

Physics of Massive Neutrinos

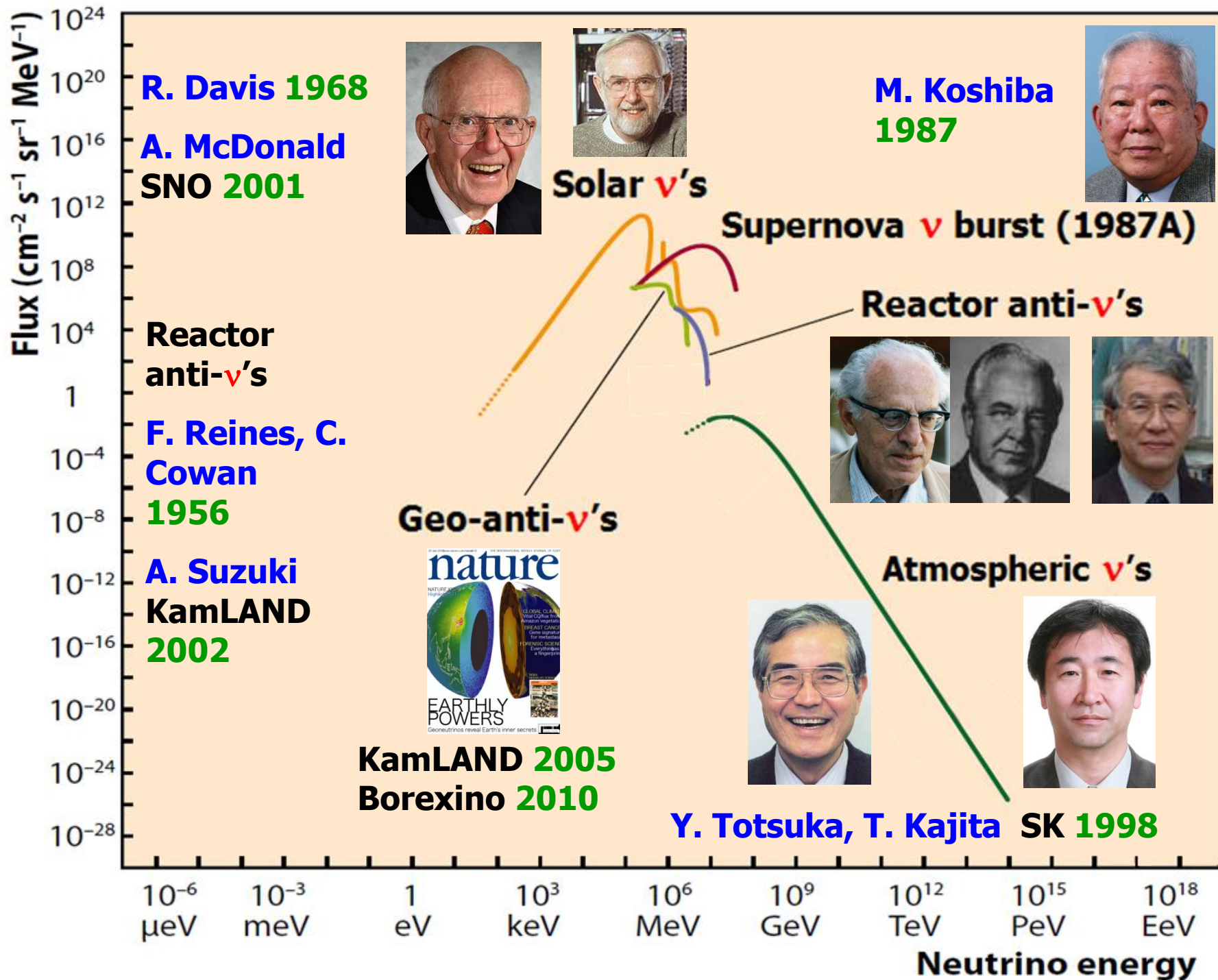
Zhi-zhong Xing
(IHEP, Beijing)

- A:** Neutrino history and lepton family
- B:** Neutrino masses and flavor mixing
- C:** Description of neutrino oscillations
- D:** Implication of neutrino oscillations
- E:** θ_{13} hint and sterile neutrino puzzle
- F:** On TeV neutrino physics at the LHC
- G:** Extreme corners in the neutrino sky
- H:** Cosmic baryon number asymmetry

@Lectures at CP3, UCL, Louvain-la-Neuve, Belgium, Jan 2012

Lecture G

- ★ **Two Extremes in the Neutrino Sky**
- ★ **UHE Cosmic Neutrino Telescopes**
- ★ **ULE Cosmic Neutrino Background**



Lesson: ν Oscillations + MSW

arXiv:1103.0734

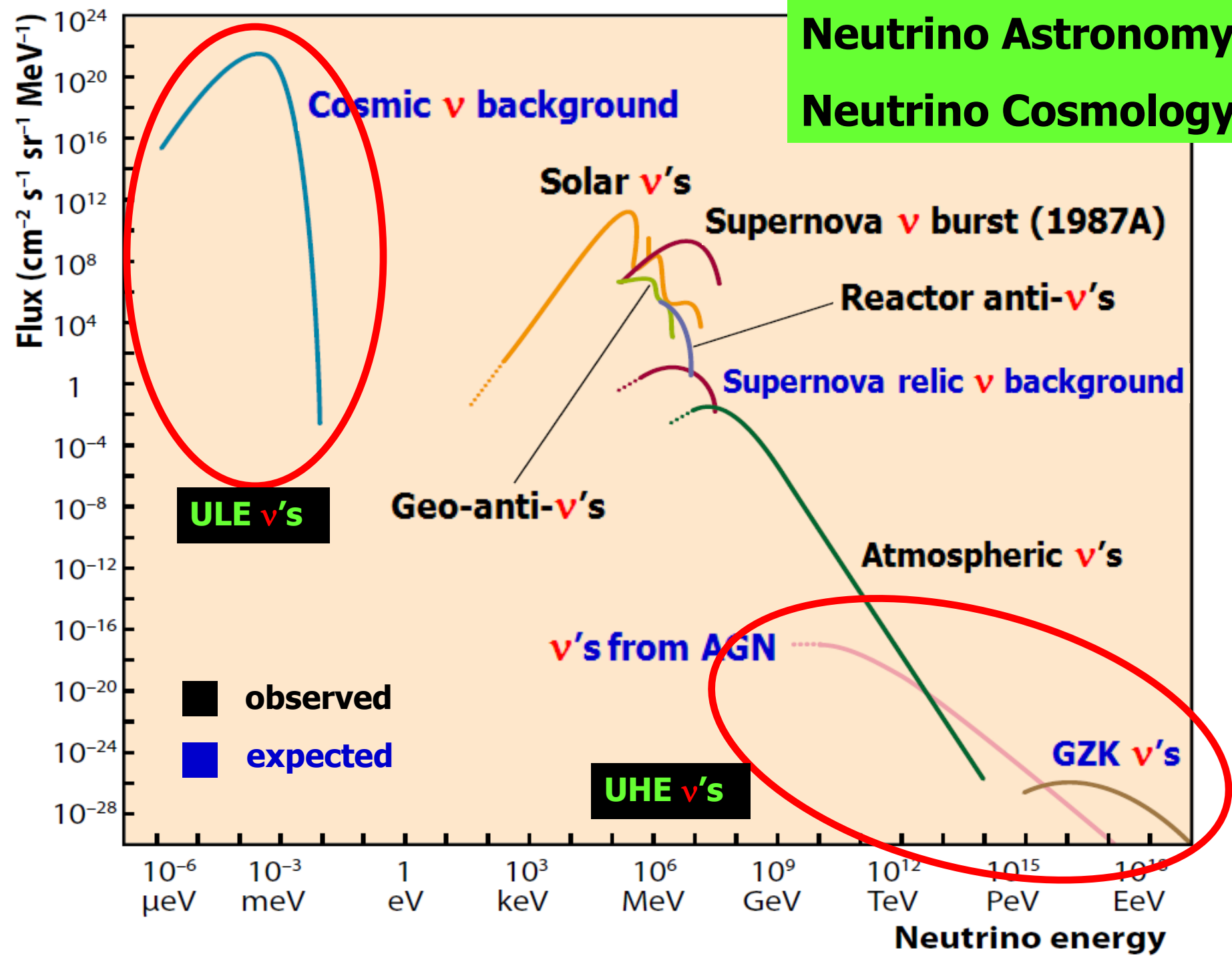
T. Schwetz, et al.

Current Data

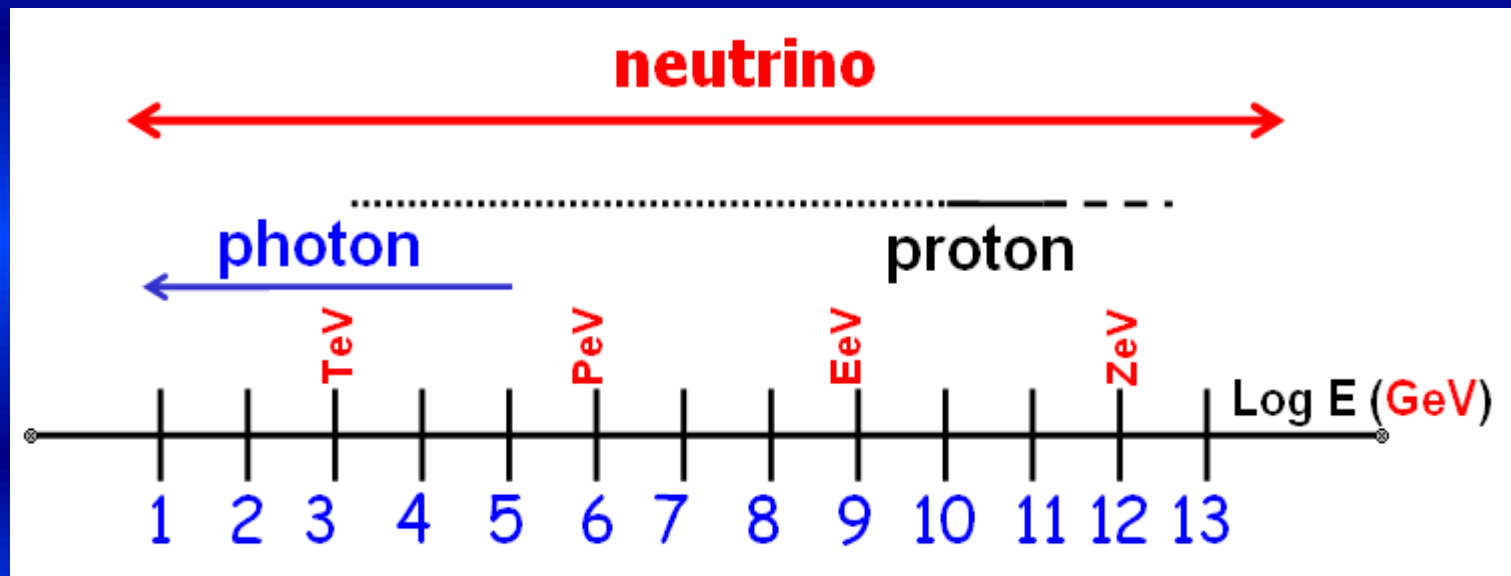
parameter	best fit $\pm 1\sigma$		3σ
$\Delta m_{21}^2 [10^{-5} \text{eV}^2]$	$7.59^{+0.20}_{-0.18}$	7.2	7.09–8.19
$\Delta m_{31}^2 [10^{-3} \text{eV}^2]$	2.45 ± 0.09 $-(2.34^{+0.10}_{-0.09})$	$2.28 - 2.64$ $-(2.17 - 2.54)$	$2.18 - 2.73$ $-(2.08 - 2.64)$
$\sin^2 \theta_{12}$	$0.312^{+0.017}_{-0.015}$	0.28–0.35	0.27–0.36
$\sin^2 \theta_{23}$	0.51 ± 0.06 0.52 ± 0.06	0.41–0.61 0.4	0.29–0.64
$\sin^2 \theta_{13}$	$0.010^{+0.009}_{-0.006}$ $0.013^{+0.009}_{-0.007}$	$\leq$ $\leq$	Much larger theta(13) T2K/MINOS/Double Chooz ~ 8 degrees (3.5σ ?)

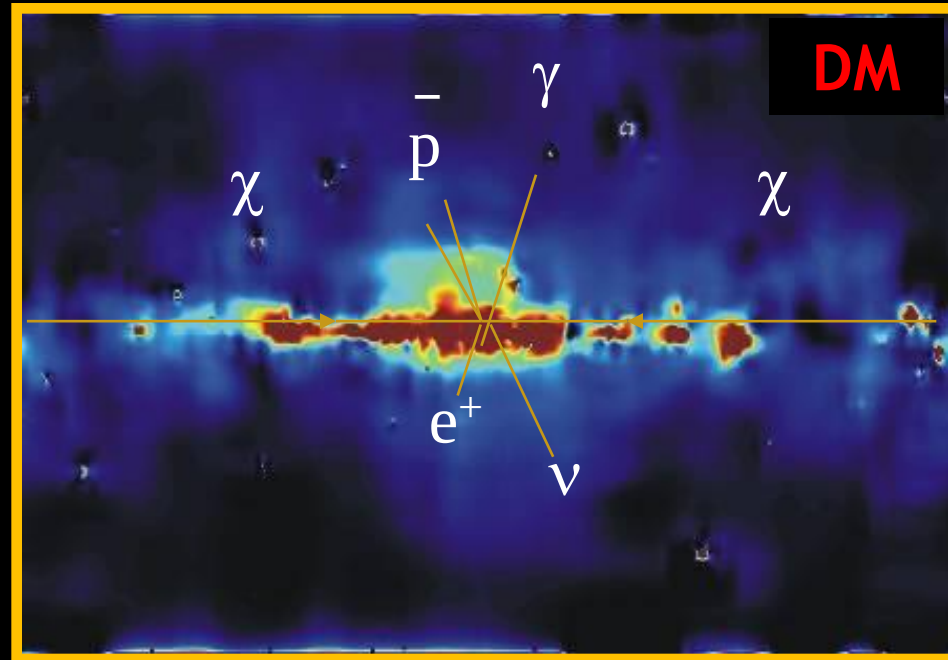
Neutrino Astronomy

Neutrino Cosmology

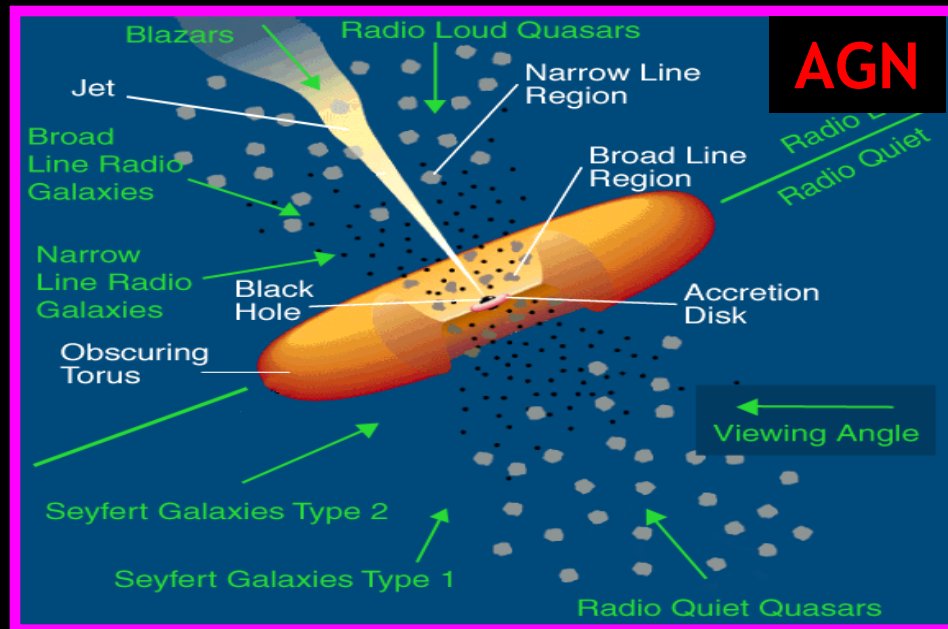


The diagram illustrates a proposed neutrino telescope concept. On the left, a 'Cosmic accelerator' (represented by a bright orange and yellow jet) emits three types of particles: 'Light absorbed by CMB' (green text), 'Neutrinos' (red text) with a ratio of $1\nu_e : 2\nu_\mu : 0\nu_\tau$, and a 'Proton scattered by the magnetic field' (cyan text). These particles travel towards a central 'CMB' (Cosmic Microwave Background) region, depicted as a large, textured blue and red oval. From this region, three paths lead to a 'ν telescope' (represented by a globe of Earth) on the right: a straight line for neutrinos with a ratio of $1\nu_e : 1\nu_\mu : 1\nu_\tau$, and two wavy lines for light and protons.





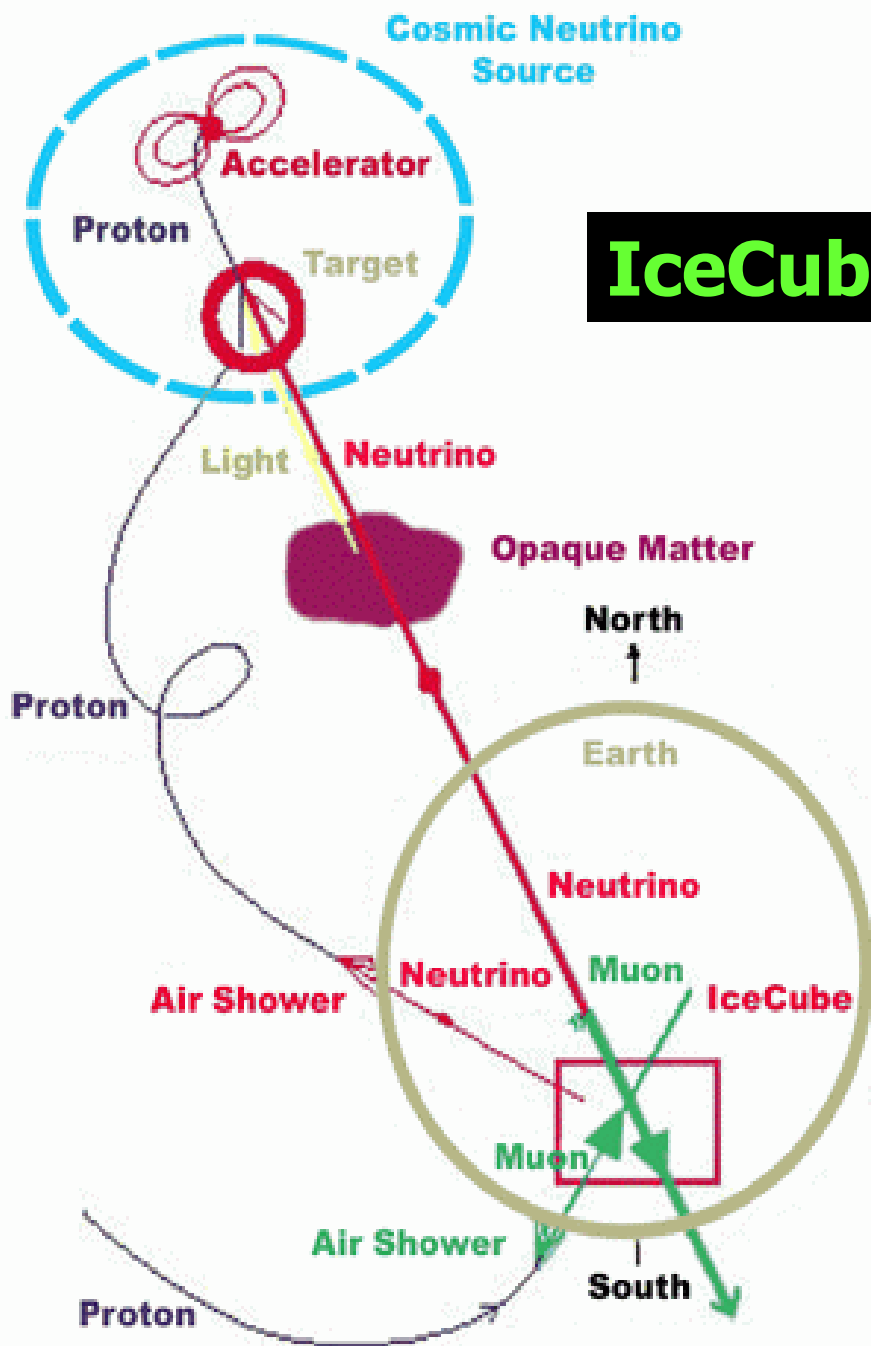
Possible astrophysical sources of UHE cosmic neutrinos ...



