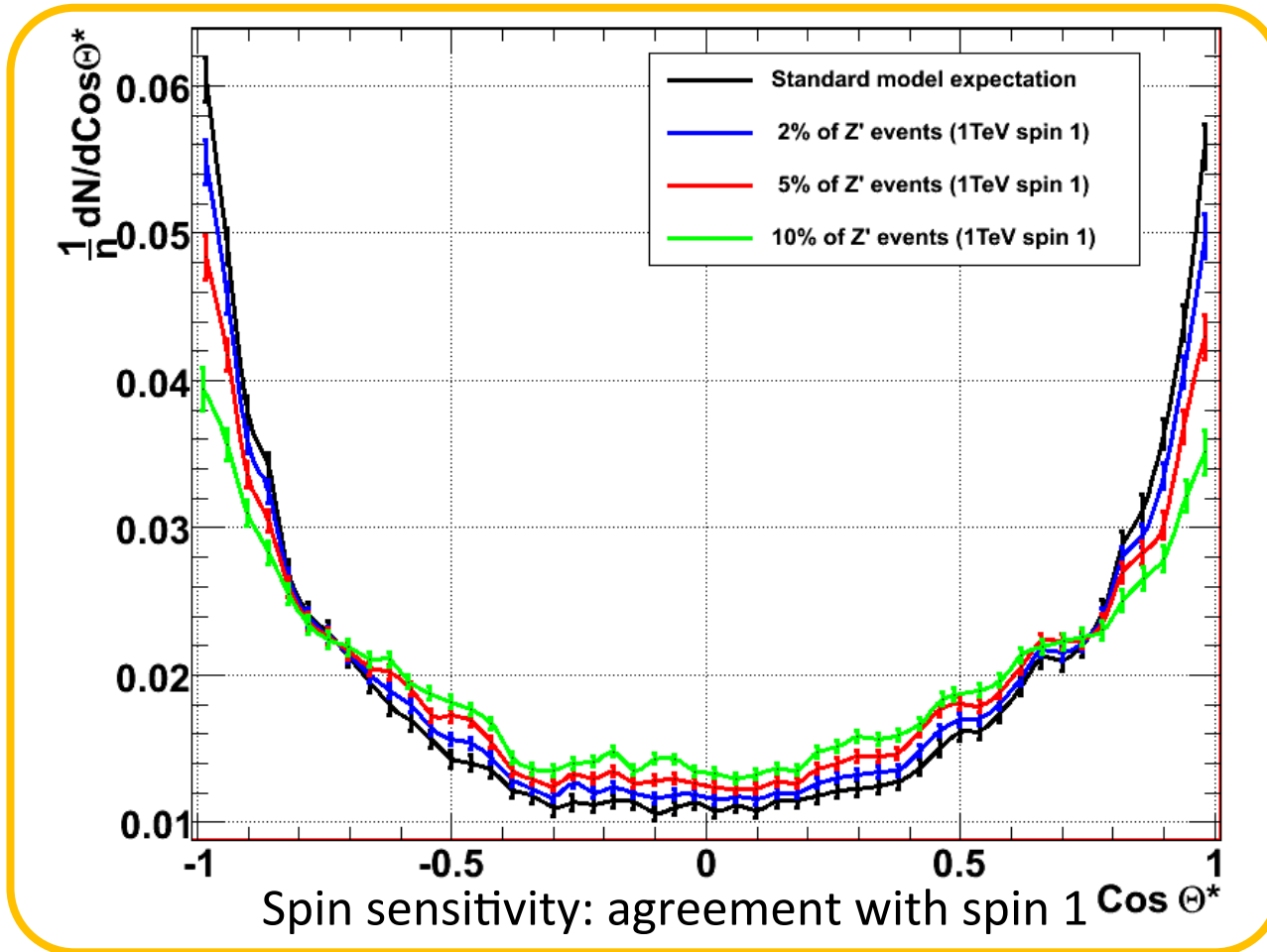


3 : Rikkert Frederix and Fabio Maltoni , « Top pair invariant mass distribution: a window on new physics » , JHEP01(2009)047



Prospect at LHC :  $(pp)\sqrt{s} = 14$  TeV

$\text{Cos}(\theta_{t\bar{t}}^*)$  reconstructed for events with  $M_{t\bar{t}}$  reconstructed above 700 GeV.



Referring to « Top pair invariant mass distribution: a window on new physics », JHEP01(2009)047

# Statistical uncertainties

- **Each event contributes to a few bins.** Errors on each bin (  $k$  ) are correlated.
- Correlation matrices have been computed :
  - using 100.000 standard model events.