Optical Cherenkov NTs

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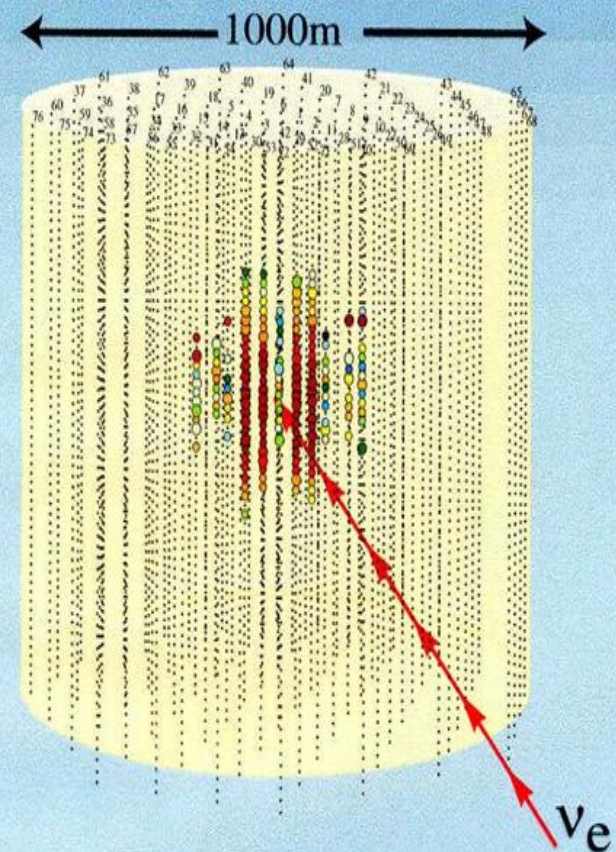




IceCube is working



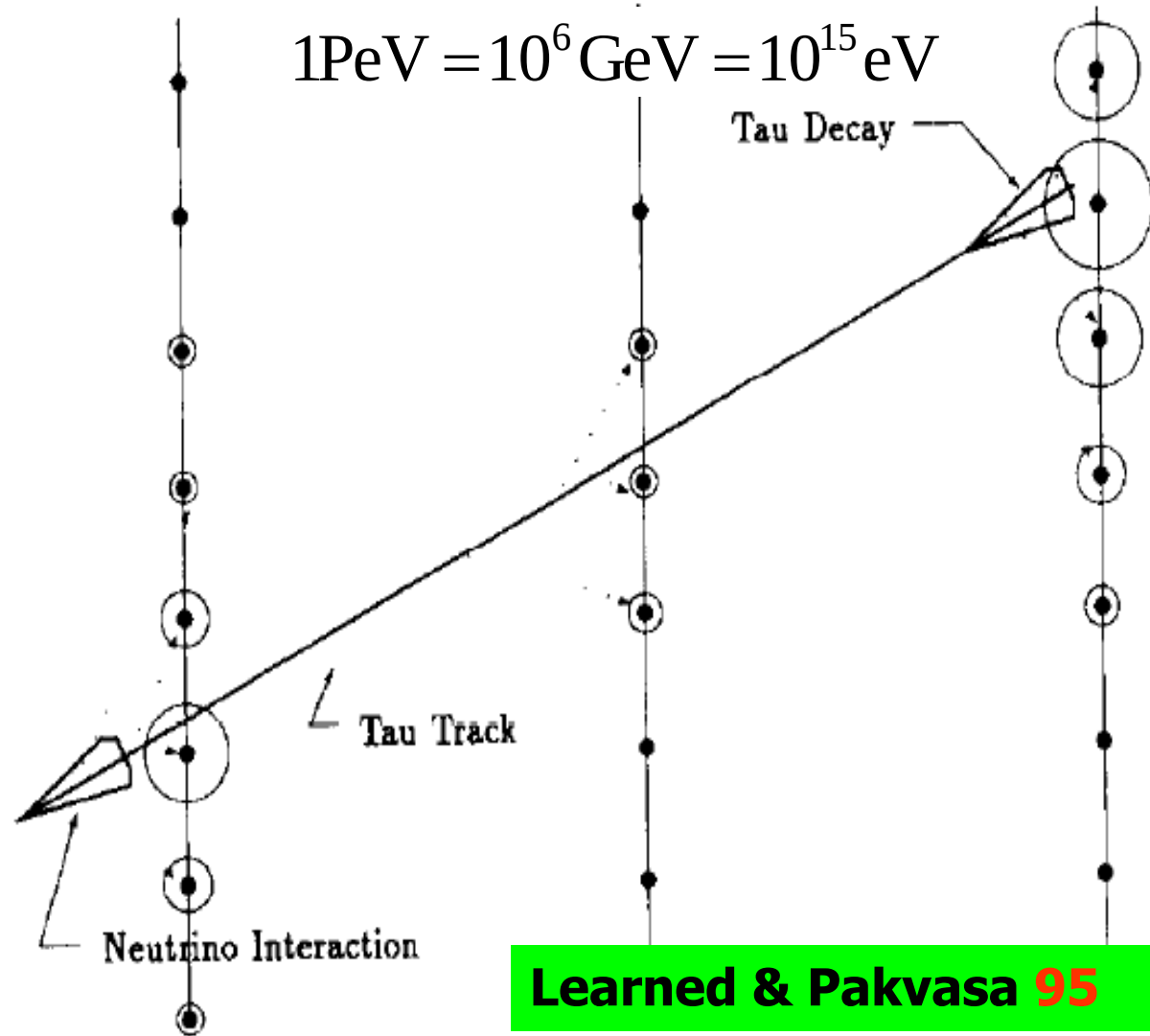
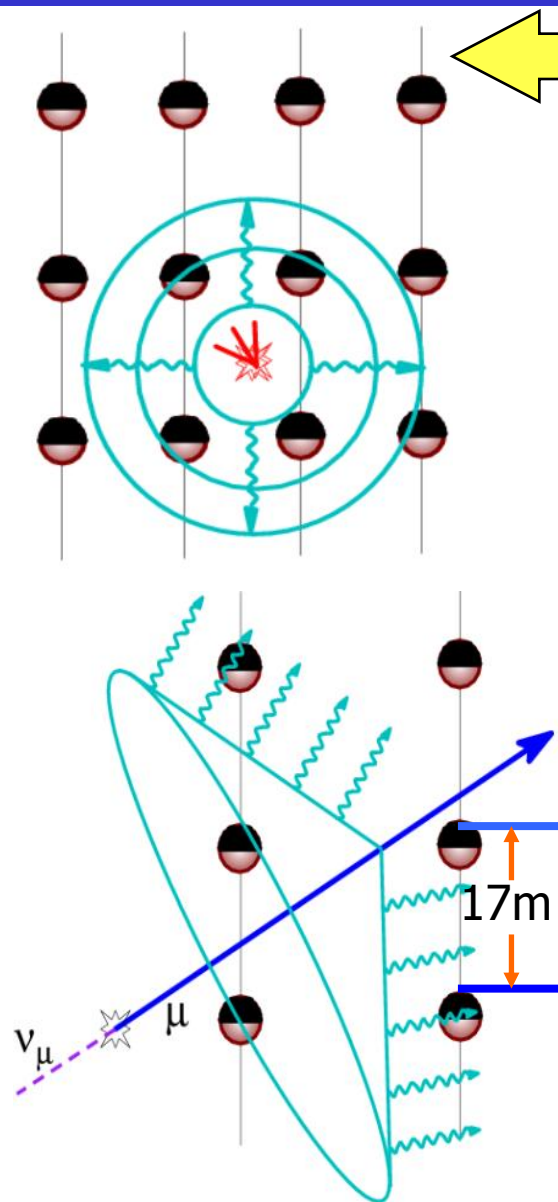
IceCube



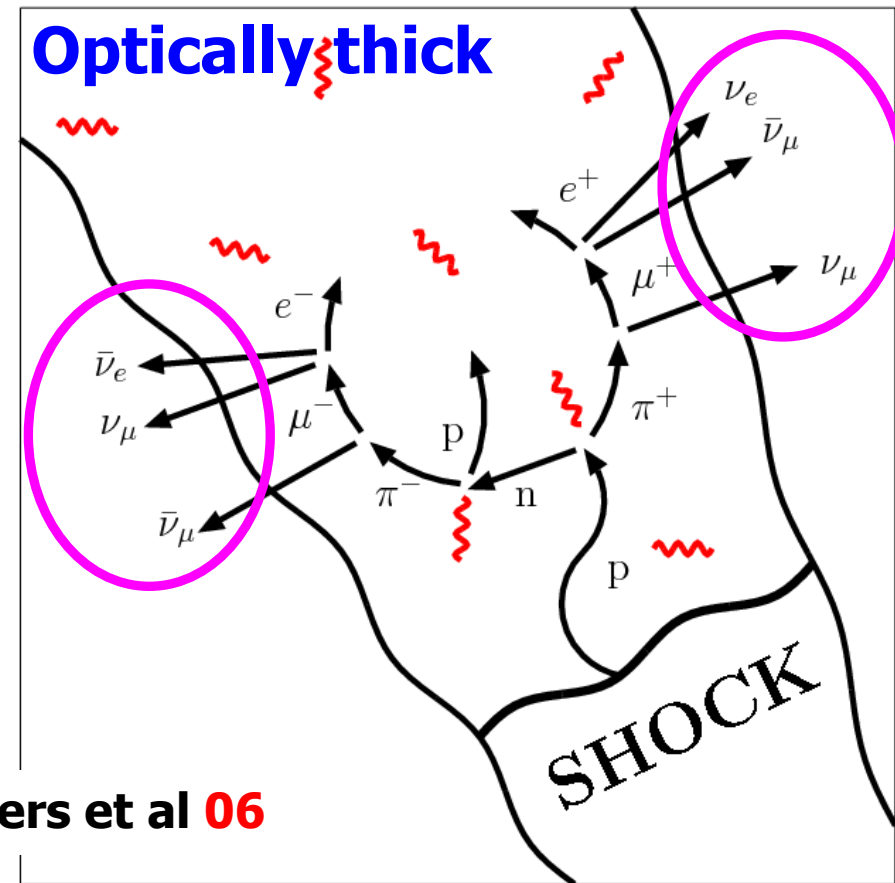
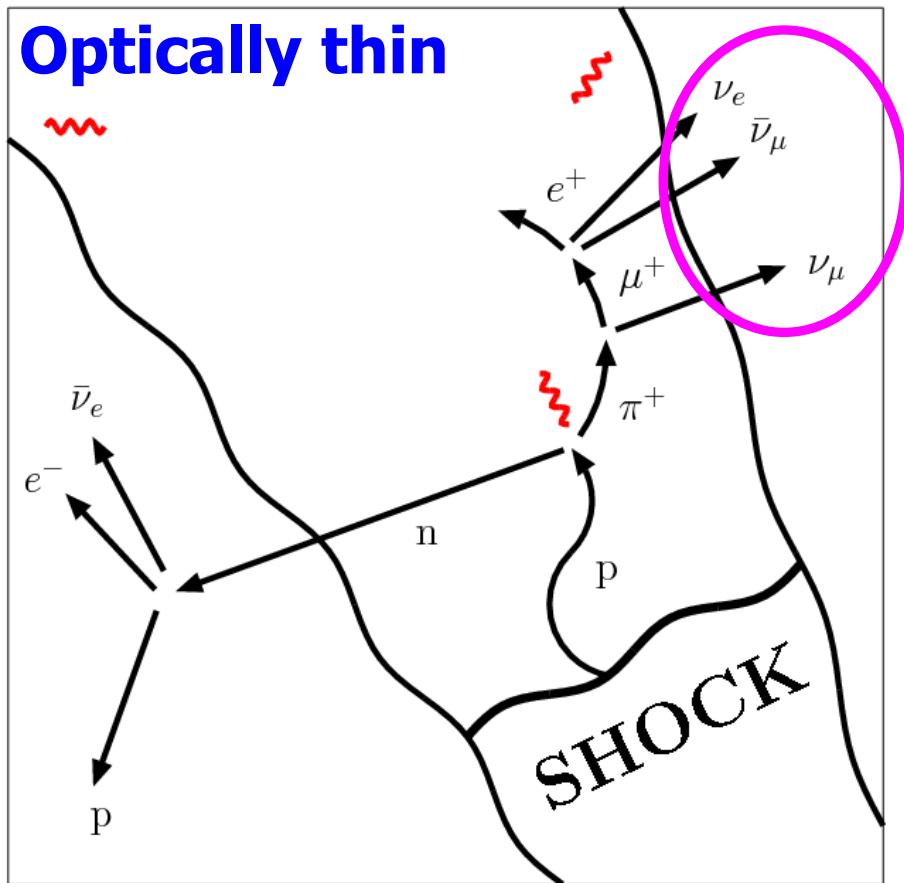
Flavor Identification

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Halzen, astro-ph/0602132



Learned & Pakvasa 95



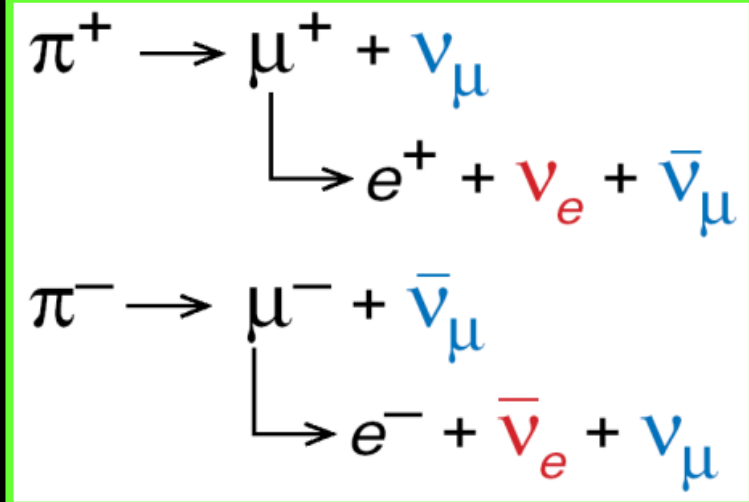
Ahlers et al 06

Conventional mechanism:

$$p + \gamma \rightarrow \Delta^+ \rightarrow \pi^+ + n$$

$$p + p \rightarrow \pi^\pm + X$$

$$\Phi_e^S : \Phi_\mu^S : \Phi_\tau^S = 1 : 2 : 0$$



Oscillations

The transition probability:

$$\alpha, \beta = e, \mu, \tau$$

$$j, k = 1, 2, 3$$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{j=1}^3 |V_{\alpha j}|^2 |V_{\beta j}|^2 + 2\text{Re} \sum_{j < k} V_{\alpha j} V_{\beta k} V_{\alpha k}^* V_{\beta j}^* \exp \left\{ -i \frac{\Delta m_{kj}^2 L}{2E} \right\}$$

Expected sources (AGN) at a typical distance: ~ 100 Mpc.

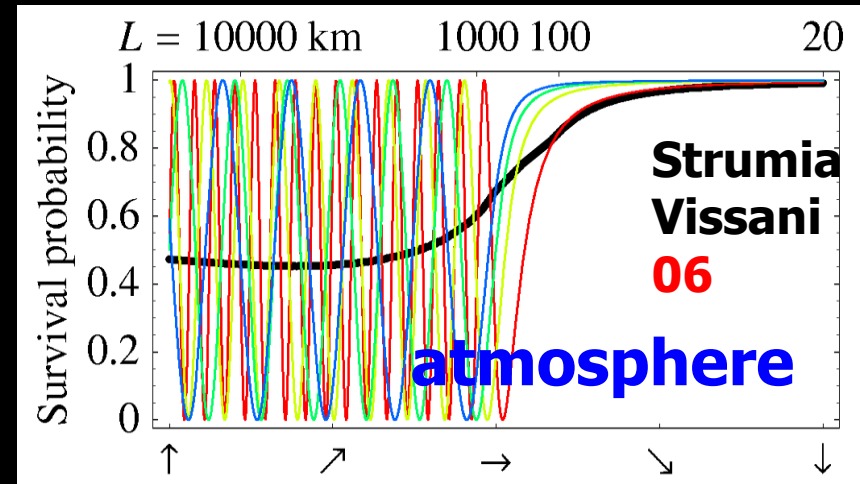
For $|\Delta m^2| \sim 10^{-4} \text{ eV}^2$, the oscillation length in vacuum:

$$L_{\text{OSC}} \equiv \frac{4\pi E_\nu}{|\Delta m^2|} \sim 8 \times 10^{-25} \text{ Mpc} \left(\frac{E_\nu}{1 \text{ eV}} \right)$$

$$1 \text{ Mpc} \approx 3.1 \times 10^{22} \text{ m}$$

After many oscillations, the averaged probability of UHE cosmic neutrinos is

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{j=1}^3 |V_{\alpha j}|^2 |V_{\beta j}|^2$$



Flavor Democracy

At an astrophysical source:

$$\Phi_e^S : \Phi_\mu^S : \Phi_\tau^S = 1 : 2 : 0$$

At a ν -telescope:

$$\Phi_\beta^T = \sum_\alpha \Phi_\alpha^S P(\nu_\alpha \rightarrow \nu_\beta) = \sum_\alpha \sum_{i=1}^3 \Phi_\alpha^S |V_{\alpha i}|^2 |V_{\beta i}|^2$$

If there is a μ - τ symmetry for V :

$$|V_{\mu i}| = |V_{\tau i}|$$

$$(i = 1, 2, 3)$$

Then the unitarity of V leads to:

$$\Phi_e^T : \Phi_\mu^T : \Phi_\tau^T = 1 : 1 : 1$$

In the PDG parametrization (Xing, Zhou, 08):

$$V = \begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & +c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & c_{13}s_{23} \\ +s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

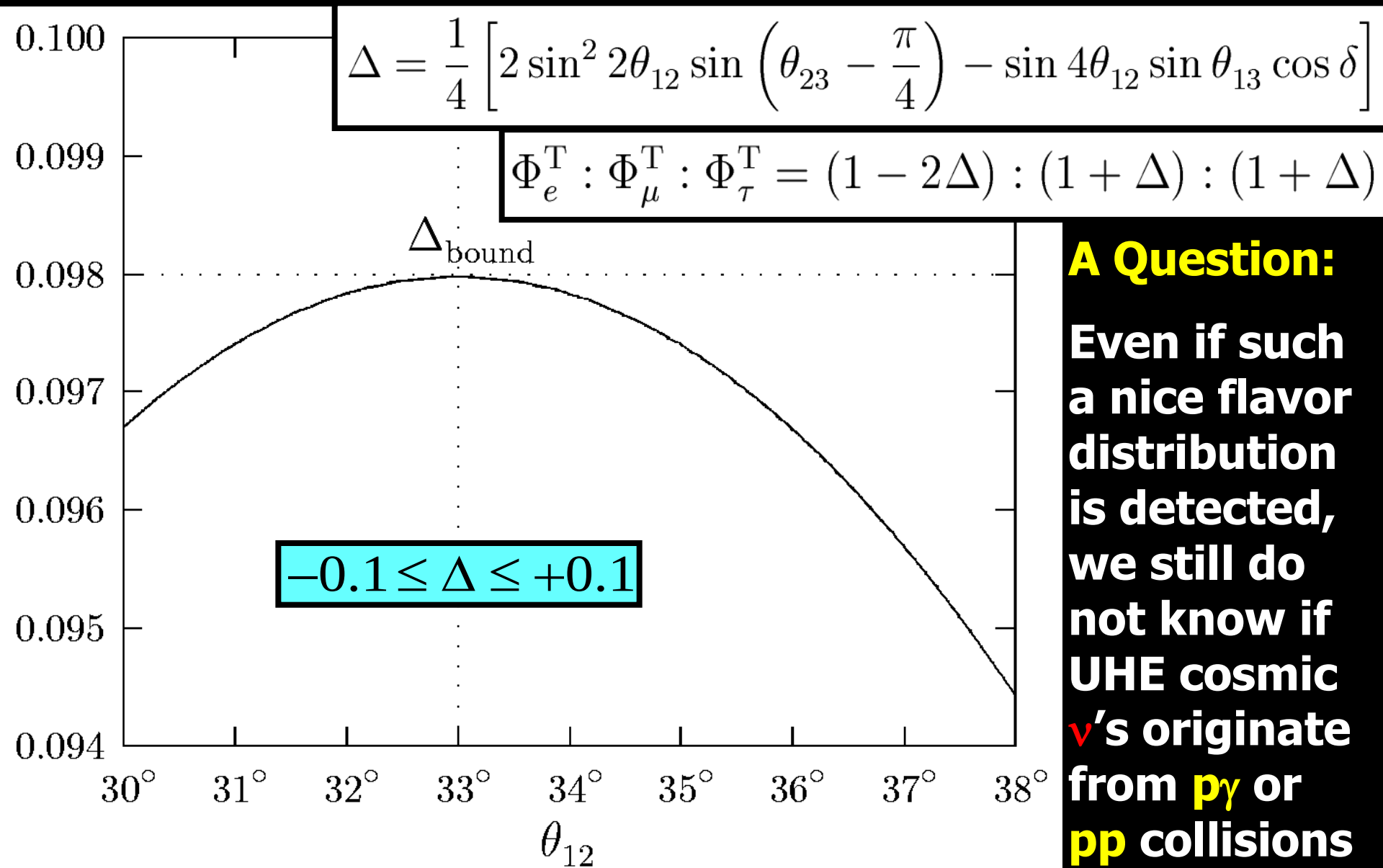
$$\begin{array}{l} \text{CPC:} \left\{ \begin{array}{l} \theta_{13} = 0 \\ \theta_{23} = \pi/4 \end{array} \right. \\ \text{or} \\ \text{CPV:} \left\{ \begin{array}{l} \delta = \pm\pi/2 \\ \theta_{23} = \pi/4 \end{array} \right. \end{array}$$

Near flavor democracy (Learned, Pakvasa, 95)

**μ - τ symmetry breaking
(Xing, 06)**

$$\Phi_e^T : \Phi_\mu^T : \Phi_\tau^T = (1 - 2\Delta) : (1 + \Delta) : (1 + \Delta)$$

μ - τ Symmetry Breaking



A Question:

Even if such a nice flavor distribution is detected, we still do not know if UHE cosmic ν 's originate from $p\gamma$ or pp collisions

The Glashow Resonance

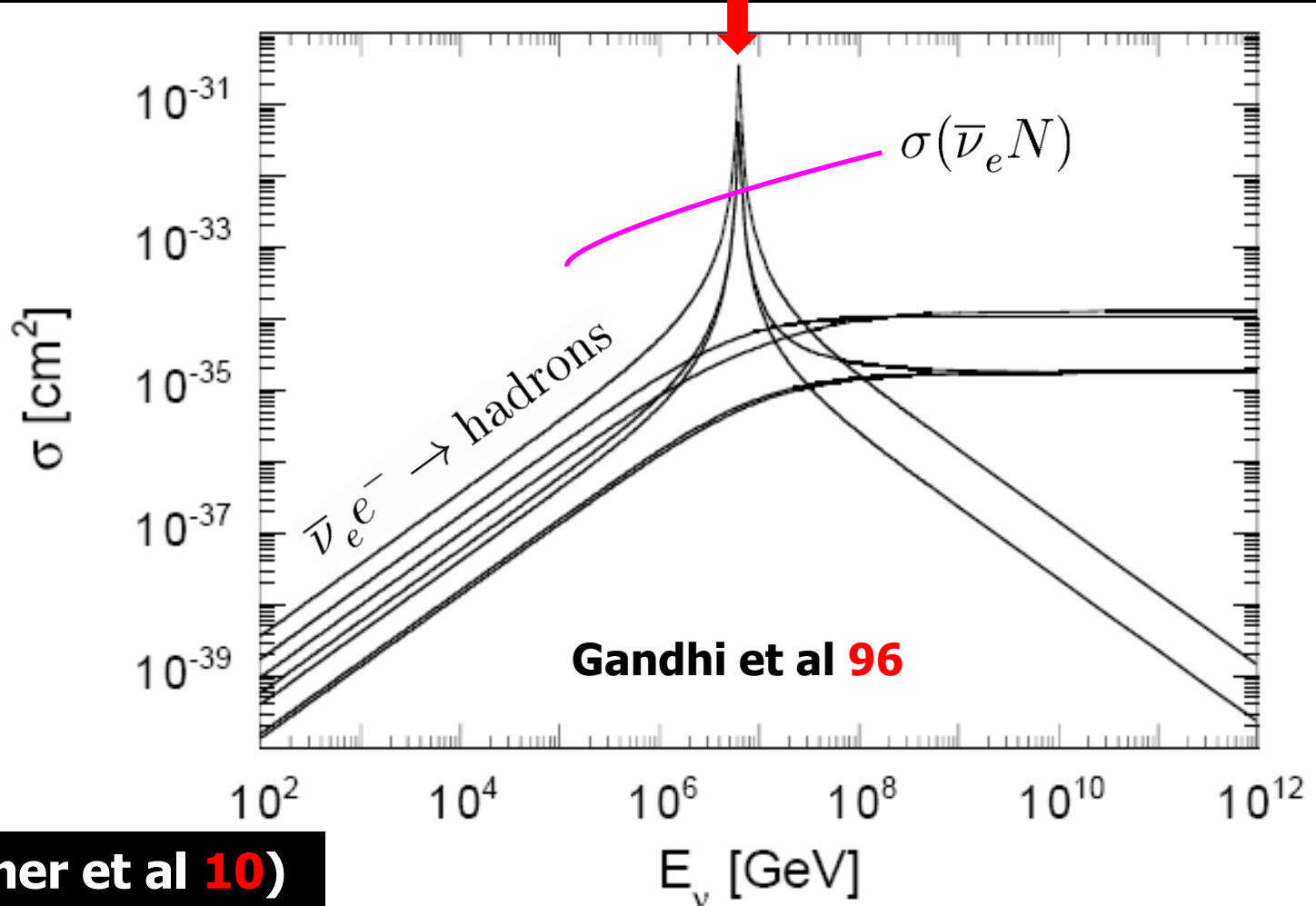
$$\bar{\nu}_e + e^- \rightarrow W^- \rightarrow \text{anything}$$

Unique for electron anti- ν 's!



(Glashow 60)

$$E_{\bar{\nu}_e} \simeq M_W^2 / (2m_e) \simeq 6.3 \text{ PeV}$$



An interesting **discriminator** between **$p\gamma$** & **pp** collisions at an optically thin source of cosmic rays. (Anchordoqui et al 05, Hummer et al 10)

A Parametrization

Assume a cosmic accelerator with both **p γ** & **pp** collisions.

★ Pure **p γ** collisions: $\kappa = 1$

★ Pure **pp** collisions: $\kappa = 0$

$$\delta_{p\gamma} \equiv \frac{\Phi_{\pi^-}^{p\gamma}}{\Phi_{\pi^+}^{p\gamma}} \quad \delta_{pp} \equiv \frac{\Phi_{\pi^-}^{pp}}{\Phi_{\pi^+}^{pp}} - 1$$

$$\kappa \equiv \frac{\Phi_{\pi^+}^{p\gamma} + \Phi_{\pi^-}^{p\gamma}}{\Phi_{\pi^+}^{pp} + \Phi_{\pi^-}^{pp} + \Phi_{\pi^+}^{p\gamma} + \Phi_{\pi^-}^{p\gamma}}$$

They describe departures from the conventional cases (Xing, Zhou, **11**)

At the source: (note that $\Phi_e^S : \Phi_\mu^S : \Phi_\tau^S = 1 : 2 : 0$ doesn't change)

$$\begin{aligned} & \left\{ \Phi_{\nu_e}^S : \Phi_{\bar{\nu}_e}^S : \Phi_{\nu_\mu}^S : \Phi_{\bar{\nu}_\mu}^S : \Phi_{\nu_\tau}^S : \Phi_{\bar{\nu}_\tau}^S \right\} \\ &= (\Phi_{\pi^+}^{p\gamma} + \Phi_{\pi^+}^{pp}) \left\{ \frac{1}{3} : 0 : \frac{1}{3} : \frac{1}{3} : 0 : 0 \right\} + (\Phi_{\pi^-}^{p\gamma} + \Phi_{\pi^-}^{pp}) \left\{ 0 : \frac{1}{3} : \frac{1}{3} : \frac{1}{3} : 0 : 0 \right\} \\ &= \left\{ \frac{1}{3} \left[\frac{1}{2 + \delta_{pp}} + \frac{1 + \delta_{pp} - \delta_{p\gamma}}{(2 + \delta_{pp})(1 + \delta_{p\gamma})} \kappa \right] : \frac{1}{3} \left[\frac{1 + \delta_{pp}}{2 + \delta_{pp}} - \frac{1 + \delta_{pp} - \delta_{p\gamma}}{(2 + \delta_{pp})(1 + \delta_{p\gamma})} \kappa \right] : \frac{1}{3} : \frac{1}{3} : 0 : 0 \right\} \end{aligned}$$

At the ν -telescope: (the **Glashow resonance** working observable)

$$R_0 \equiv \frac{\Phi_{\bar{\nu}_e}^T}{\Phi_{\nu_\mu}^T + \Phi_{\bar{\nu}_\mu}^T} = \left[\frac{1 + \delta_{pp}}{2 + \delta_{pp}} - \frac{1 + \delta_{pp} - \delta_{p\gamma}}{(2 + \delta_{pp})(1 + \delta_{p\gamma})} \kappa \right] \frac{P_{ee}}{P_{e\mu} + 2P_{\mu\mu}} + \frac{P_{e\mu}}{P_{e\mu} + 2P_{\mu\mu}}$$

Numerical Illustration

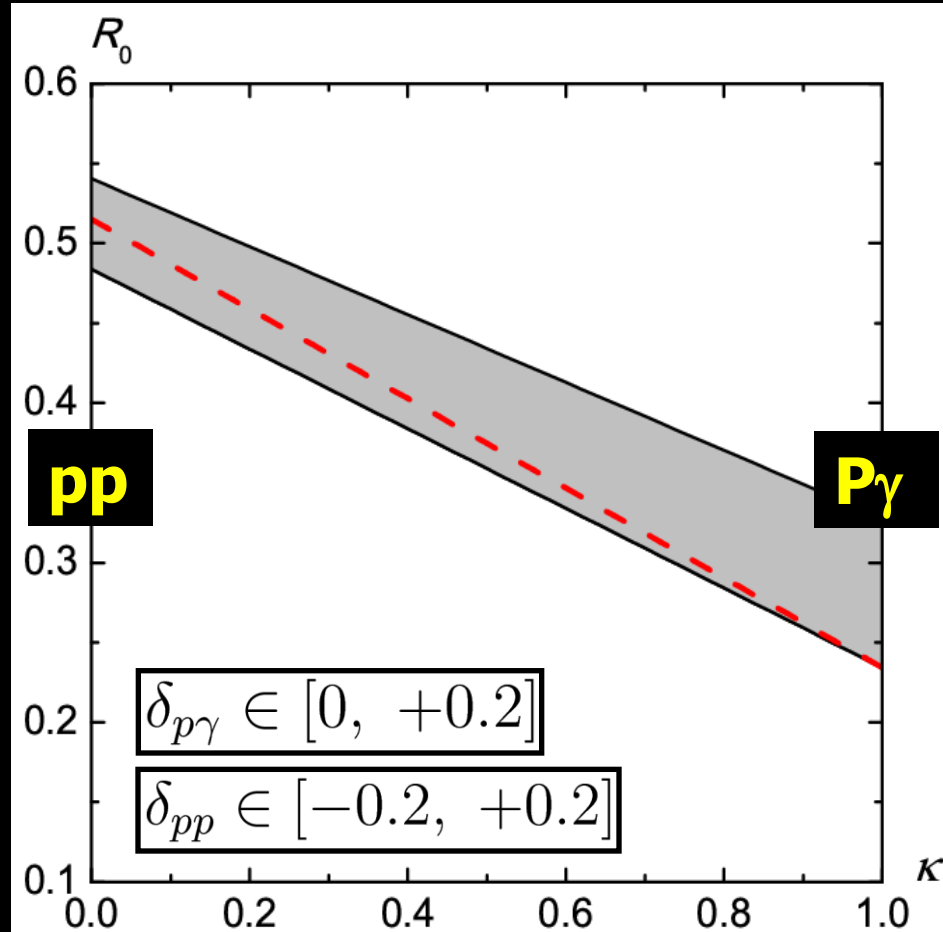
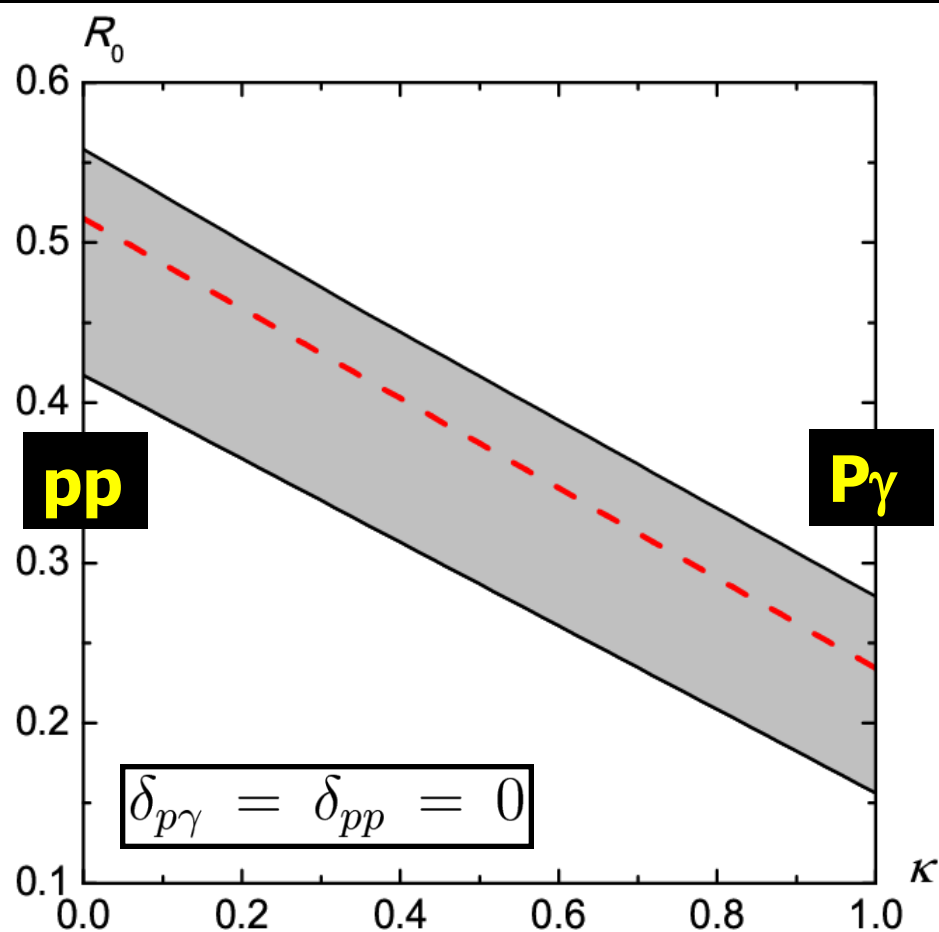
Input the **best-fit** values + **1σ error** bars of **3** neutrino mixing angles (Schwetz et al **11**)

---- : **best-fit** + $\delta = 0$ + $\delta_{p\gamma} = \delta_{pp} = 0$

$$\sin^2 \theta_{12} = 0.312^{+0.017}_{-0.015}$$

$$\sin^2 \theta_{23} = 0.51 \pm 0.06$$

$$\sin^2 \theta_{13} = 0.010^{+0.009}_{-0.006}$$



IceCube

WB $E_\nu^2 \Phi_{\nu+\bar{\nu}} = 2 \times 10^{-8} \epsilon_\pi \xi_z \text{ GeV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$

$\Phi_0 \equiv 6 \times 10^{-8} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} (1 \text{ GeV}/E_\nu)^2$

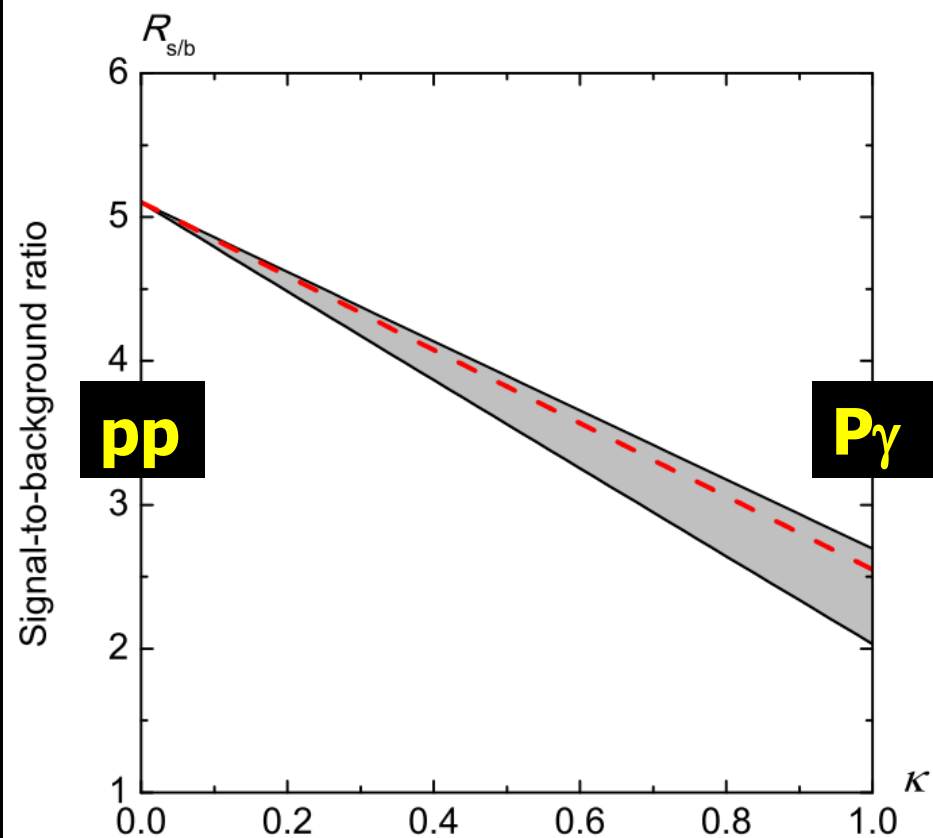
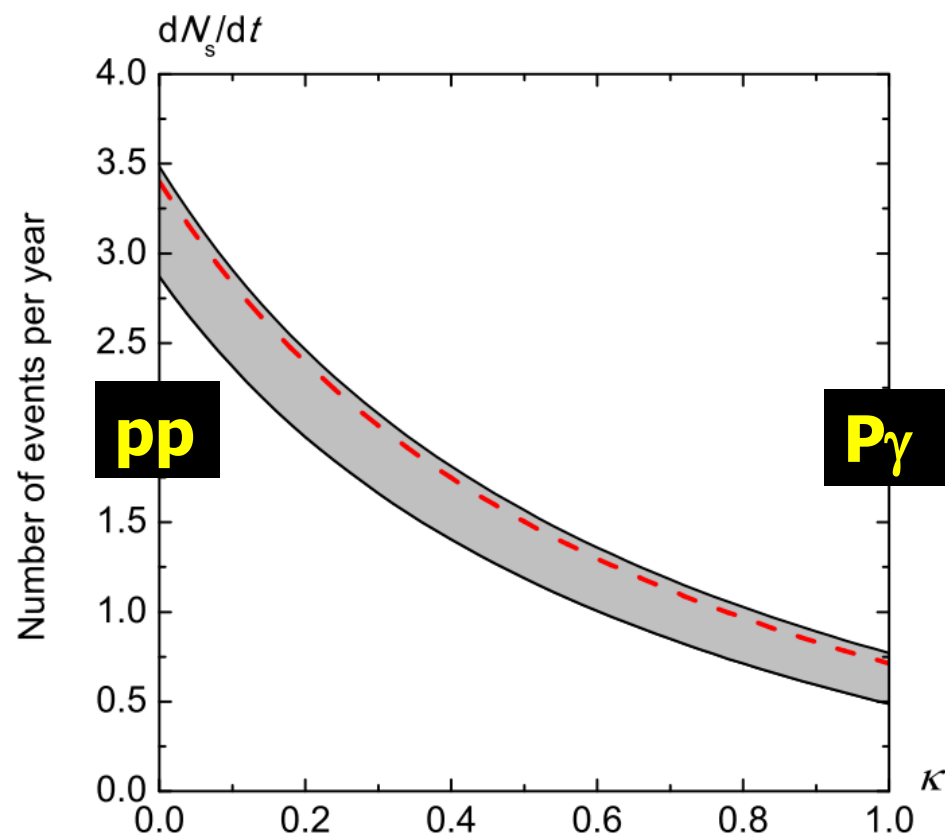
$$\Phi_{\nu_\alpha}^T = \Phi_0 \frac{\epsilon_\pi^{pp} \epsilon_\pi^{p\gamma}}{(1-\kappa) \epsilon_\pi^{p\gamma} + \kappa \epsilon_\pi^{pp}} \times \left\{ \frac{1}{3} \left[\frac{1}{2+\delta_{pp}} + \frac{1+\delta_{pp}-\delta_{p\gamma}}{(2+\delta_{pp})(1+\delta_{p\gamma})} \kappa \right] P_{e\alpha} + \frac{1}{3} P_{\mu\alpha} \right\}$$