- following :  $COR(k, l) = \frac{Cov(k, l)}{\sigma(k)\sigma(l)}$  with  $cov(k, l) = \frac{1}{N} \sum_{events} (k_i - \bar{k})(l_i - \bar{l})$

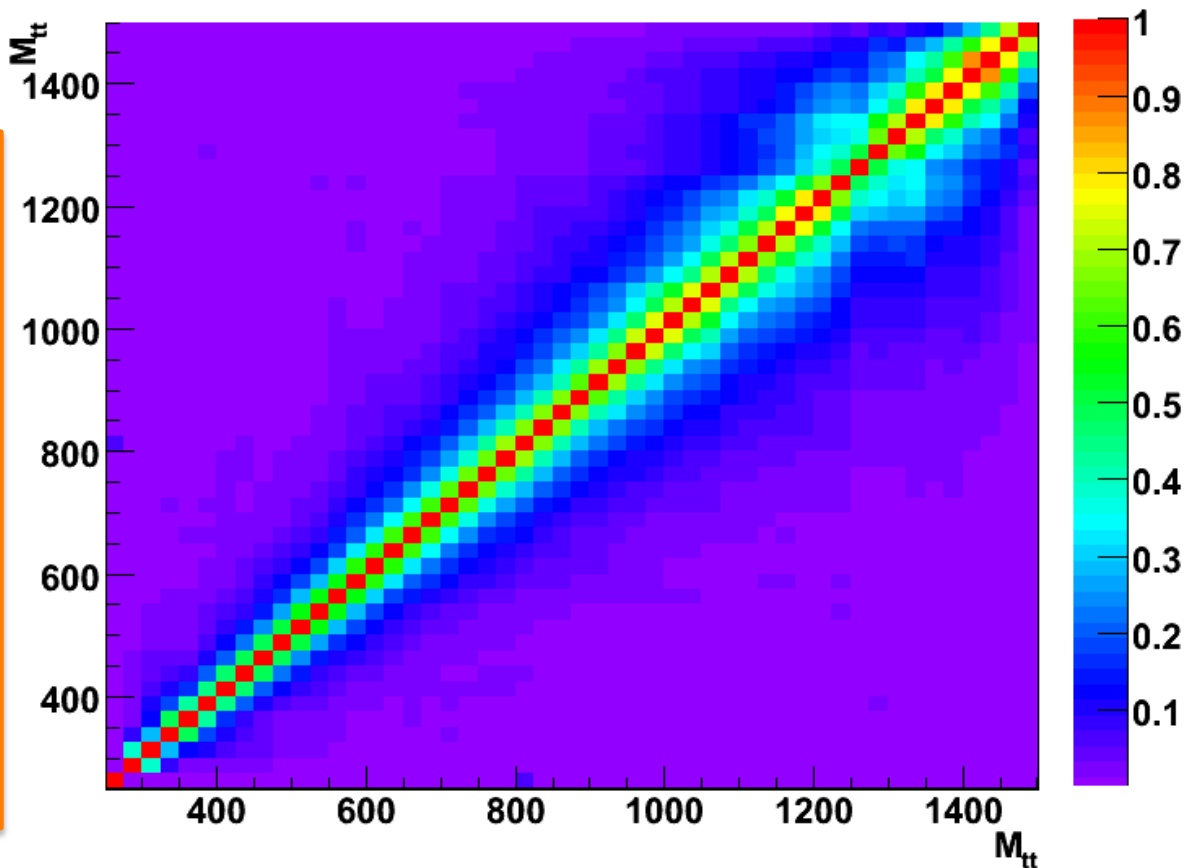
## S.M. deviation

$\chi^2$  is defined between the standard model expectation and the observed result.

$$\chi^2 = \sum_i \frac{(x_i - x_i^{th})^2}{\sigma_i^2}$$

Taking into account the correlation :

$$\chi^2 = \sum_{ij} C_{ij}^{-1} (x_i - x_i^{th})(x_j - x_j^{th})$$



## Summary

The **Matrix Element Method**:

- is not only for precise measurement.
- Is adapted to perform differential analysis:  $\frac{d\sigma}{dm}$  .
  - It is an inclusive search approach.

This technique allows the observation of resonances decaying in  $t\bar{t}$ :

- Visible in the invariant mass spectrum.
- Sensitivity to the spin of the resonance.