$$\Phi_{\bar{\nu}_\alpha}^T = \Phi_0 \frac{\epsilon_\pi^{pp} \epsilon_\pi^{p\gamma}}{(1-\kappa) \epsilon_\pi^{p\gamma} + \kappa \epsilon_\pi^{pp}} \times \left\{ \frac{1}{3} \left[\frac{1+\delta_{pp}}{2+\delta_{pp}} - \frac{1+\delta_{pp}-\delta_{p\gamma}}{(2+\delta_{pp})(1+\delta_{p\gamma})} \kappa \right] P_{e\alpha} + \frac{1}{3} P_{\mu\alpha} \right\}$$

$\epsilon_\pi^{p\gamma} \approx 0.25$

$\epsilon_\pi^{pp} \approx 0.6$

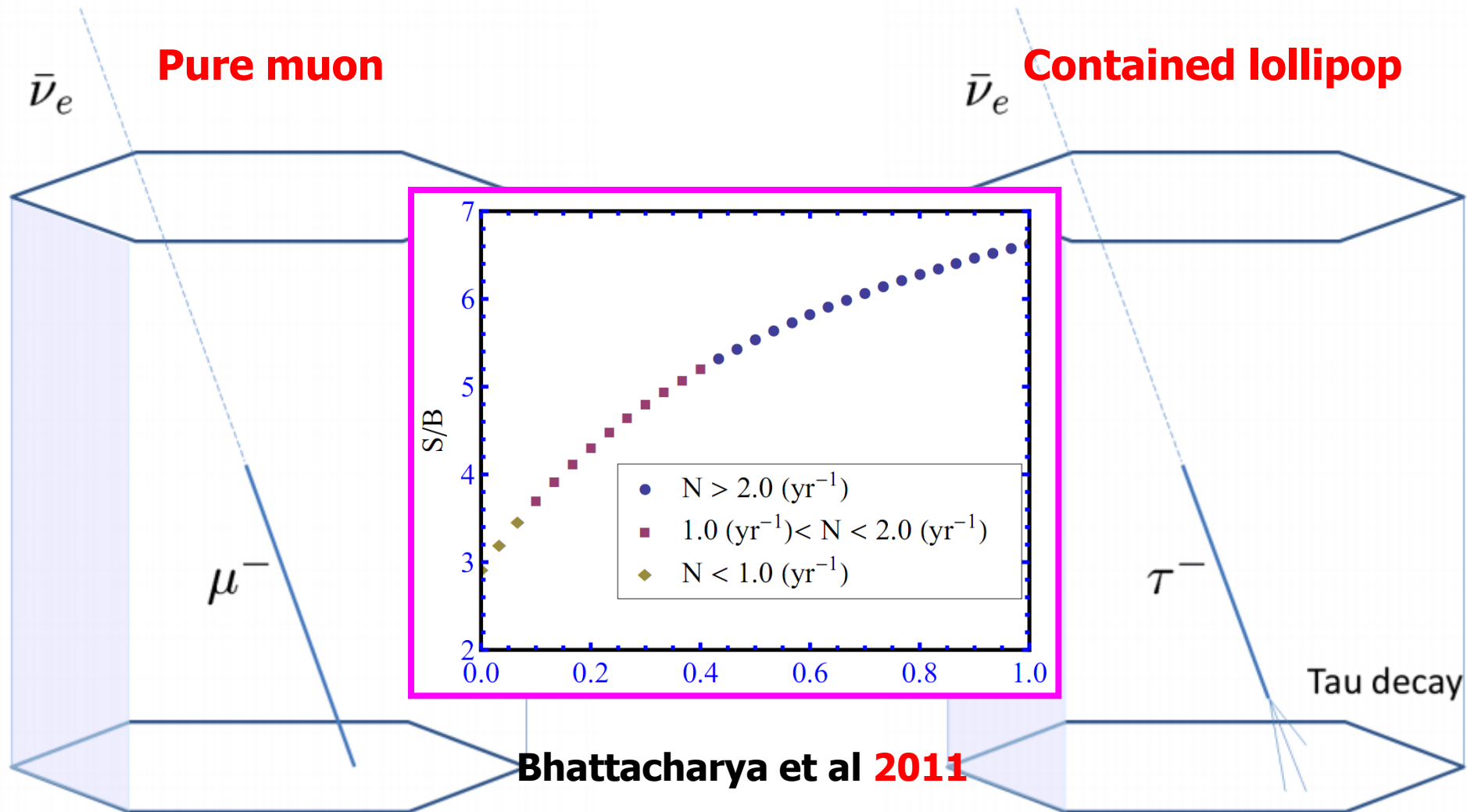
$\delta_{p\gamma} = \delta_{pp} = 0$



$\mu + \tau$ modes

Interaction	σ [cm ²]
$\bar{\nu}_e e \rightarrow \bar{\nu}_e e$	5.38×10^{-32}
$\bar{\nu}_e e \rightarrow \bar{\nu}_\mu \mu$	5.38×10^{-32}
$\bar{\nu}_e e \rightarrow \bar{\nu}_\tau \tau$	5.38×10^{-32}
$\bar{\nu}_e e \rightarrow \text{hadrons}$	3.41×10^{-31}
$\bar{\nu}_e e \rightarrow \text{anything}$	5.02×10^{-31}

Interaction	σ [cm ²]
$\nu_\mu N \rightarrow \mu + \text{anything}$	1.43×10^{-33}
$\nu_\mu N \rightarrow \nu_\mu + \text{anything}$	6.04×10^{-34}
$\nu_\mu e \rightarrow \nu_e \mu$	5.42×10^{-35}



Generic Flavor Distribution

Parametrization [Xing, Zhou 06]:

$$\{\phi_e, \phi_\mu, \phi_\tau\} = \{\sin^2 \xi \cos^2 \zeta, \cos^2 \xi \cos^2 \zeta, \sin^2 \zeta\} \phi_0$$

where ζ characterizes the small amount of tau ν 's at the source [e.g., from Ds- or B-meson decays (Learned, Pakvasa 95)].

Lipari et al 07; Pakvasa et al 08: 1 : 2 : 0 $\rightarrow$ 1 : 1.852 : 0.001

❑ **Conventional (or standard) source:**

$$\phi_e : \phi_\mu : \phi_\tau = 1 : 2 : 0$$



$$(\xi, \zeta) = (35.3^\circ, 0^\circ)$$

❑ **Postulated neutron source:**

$$\phi_e : \phi_\mu : \phi_\tau = 1 : 0 : 0$$



$$(\xi, \zeta) = (90^\circ, 0^\circ)$$

❑ **Possible muon-damped source:**

$$\phi_e : \phi_\mu : \phi_\tau = 0 : 1 : 0$$



$$(\xi, \zeta) = (0^\circ, 0^\circ)$$

Working Observables

We define the following observables:

$$\{R_e, R_\mu, R_\tau\} \equiv \left\{ \frac{\phi_e^T}{\phi_\mu^T + \phi_\tau^T}, \frac{\phi_\mu^T}{\phi_\tau^T + \phi_e^T}, \frac{\phi_\tau^T}{\phi_e^T + \phi_\mu^T} \right\}$$

Only two of them are independent, because

$$\hat{R}_e + \hat{R}_\mu + \hat{R}_\tau = 1$$

with

$$\hat{R}_\alpha \equiv \frac{R_\alpha}{1 + R_\alpha}$$

Another observable is the total neutrino flux of all flavors:

$$\phi_0 = \phi_e + \phi_\mu + \phi_\tau = \phi_e^T + \phi_\mu^T + \phi_\tau^T$$

Question: can all of the three observables be well measured?

Point: by using any two observables, we may determine the initial flavor composition of UHE neutrino fluxes (i.e., ξ and ζ)

Formula

Definition:

$$\{R_e, R_\mu, R_\tau\} \equiv \left\{ \frac{\phi_e^T}{\phi_\mu^T + \phi_\tau^T}, \frac{\phi_\mu^T}{\phi_\tau^T + \phi_e^T}, \frac{\phi_\tau^T}{\phi_e^T + \phi_\mu^T} \right\}$$

Parametrization:

$$\{\phi_e, \phi_\mu, \phi_\tau\} = \{\sin^2 \xi \cos^2 \zeta, \cos^2 \xi \cos^2 \zeta, \sin^2 \zeta\} \phi_0$$

$$\phi_\beta^T = \sum (\phi_\alpha P_{\alpha\beta})$$

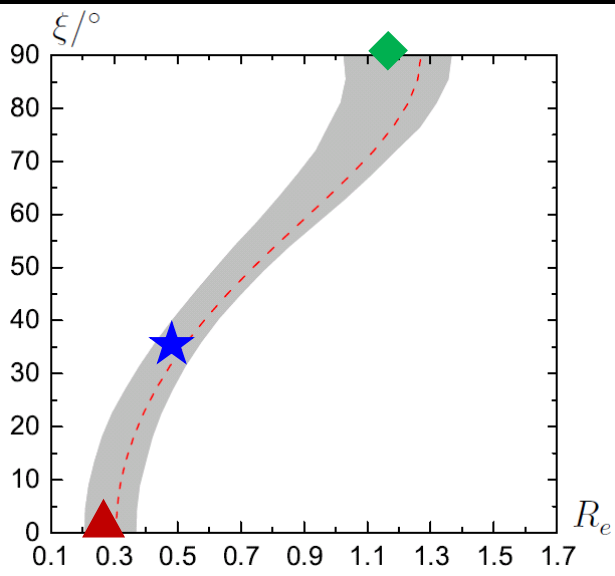


$$R_\alpha = \frac{P_{e\alpha} \sin^2 \xi + P_{\mu\alpha} \cos^2 \xi + P_{\tau\alpha} \tan^2 \zeta}{\sec^2 \zeta - (P_{e\alpha} \sin^2 \xi + P_{\mu\alpha} \cos^2 \xi + P_{\tau\alpha} \tan^2 \zeta)}$$

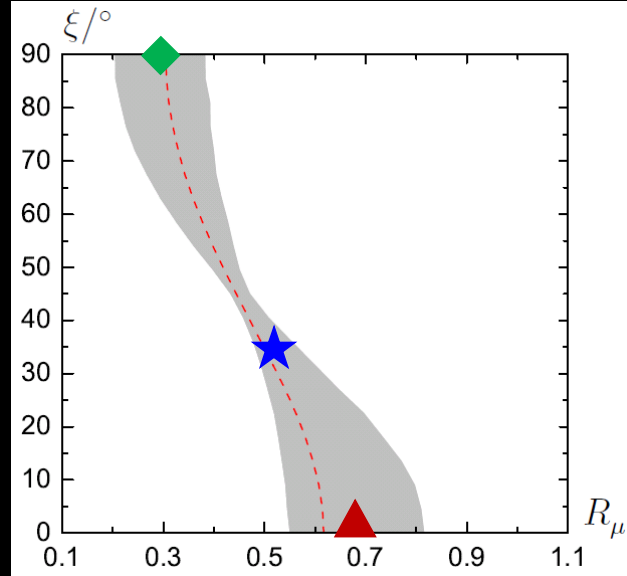
Determination of the source parameters

$$\sin^2 \xi = \frac{\hat{R}_\alpha (P_{\tau\beta} - P_{\mu\beta}) - \hat{R}_\beta (P_{\tau\alpha} - P_{\mu\alpha}) + (P_{\mu\beta} P_{\tau\alpha} - P_{\mu\alpha} P_{\tau\beta})}{(\hat{R}_\alpha - P_{\tau\alpha})(P_{e\beta} - P_{\mu\beta}) - (\hat{R}_\beta - P_{\tau\beta})(P_{e\alpha} - P_{\mu\alpha})}$$

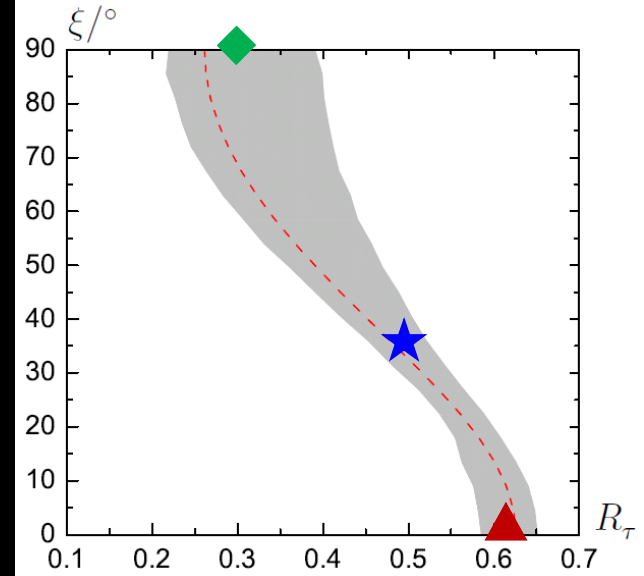
$$\tan^2 \zeta = \frac{\hat{R}_\alpha (P_{\mu\beta} - P_{e\beta}) - \hat{R}_\beta (P_{\mu\alpha} - P_{e\alpha}) + (P_{e\beta} P_{\mu\alpha} - P_{e\alpha} P_{\mu\beta})}{(\hat{R}_\alpha - P_{\tau\alpha})(P_{e\beta} - P_{\mu\beta}) - (\hat{R}_\beta - P_{\tau\beta})(P_{e\alpha} - P_{\mu\alpha})}$$



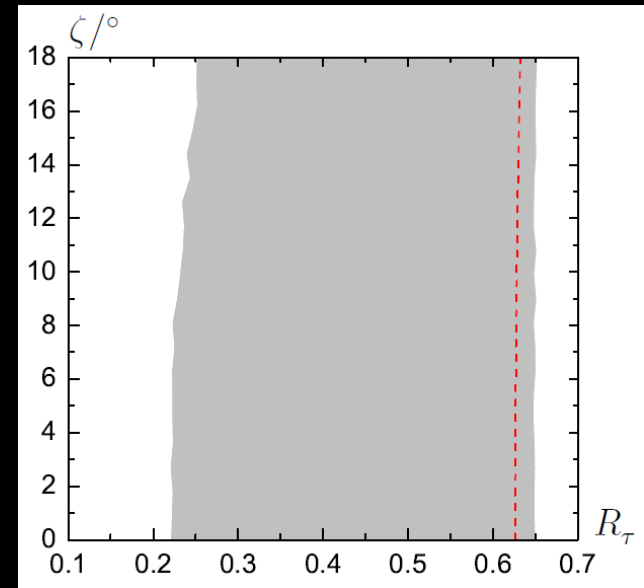
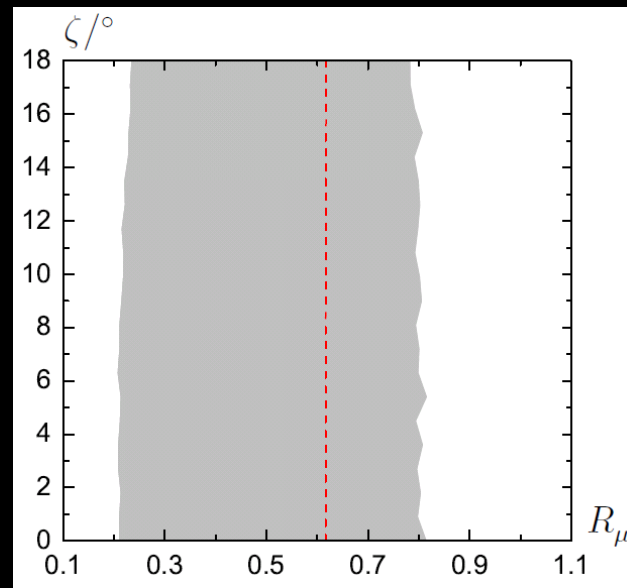
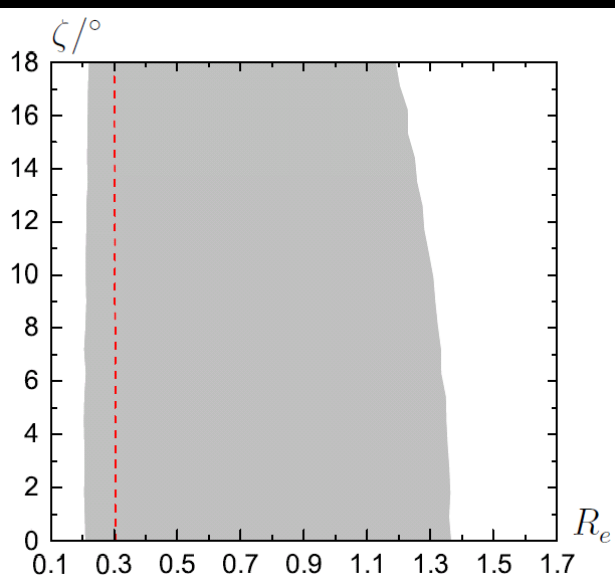
$$\phi_e : \phi_\mu : \phi_\tau = 1 : 2 : 0$$



$$\phi_e : \phi_\mu : \phi_\tau = 1 : 0 : 0$$



$$\phi_e : \phi_\mu : \phi_\tau = 0 : 1 : 0$$



Is C_vB Detectable?

Today's **matter** & **energy** densities in the Universe (Dunkley et al **09**; Komatsu et al **09**; Nakamura et al **10**): **5-year WMAP** + **Λ CDM** model

Parameter	Value
Hubble parameter h	0.72 ± 0.03
Total matter density Ω_m	$\Omega_m h^2 = 0.133 \pm 0.006$
Baryon density Ω_B	$\Omega_B h^2 = 0.0227 \pm 0.0006$
Vacuum energy density Ω_v	$\Omega_v = 0.74 \pm 0.03$
Radiation density Ω_r 	$\Omega_r h^2 = 2.47 \times 10^{-5}$
Neutrino density Ω_ν 	$\Omega_\nu h^2 = \sum m_i / (94 \text{ eV})$
Cold dark matter density Ω_{CDM}	$\Omega_{\text{CDM}} h^2 = 0.110 \pm 0.006$

The **CMB** (**t ~ 380 000 years**) is already measured today

Is it likely to detect the **C_vB** (**t ~ 1 s**) in the foreseeable future? ---- Here we'll look at a **Gedankenexperiment**.

Formation of CνB

As $T \sim$ a few MeV in the Universe, the survival relativistic particles were photons, electrons, positrons, neutrinos and antineutrinos.

Electroweak reactions: $\gamma + \gamma \rightleftharpoons e^+ + e^- \rightleftharpoons \nu_\alpha + \bar{\nu}_\alpha$ (for $\alpha = e, \mu, \tau$)

$$\nu_e + n \rightleftharpoons e^- + p, \bar{\nu}_e + p \rightleftharpoons e^+ + n \quad \bar{\nu}_e + e^- + p \rightleftharpoons n$$

Neutrinos decoupled from matter:

Weak interactions

Hubble expansion

$$\Gamma \sim G_F^2 T^5$$

$$H \sim \frac{\sqrt{g_*} T^2}{M_{\text{Pl}}}$$

$$\Gamma > H$$

$$\Gamma \sim H$$

$$\Gamma < H$$

Number density of 6 relic ν's:

$$n_\nu = \frac{9}{11} n_\gamma \approx 336 \left(\frac{T_\gamma}{2.725 \text{ K}} \right)^3 \text{ cm}^{-3}$$

ν's in thermal contact with cosmic plasma

ν's not in thermal contact with matter

arrow of time

neutrino and photon temperatures (blue)

neutrino decoupling

$$T < m_e \quad e^+ + e^- \rightarrow \gamma + \gamma$$

$$T_\nu = T_\gamma$$

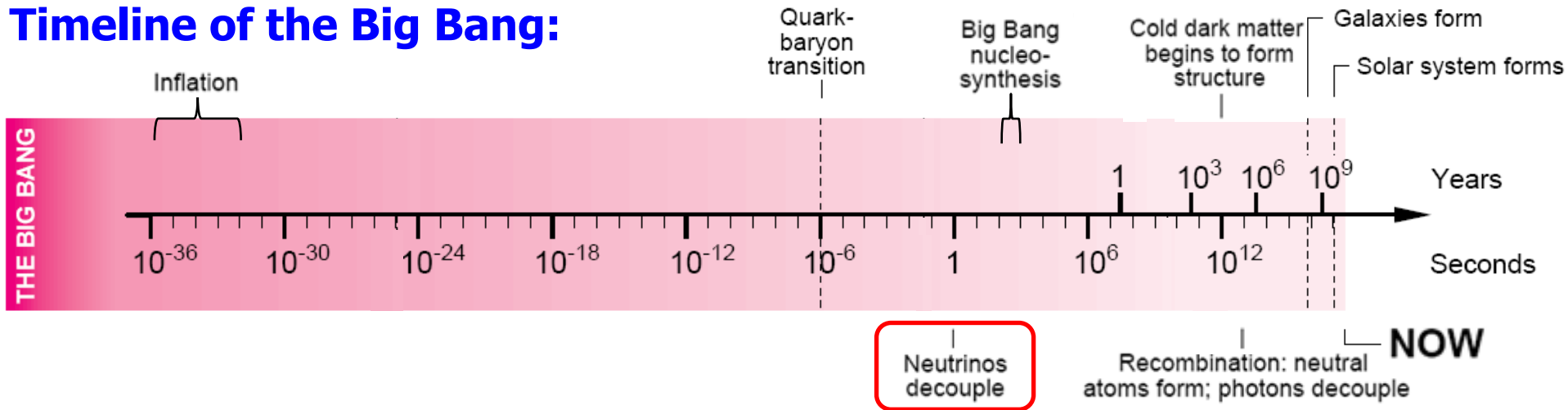
$$T_{\text{fr}} \sim \left(\frac{\sqrt{g_*}}{G_F^2 M_{\text{Pl}}} \right)^{1/3} \sim 1 \text{ MeV}$$

$$T_\nu = \left(\frac{4}{11} \right)^{1/3} T_\gamma$$

Witness / Participant

CMB and **LSS**: the existence of **relic neutrinos** had an impact on the epoch of **matter-radiation equality**, their **species** and **masses** could affect the CMB anisotropies and large scale structures.

Timeline of the Big Bang:



At the time of **recombination** ($t \sim 380\,000$ yrs):

$$\rho_\gamma + \rho_\nu = \rho_\gamma \left[1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_\nu^{\text{CMB}} \right]$$

The **C_vB** contribution to the total energy density of the Universe today

relativistic **non-relativistic**

$$\Omega_\nu = \frac{21}{8} \left(\frac{4}{11} \right)^{4/3} \Omega_\gamma \approx 1.68 \times 10^{-5} h^{-2}$$

$$\Omega_\nu = \frac{8\pi G_N}{3H^2} \sum_i m_i (n_{\nu_i} + n_{\bar{\nu}_i}) \approx \frac{1}{94 h^2 \text{ eV}} \sum_i m_i$$

Detection of $C\nu B$

Way 1: $C\nu B$ -induced **mechanical effects** on Cavendish-type torsion balance;

Way 2: **Capture** of relic ν 's on radioactive β -decaying nuclei (Weinberg 62);

Way 3: **Z-resonance annihilation** of UHE cosmic ν 's and relic ν 's (Weiler 82).

Temperature today

$$T_\nu = \left(\frac{4}{11}\right)^{1/3} T_\gamma \simeq 1.945 \text{ K}$$

Mean momentum today

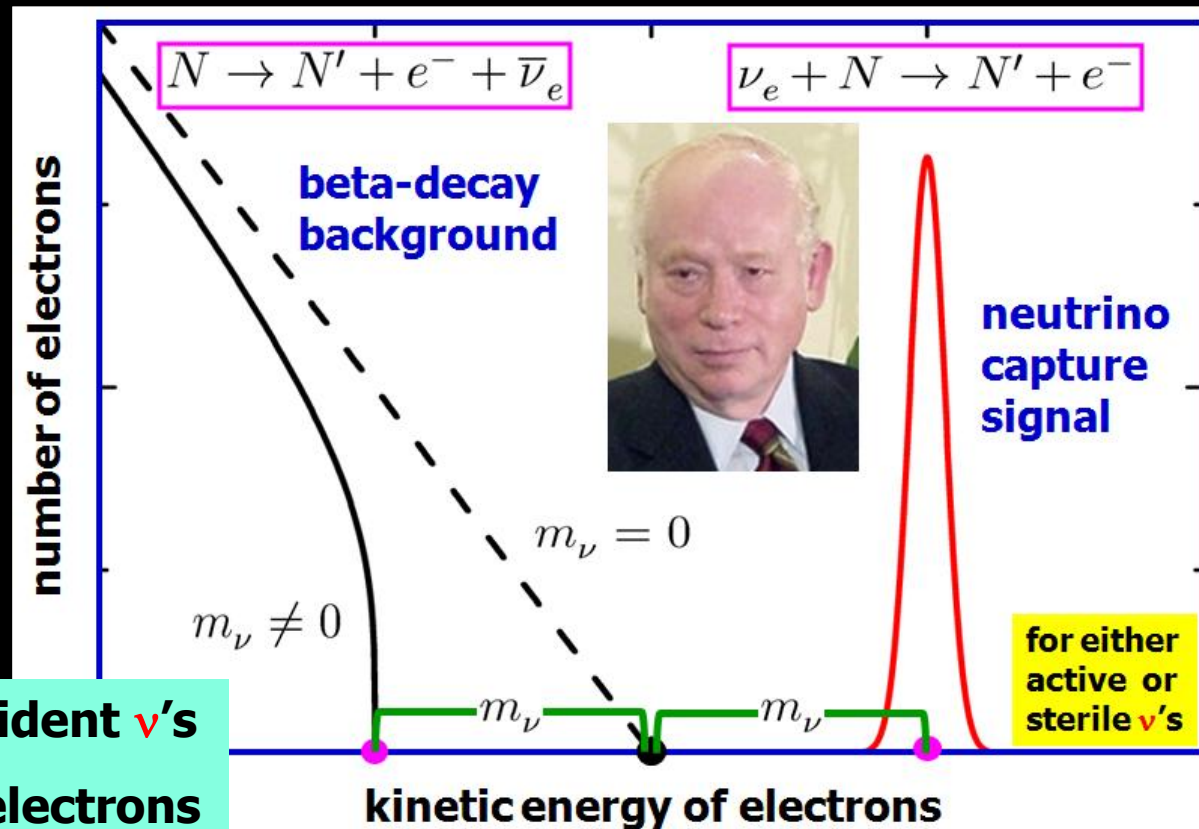
$$\begin{aligned}\langle p_\nu \rangle &\simeq 3.151 T_\nu \\ &\simeq 5.281 \times 10^{-4} \text{ eV}\end{aligned}$$

At least **2 ν 's cold** today

How to detect ULE ν 's ?

(Irvine & Humphreys, 83)

Relic neutrino capture on β -decaying nuclei



- no energy threshold on incident ν 's
- **mono**-energetic outgoing electrons

Example

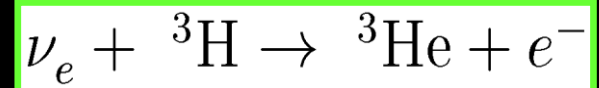
Salient feature: the cross section of a capture reaction scales with $\frac{c}{v_\nu}$ so that the number of events converges to a constant for $v_\nu \rightarrow 0$:

$$\sigma(\nu_e N) \cdot \frac{v_\nu}{c} \Big|_{v_\nu \rightarrow 0} = \text{const.}$$

e.g.

$$\sigma(\nu_e {}^3\text{H}) \cdot \frac{v_\nu}{c} \Big|_{v_\nu \rightarrow 0} \simeq (7.84 \pm 0.03) \times 10^{-45} \text{cm}^2$$

(Cocco et al **07**, Lazauskas et al **08**).



Capture rate: (1 MCi = 100 g = $N_T \approx 2.1 \times 10^{25}$ tritium atoms)

$$\frac{d\mathcal{N}_{\text{C}\nu\text{B}}}{dT_e} \approx 6.5 \sum_i |V_{ei}|^2 \frac{n_{\nu_i}}{\langle n_{\nu_i} \rangle} \cdot \frac{1}{\sqrt{2\pi} \sigma} \exp \left[-\frac{(T_e - T_e^i)^2}{2\sigma^2} \right] \text{yr}^{-1} \text{MCi}^{-1} \quad T_e^i = Q_\beta + E_{\nu_i}$$

Background: (the tritium β -decay)

$$E_e = T'_e + m_e \quad \langle n_{\nu_i} \rangle \approx \langle n_{\bar{\nu}_i} \rangle \approx 56 \text{ cm}^{-3}$$

$$\begin{aligned} \frac{d\mathcal{N}_\beta}{dT_e} \approx & 5.55 \int_0^{Q_\beta - \min(m_i)} dT'_e \left\{ N_T \frac{G_F^2 \cos^2 \theta_C}{2\pi^3} F(Z, E_e) \sqrt{E_e^2 - m_e^2} E_e (Q_\beta - T'_e) \right. \\ & \times \sum_i \left[|V_{ei}|^2 \sqrt{(Q_\beta - T'_e)^2 - m_i^2} \Theta(Q_\beta - T'_e - m_i) \right] \frac{1}{\sqrt{2\pi} \sigma} \exp \left[-\frac{(T_e - T'_e)^2}{2\sigma^2} \right] \Big\} \end{aligned}$$

Energy resolution (Gaussian function) :

$$\Delta = 2\sqrt{2 \ln 2} \sigma \approx 2.35482 \sigma$$

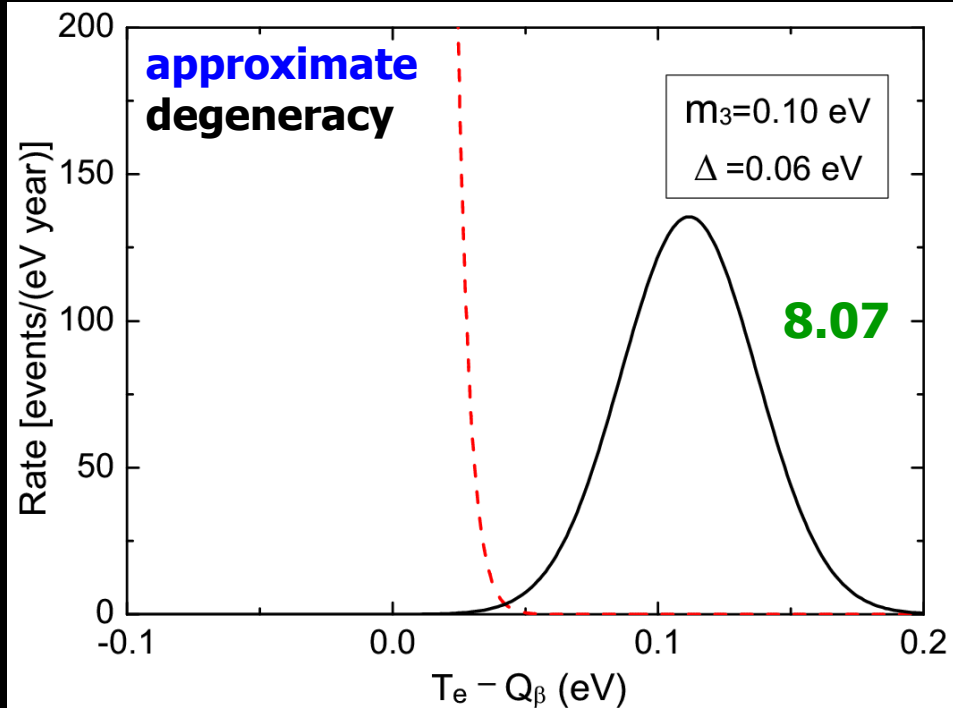
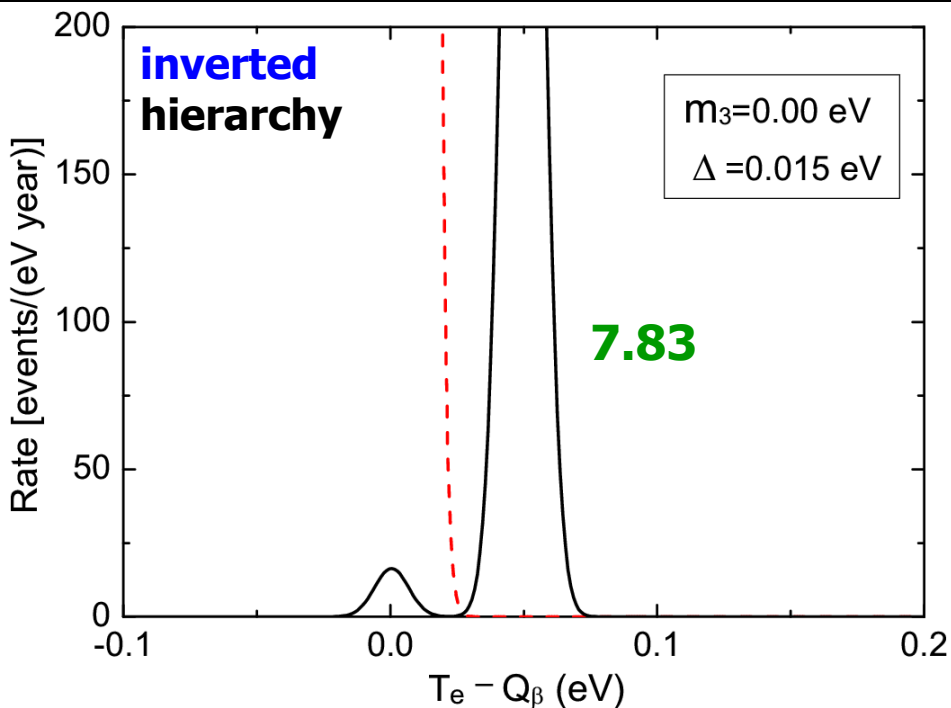
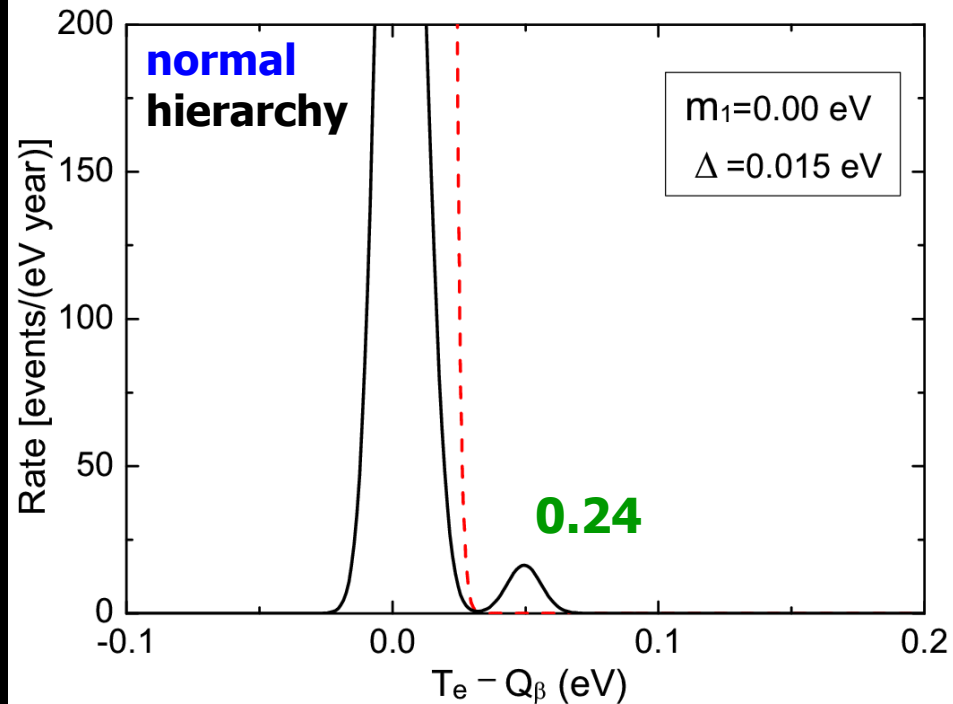
Illustration

Target mass: 100 g tritium atoms

Input $\theta(13)$: 10 degrees

Number of events per year: ~ 8

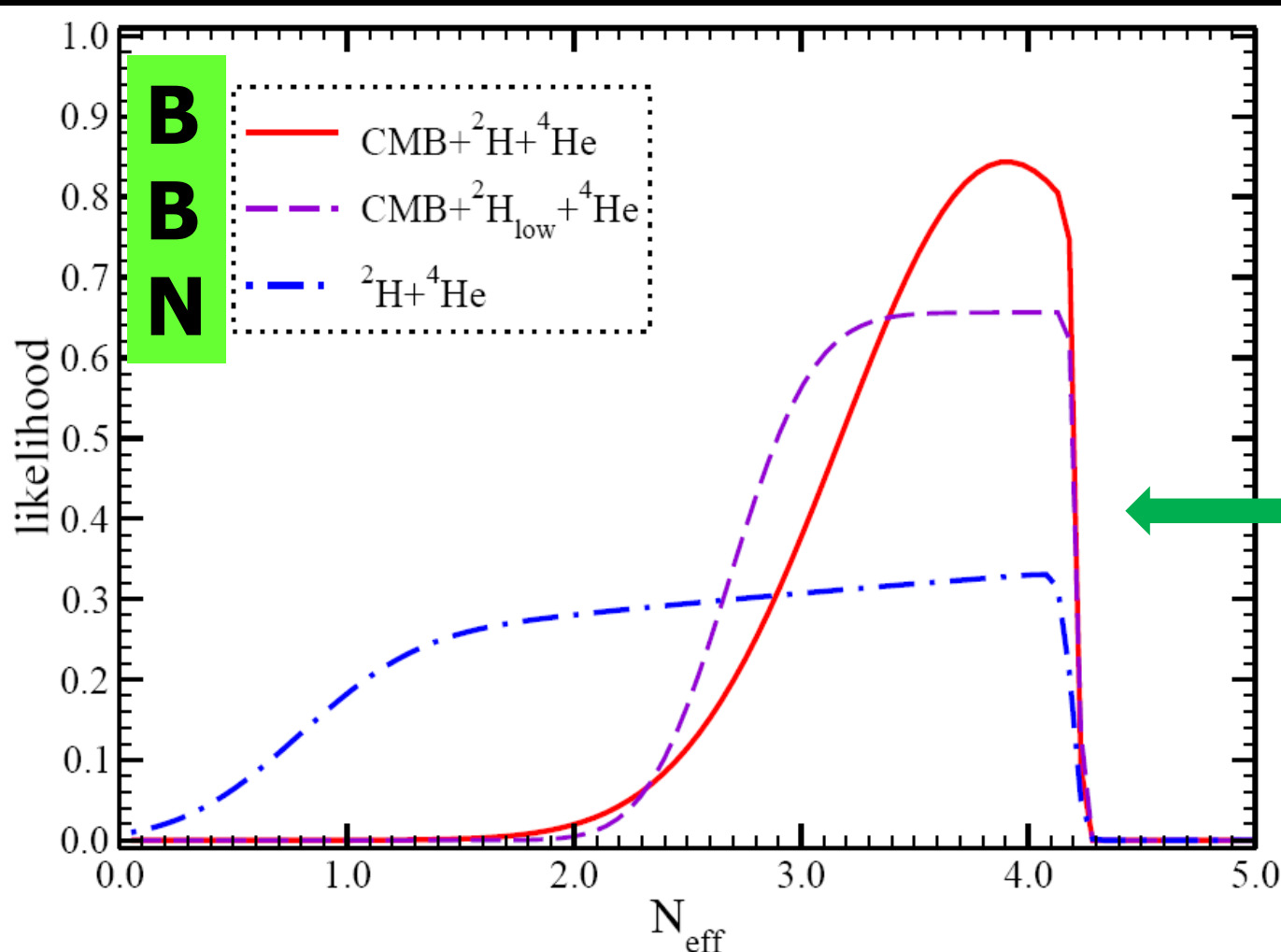
The **gravitational clustering** effect may help enhance the signal rates (Ringwald & Wong, **04**).



Sub-eV Sterile ν 's?

BBN: current data only allow **one** sub-eV **sterile** neutrino;

CMB: current data can allow **two** sub-eV **sterile** neutrinos.



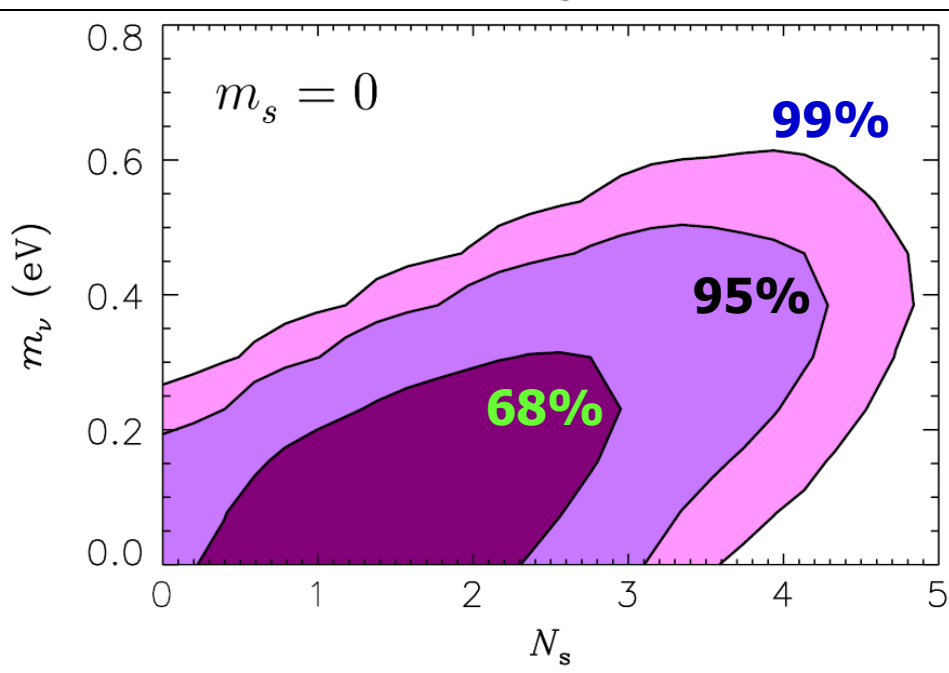
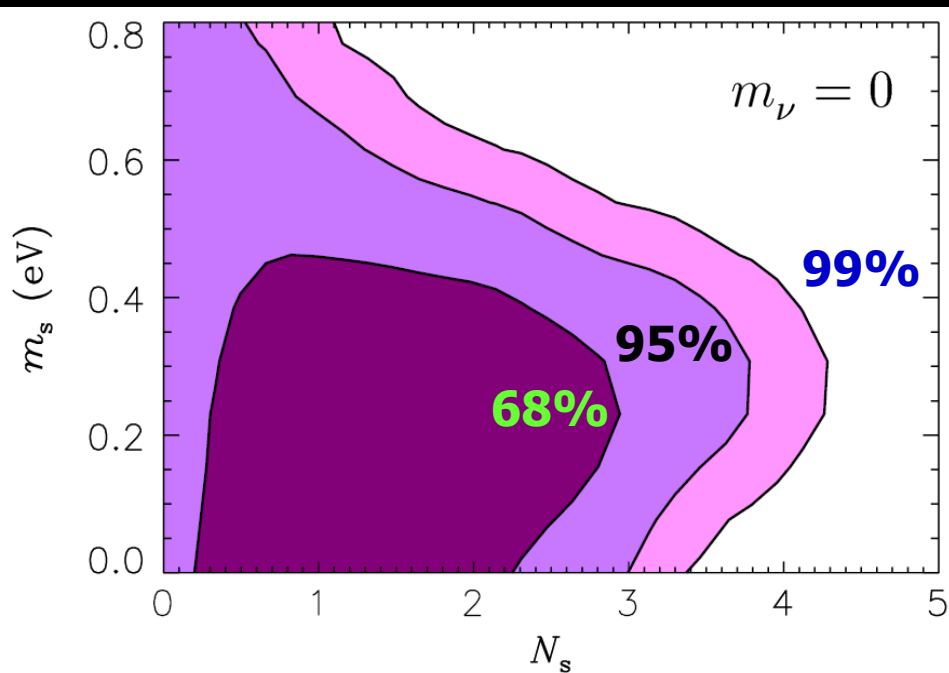
**G. Mangano,
P. Serpico,
arXiv:1103.1261**

$$N_{\text{eff}} < 4.2$$

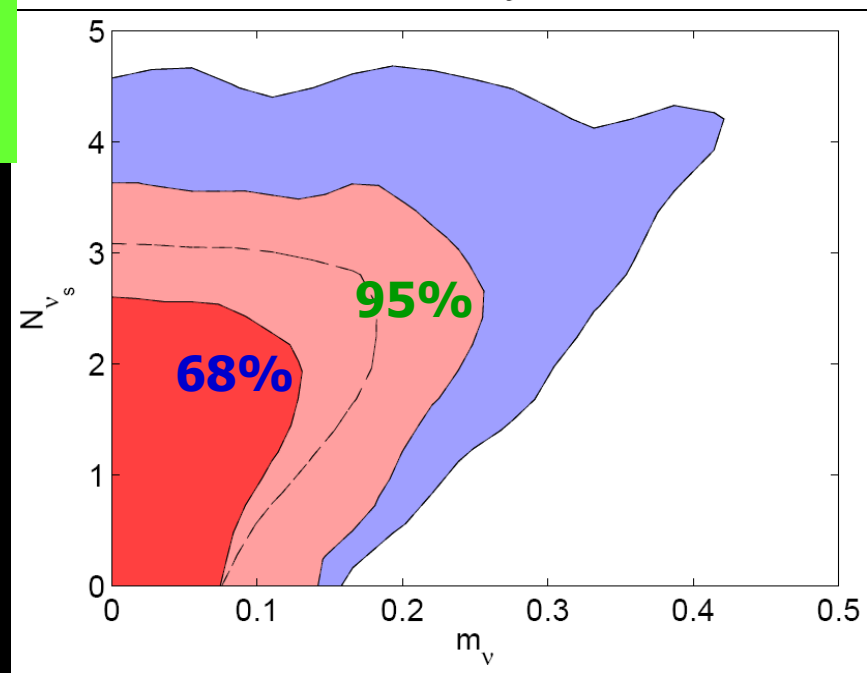
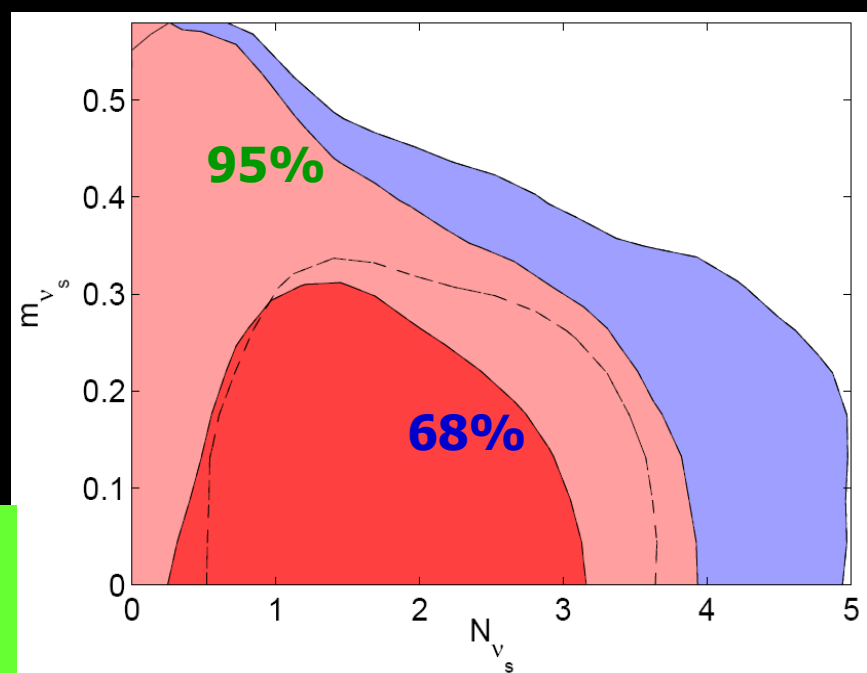
(95% C.L.)

The sharp cut-off
is due to a **He-4**
abundance upper
bound (<0.2631).

$$N_{\text{eff}}^{\text{SM}} = 3.046$$



**C
M
B**

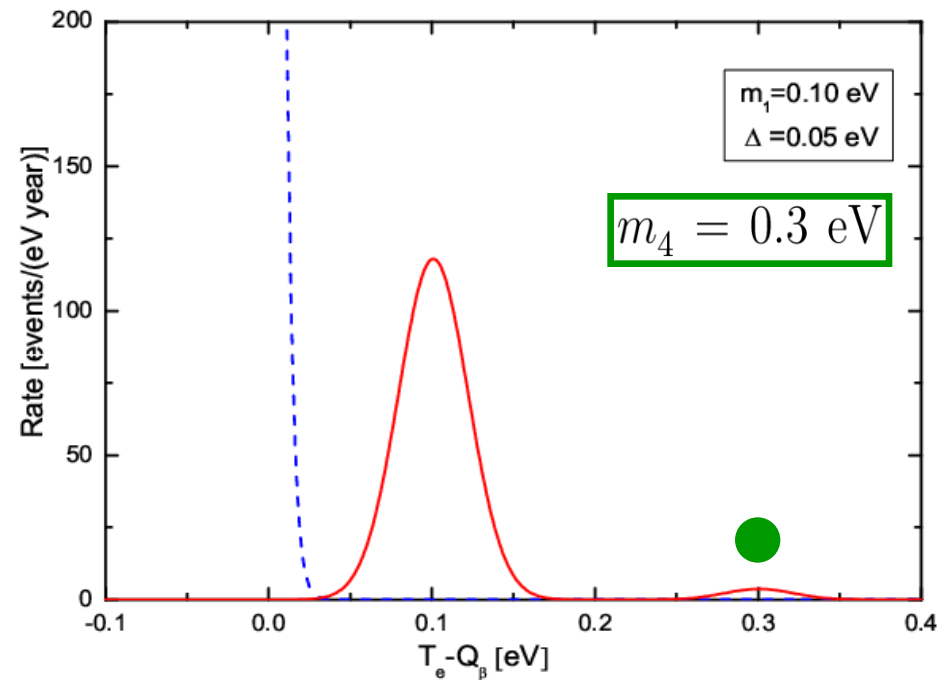
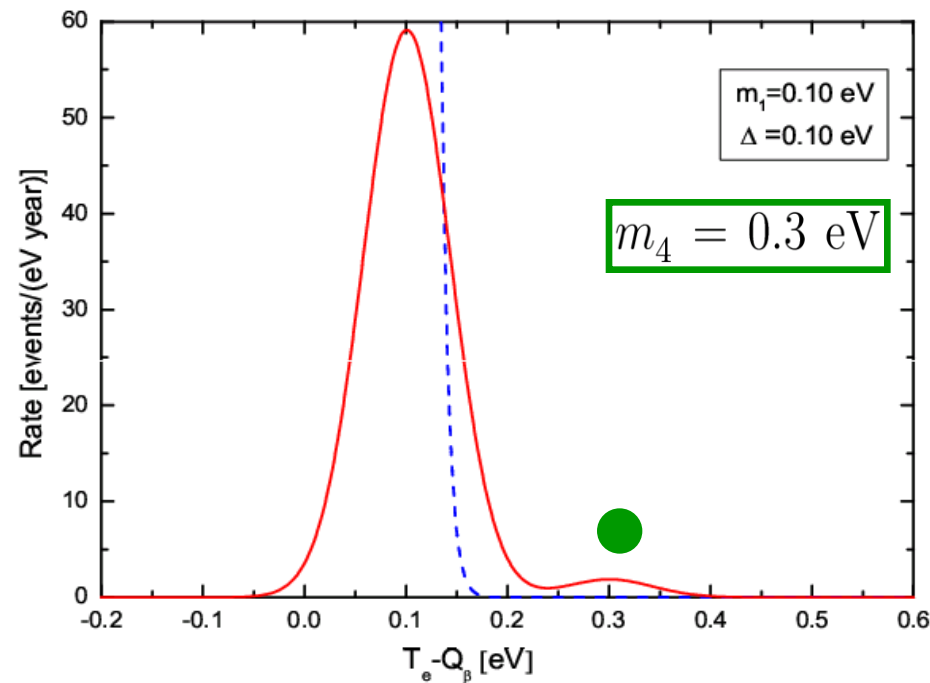


(3+1) Scheme

Besides the **CMB + BBN** hints, the **LSND + MiniBOONE** anomalies and the **reactor antineutrino anomaly** also hint at **1 or 2 sub-eV sterile ν 's**.

They could be thermally excited in the early Universe via oscillations or collisions with active ν 's; they are now non-relativistic; and their number density per species is expected to equal that of active ν 's.

Input: $|V_{e1}| \approx 0.804$, $|V_{e2}| \approx 0.542$, $|V_{e3}| \approx 0.171$, $|V_{e4}| \approx 0.174$ (Li, Xing, Luo, **10**)



Overdensity

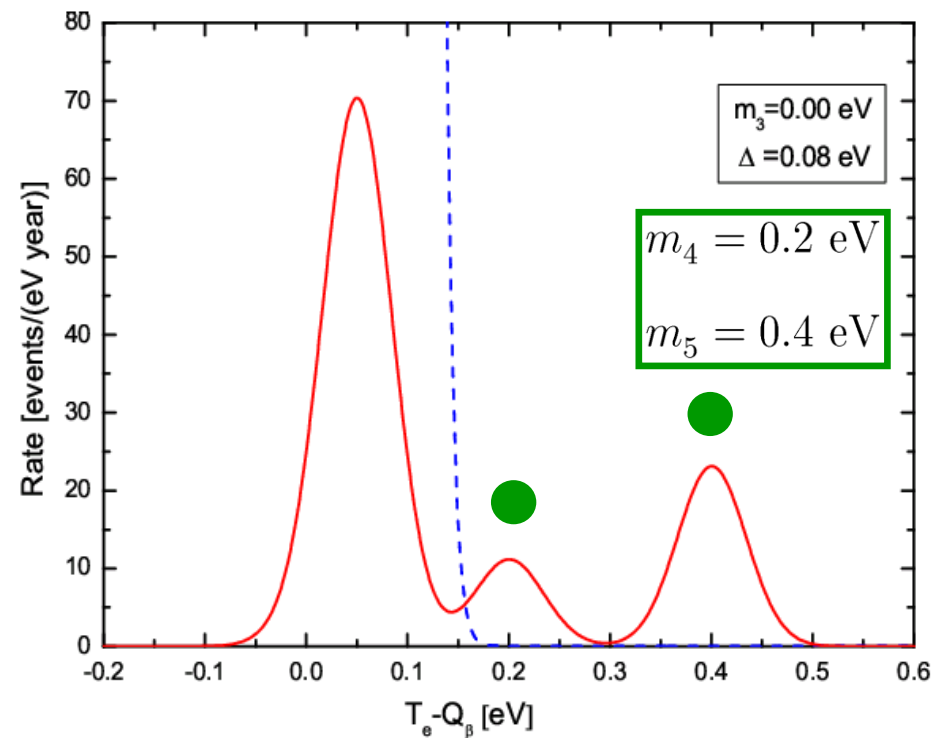
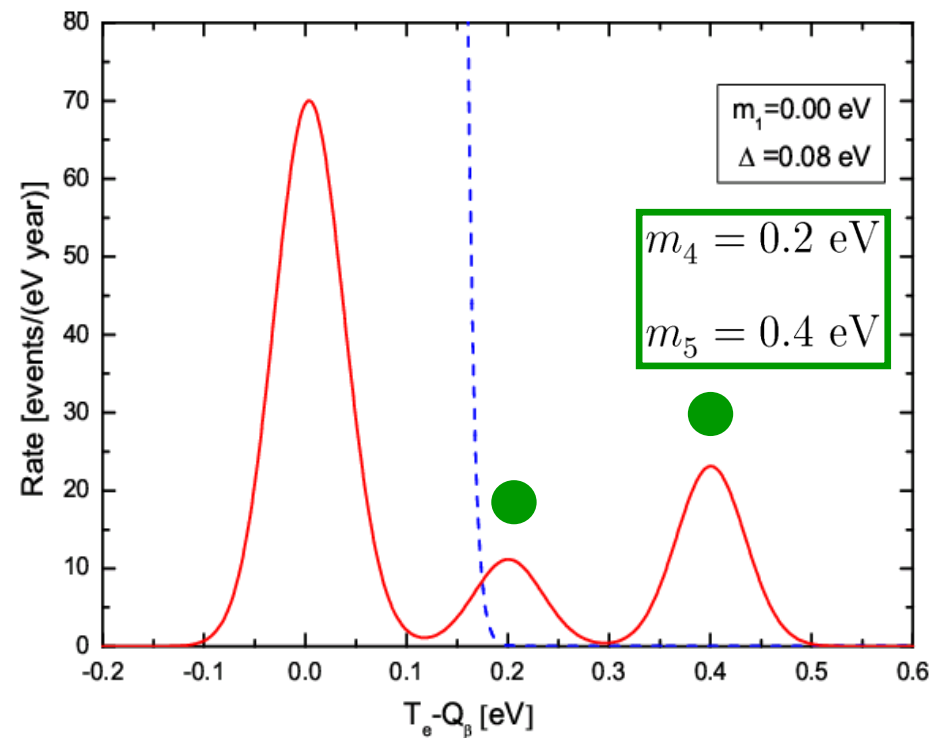
Gravitational clustering: only those cosmic ν 's with velocities smaller than the escape velocity of a given structure can be bound to it. Let's assume a larger GC effect for a heavier ν around the Earth.

The (3+2) scheme:

$$\frac{n_{\nu_1}}{\langle n_{\nu_i} \rangle} \approx \frac{n_{\nu_2}}{\langle n_{\nu_i} \rangle} \approx \frac{n_{\nu_3}}{\langle n_{\nu_i} \rangle} \approx 1, \quad \frac{n_{\nu_5}}{\langle n_{\nu_i} \rangle} \approx 2 \frac{n_{\nu_4}}{\langle n_{\nu_i} \rangle} \approx 10$$

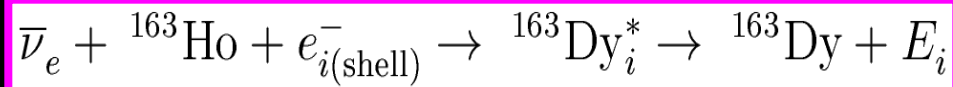
Input:

$$|V_{e1}| \approx 0.792, \quad |V_{e2}| \approx 0.534, \quad |V_{e3}| \approx 0.168, \quad |V_{e4}| \approx 0.171, \quad |V_{e5}| \approx 0.174$$

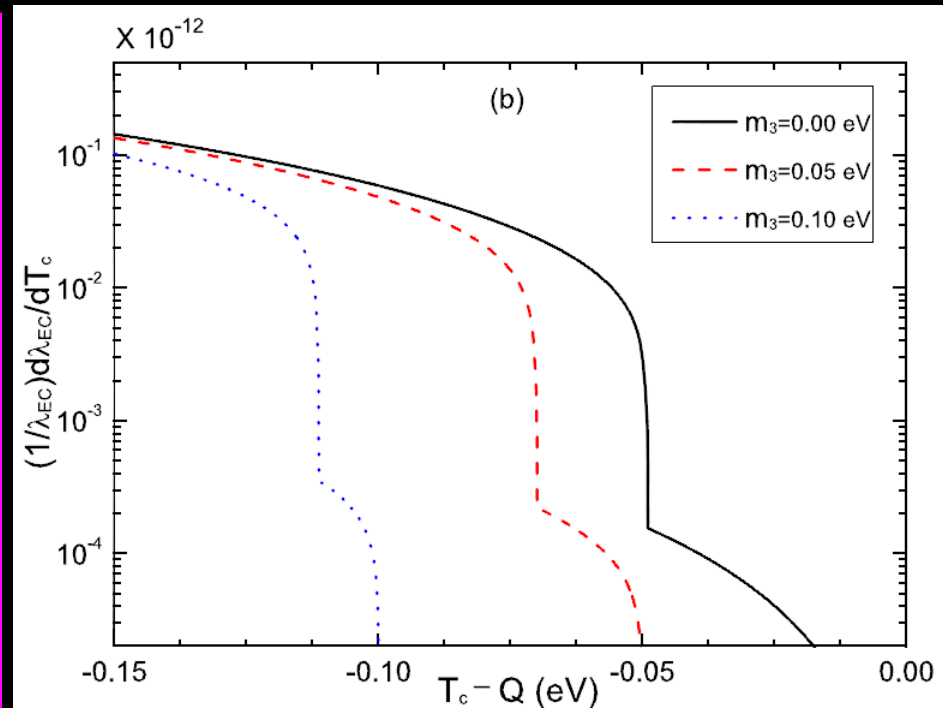
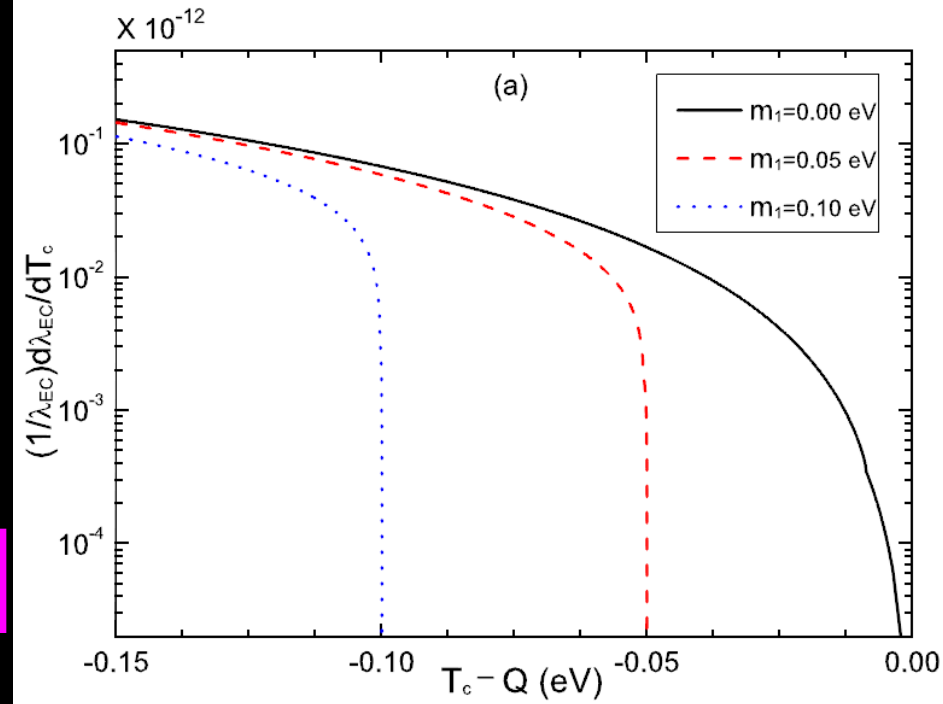
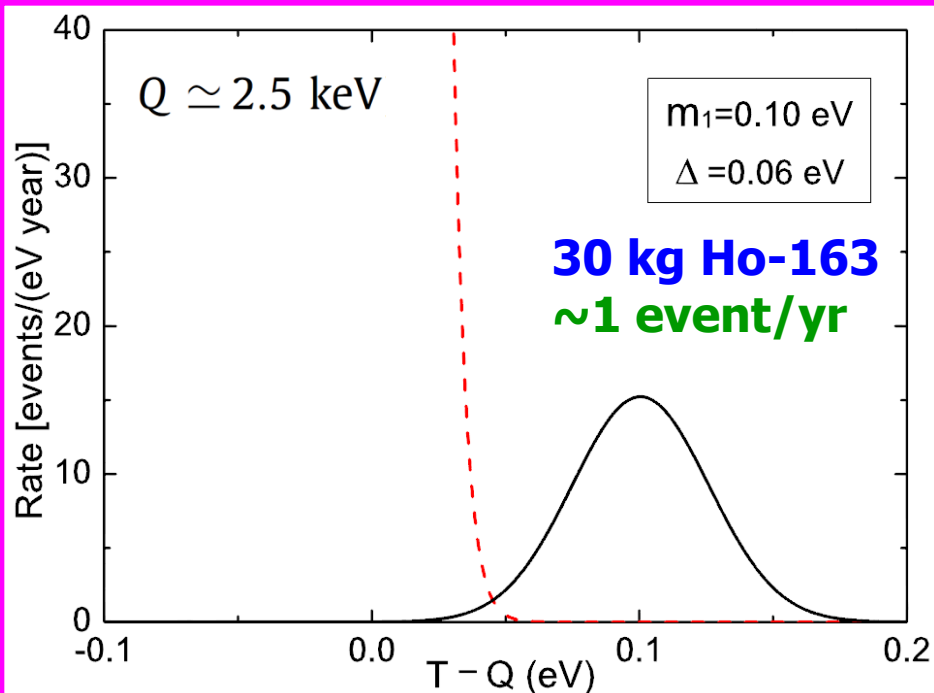


Cosmic anti- ν Background?

Relic antineutrino capture on
EC-decaying Ho-163 nuclei.



(Lusignoli, Vignati, **11**; Li, Xing, **11**)



A Naïve (Why Not) Picture



Hot dark matter: CvB is guaranteed but not significant.

Cold dark matter: most likely? At present most popular.

Warm dark matter: suppress the small-scale structures.

If you think so,

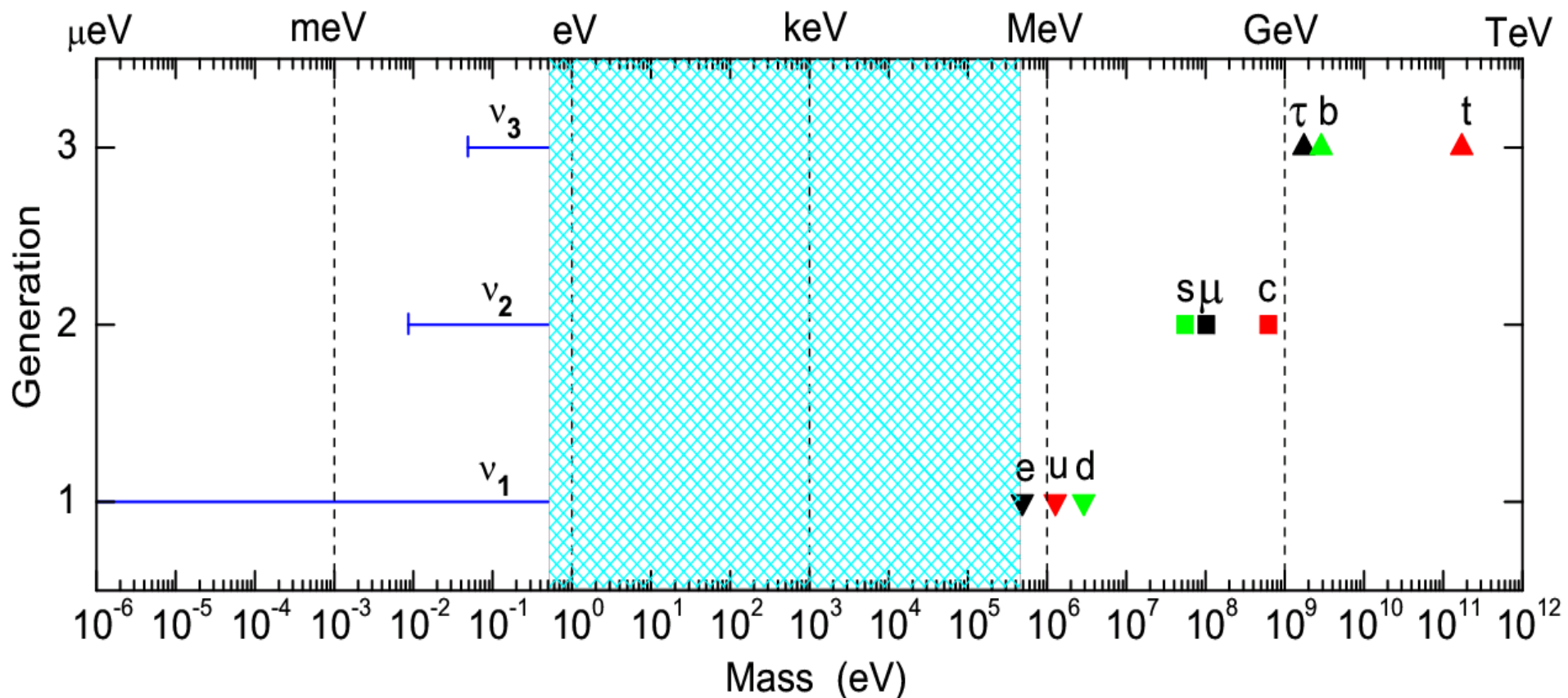
**Do not put all your
eggs in one basket**



keV sterile ν Dark Matter

NO strong prior theoretical motivation for the existence of keV sterile ν 's. **Typical models:** Asaka et al, 05; Kusenko et al, 10; Lindner et al, 11....

A purely phenomenological argument to support keV sterile ν 's in the **FLAVOR DESERT** of the standard model (Xing, 09).



keV sterile ν Dark Matter

NO strong prior theoretical support for the existence of keV sterile ν 's. **Typical models:** Asaoka et al, **10**; Lindner et al, **11**....

keV sterile ν 's

the existence of keV sterile ν 's. **Typical models:** Asaoka et al, **10**; Lindner et al, **11**....

support keV sterile ν 's in the

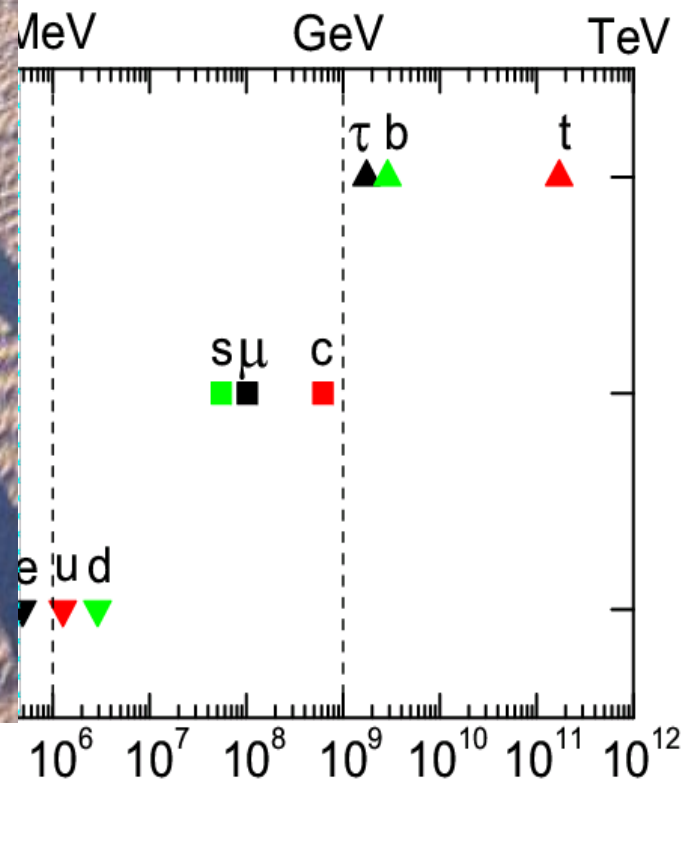


Planck

gauge hierarchy
+
desert problems



Fermi



keV sterile ν Dark Matter

Production: via active-sterile ν oscillations in the early Universe, etc;
Salient feature: warm DM in the form of keV sterile ν 's can suppress the formation of dwarf galaxies and other small-scale structures.

Bounds on 2-flavor parameters:
 (Abazajian, Koushiappas, 2006)

For simplicity, we assume only one type of keV sterile neutrinos:

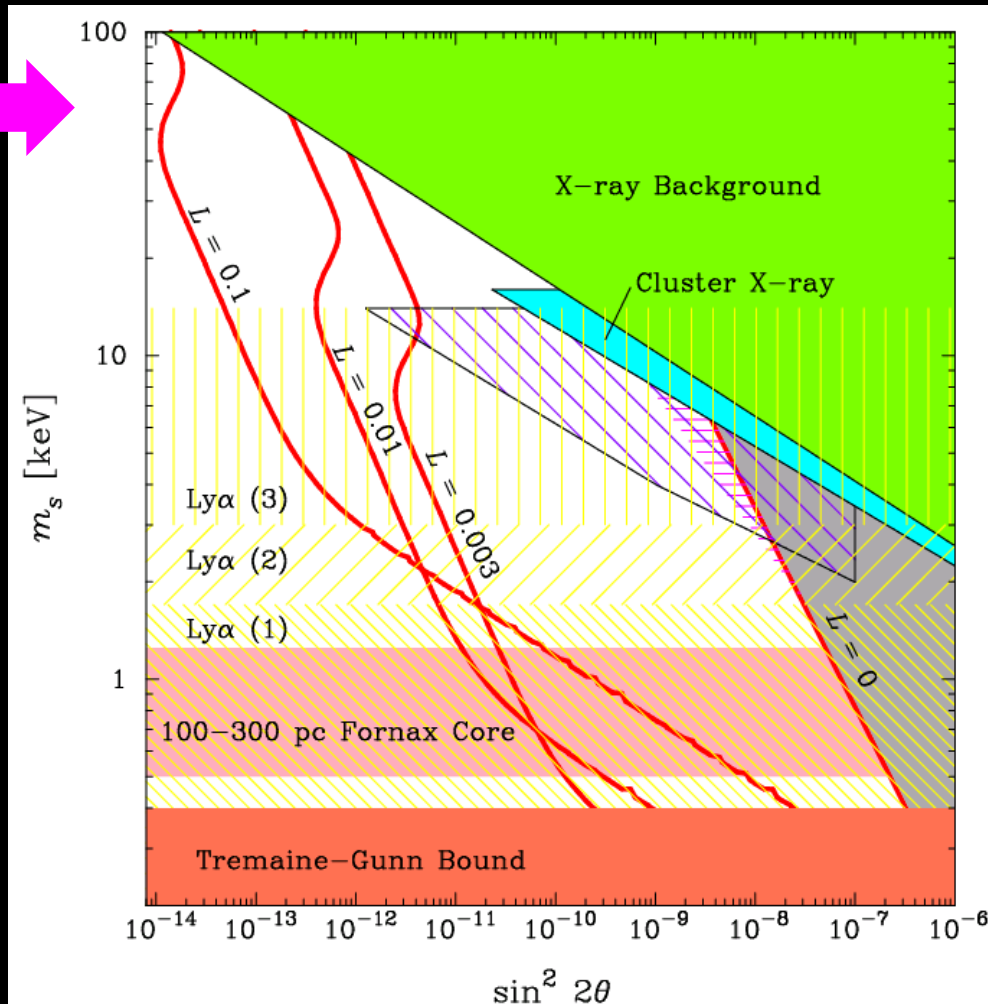
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix} = \begin{pmatrix} V_{e1} & V_{e2} & V_{e3} & V_{e4} \\ V_{\mu1} & V_{\mu2} & V_{\mu3} & V_{\mu4} \\ V_{\tau1} & V_{\tau2} & V_{\tau3} & V_{\tau4} \\ V_{s1} & V_{s2} & V_{s3} & V_{s4} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \end{pmatrix}$$

Standard parameterization of V :
 6 mixing angles & 3 (Dirac) or 6 (Majorana) CP-violating phases.

$$V_{s1} \simeq s_{14} e^{-i\delta_{14}}, \quad V_{s2} \simeq s_{24} e^{-i\delta_{24}}$$

$$V_{s3} \simeq s_{34} e^{-i\delta_{34}}, \quad V_{s4} \simeq 1$$

$$V_{e4} \simeq -c_{12}c_{13}s_{14}e^{i\delta_{14}} - s_{12}c_{13}s_{24}e^{i(\delta_{24}-\delta_{12})}$$



Decay Rates

Dominant decay mode [$C_\nu = 1$ (Dirac) or 2 (Majorana)]:

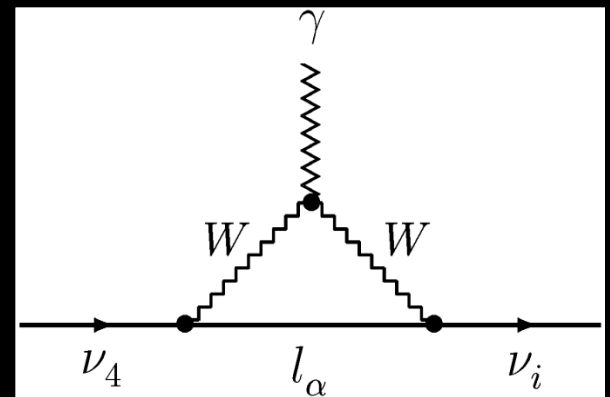
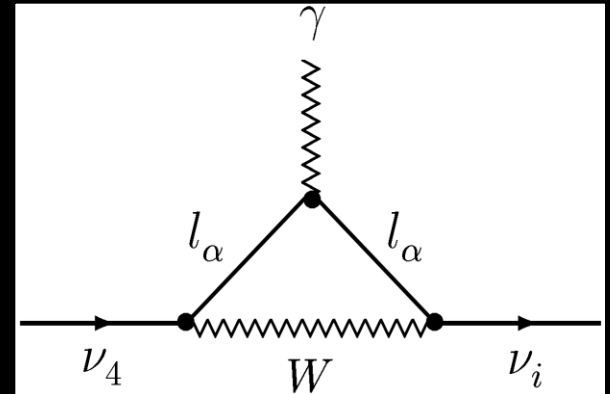
$$\sum_{\alpha=e}^{\tau} \sum_{\beta=e}^{\tau} \Gamma(\nu_4 \rightarrow \nu_\alpha + \nu_\beta + \bar{\nu}_\beta) = \frac{C_\nu G_F^2 m_4^5}{192\pi^3} \sum_{\alpha=e}^{\tau} |V_{\alpha 4}|^2 = \frac{C_\nu G_F^2 m_4^5}{192\pi^3} \sum_{i=1}^3 |V_{si}|^2$$

Lifetime (the Universe's age $\sim 10^{17}$ s):

$$\tau_{\nu_4} \simeq \frac{2.88 \times 10^{27}}{C_\nu} \left(\frac{m_4}{1 \text{ keV}} \right)^{-5} \left(\frac{s_{14}^2 + s_{24}^2 + s_{34}^2}{10^{-8}} \right)^{-1} \text{ s}$$

Radiative decay: X-ray and Lyman-alpha forest observations.

$$\begin{aligned} \sum_{i=1}^3 \Gamma(\nu_4 \rightarrow \nu_i + \gamma) &\simeq \frac{9\alpha_{\text{em}} C_\nu G_F^2 m_4^5}{512\pi^4} \sum_{i=1}^3 \left| \sum_{\alpha=e}^{\tau} V_{\alpha 4} V_{\alpha i}^* \right|^2 \\ &= \frac{9\alpha_{\text{em}} C_\nu G_F^2 m_4^5}{512\pi^4} \sum_{i=1}^3 |V_{s4} V_{si}^*|^2 \\ &\simeq \frac{9\alpha_{\text{em}} C_\nu G_F^2 m_4^5}{512\pi^4} (s_{14}^2 + s_{24}^2 + s_{34}^2) \end{aligned}$$



Detection in the Lab

The same method as the detection of the **CvB** in the lab.

$$\nu_e + N \rightarrow N' + e^-$$

Capture rate with a Gaussian energy resolution:

$$Q_\beta = m_N - m_{N'} - m_e$$

$$\frac{d\mathcal{N}_\nu}{dT_e} = \sum_{i=1}^4 N_T |V_{ei}|^2 \sigma_{\nu_i} v_{\nu_i} n_{\nu_i} \frac{1}{\sqrt{2\pi} \sigma} \exp \left[-\frac{(T_e - T_e^i)^2}{2\sigma^2} \right]$$

$$N \rightarrow N' + e^- + \bar{\nu}_e$$

Assumption: the number density of **sterile ν 's** is equivalent to the total amount of DM in our galactic neighborhood.

$$\rho_{\text{DM}}^{\text{local}} \simeq 0.3 \text{ GeV cm}^{-3}$$

$$n_{\nu_4} \simeq 10^5 (3 \text{ keV}/m_4) \text{ cm}^{-3}$$

Half-life effect of target nuclei (Li, Xing, 11)

$$N_T = \frac{N(0)}{\lambda t} (1 - e^{-\lambda t}), \quad \lambda = \frac{\ln 2}{t_{1/2}}$$

Two sources (Liao, 10; Li, Xing, 11):

$${}^3\text{H} : Q_\beta = 18.6 \text{ keV}, \quad t_{1/2} = 3.888 \times 10^8 \text{ s}, \quad \sigma_{\nu_i} v_{\nu_i}/c = 7.84 \times 10^{-45} \text{ cm}^2$$

$${}^{106}\text{Ru} : Q_\beta = 39.4 \text{ keV}, \quad t_{1/2} = 3.228 \times 10^7 \text{ s}, \quad \sigma_{\nu_i} v_{\nu_i}/c = 5.88 \times 10^{-45} \text{ cm}^2$$

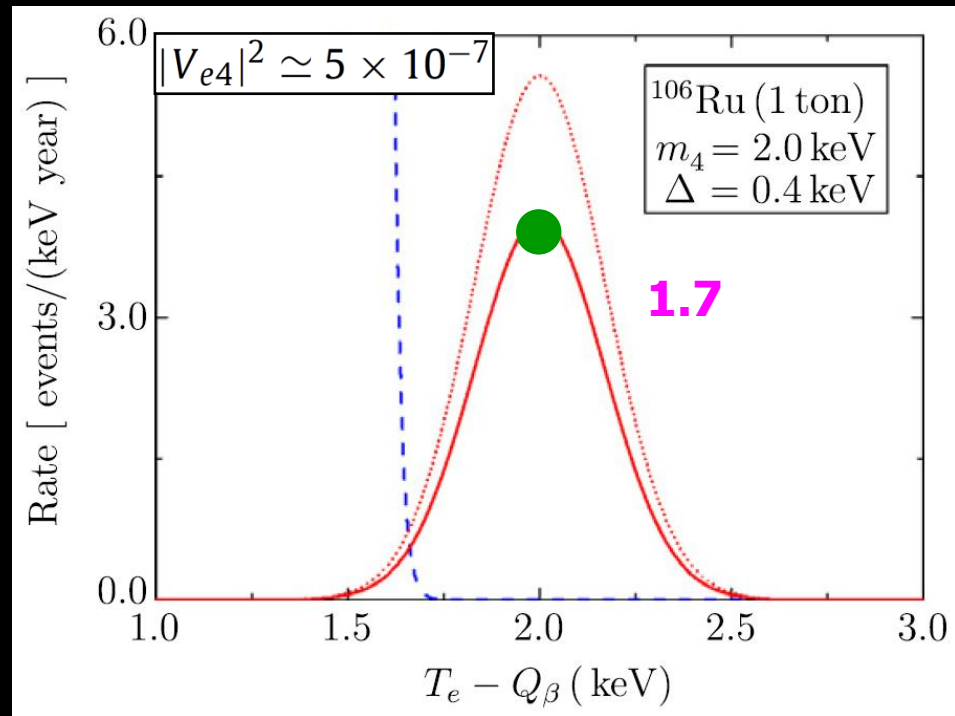
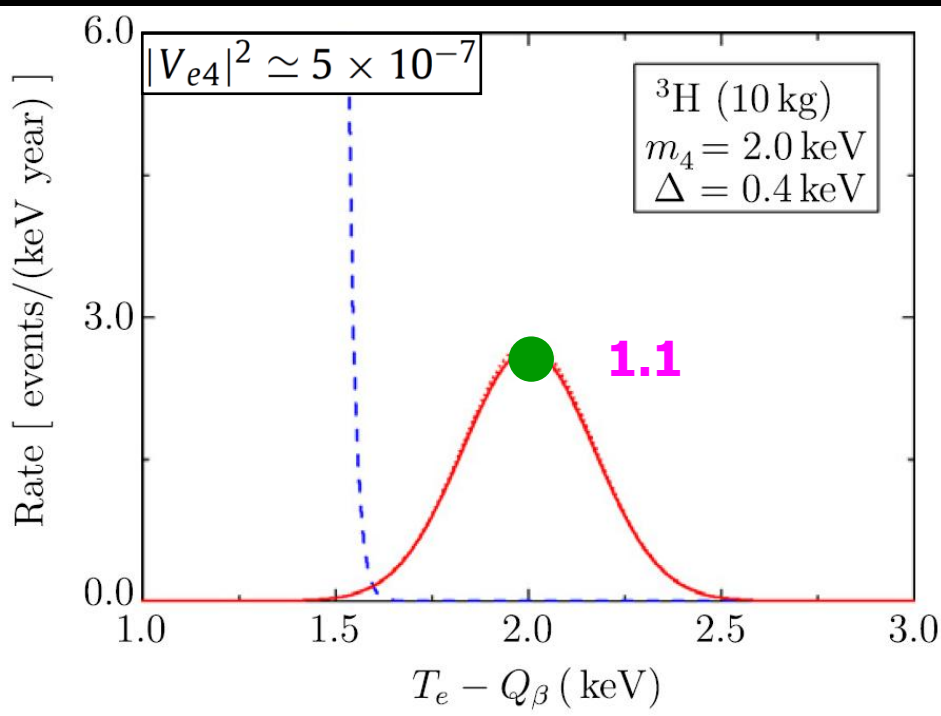
This method & the X-ray detection probe different parameter space.

$$|V_{e4}|^2 \simeq c_{12}^2 s_{14}^2 + s_{12}^2 s_{24}^2 + 2c_{12} s_{12} s_{14} s_{24} \cos(\delta_{24} - \delta_{12} - \delta_{14})$$

Illustration

For illustration: solid (dotted) curves with (without) half-life effects.

Number of events per year: pink



Dim and remote observability of keV sterile neutrino DM in this way:

--- tiny active-sterile neutrino mixing angles (main problem)

--- background: keV solar neutrinos or $\nu_4 + e^- \rightarrow \nu_i + e^-$ scattering.

Summary

There remain some big unknowns in the ν sky:

---- $C\nu B$: a test of cosmology as early as $t \sim 1\text{ s}$ after the Big Bang, but a direct measurement is extremely difficult

The Weinberg trap?

---- **UHE** cosmic ν 's: a probe to the origin of UHE cosmic rays, but a direct measurement is extremely challenging

ν telescopes? **The Glashow resonance?**

---- **Sterile** ν 's as either **hot DM** (**eV**) or **warm DM** (**keV**), but this seems hopeless

The Weinberg trap?

These dreams are so remote that better ideas are needed.

Lecture H

- ★ **Where is Primordial Antimatter?**
- ★ **Sakharov Conditions**
- ★ **Baryogenesis via Leptogenesis**

Dirac's Expectation

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PAUL A. M. DIRAC

Theory of electrons and positrons

Nobel Lecture, December 12, 1933



If we accept the view of complete symmetry between positive and negative electric charge so far as concerns the fundamental laws of Nature, we must regard it rather as an accident that the Earth (and presumably the whole solar system), contains a preponderance of negative electrons and positive protons. It is quite possible that for some of the stars it is the other way about, these stars being built up mainly of positrons and negative protons. In fact, there may be half the stars of each kind. The two kinds of stars would both show exactly the same spectra, and there would be no way of distinguishing them by present astronomical methods.

The Puzzle

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Why is there **not** an anti-
Universe as expected by Dirac?

$$t = 10^{16} \text{ sec}$$

$$r = 10^{29} \text{ cm}$$

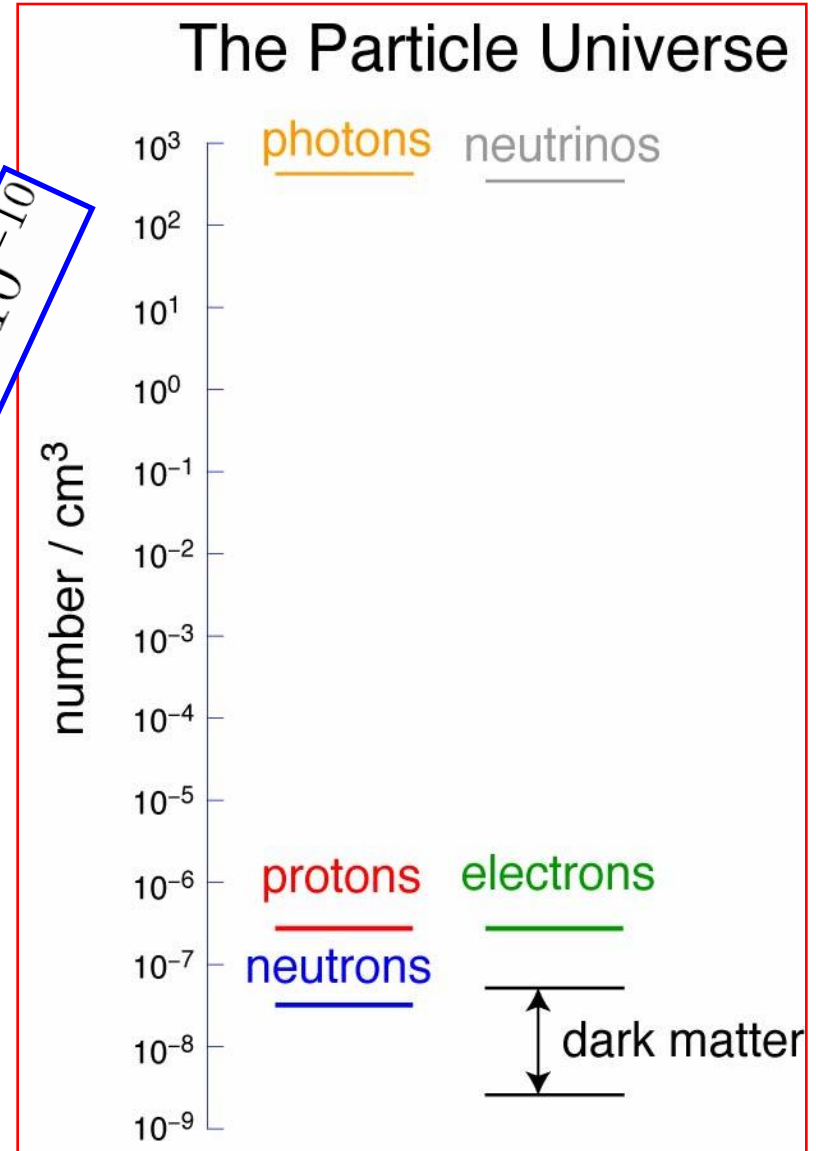
$$T = 2.7 \text{ K}$$

$$400 \gamma / \text{cm}^3$$

$$10^{80} p, n$$

$$0 \quad \bar{p}, \bar{n}$$

$$\eta_B \equiv n_B / n_\gamma = (6.1 \pm 0.2) \times 10^{-10}$$

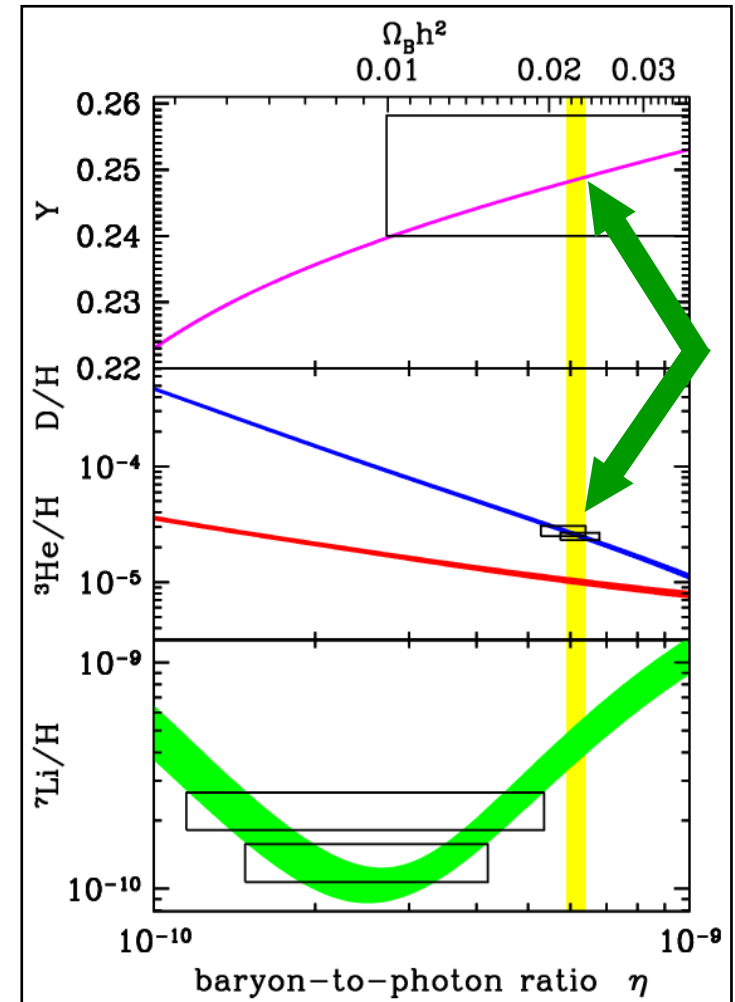
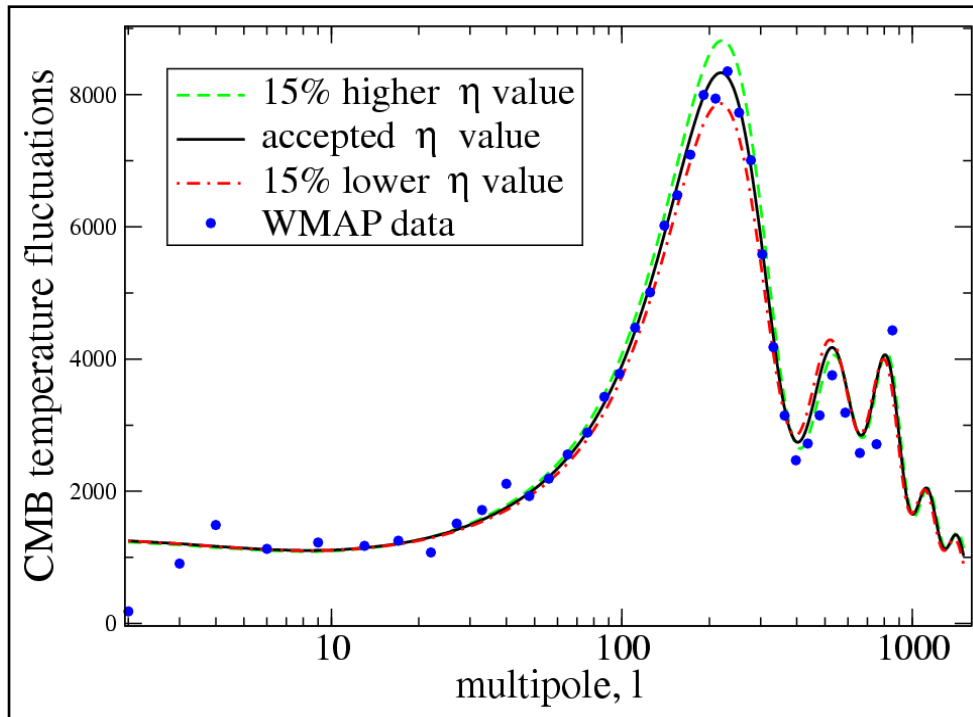


Evidence

47

η_B was historically determined from the **Big Bang Nucleosynthesis**: Primordial abundances of BBN light elements are sensitive to it.

η_B can now be measured from **Cosmic Microwave Background**: Relative sizes of those Doppler peaks of CMB temperature anisotropy are sensitive to it.



Sakharov Conditions

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Baryogenesis: ★ Just-So: $B > 0$ from the very beginning up to now;
★ ★ Dynamical picture: $B > 0$ evolved from $B = 0$ after inflation.

Condition 1: baryon number (B) violation.

[GUT, SUSY & even SM allow it, but no direct experimental evidence]

Condition 2: breaking of C and CP symmetries.

[C & CP asymmetries are both needed to keep B violation survivable]

Condition 3: departure from thermal equilibrium.

[Thermal equilibrium might erase B asymmetry due to CPT symmetry]



Baryogenesis Mechanisms

- ◆ Planck/GUT Baryogenesis;
- ◆ Electroweak Baryogenesis;
- ◆ Leptogenesis;
- ◆ Affleck-Dine Mechanism; ...

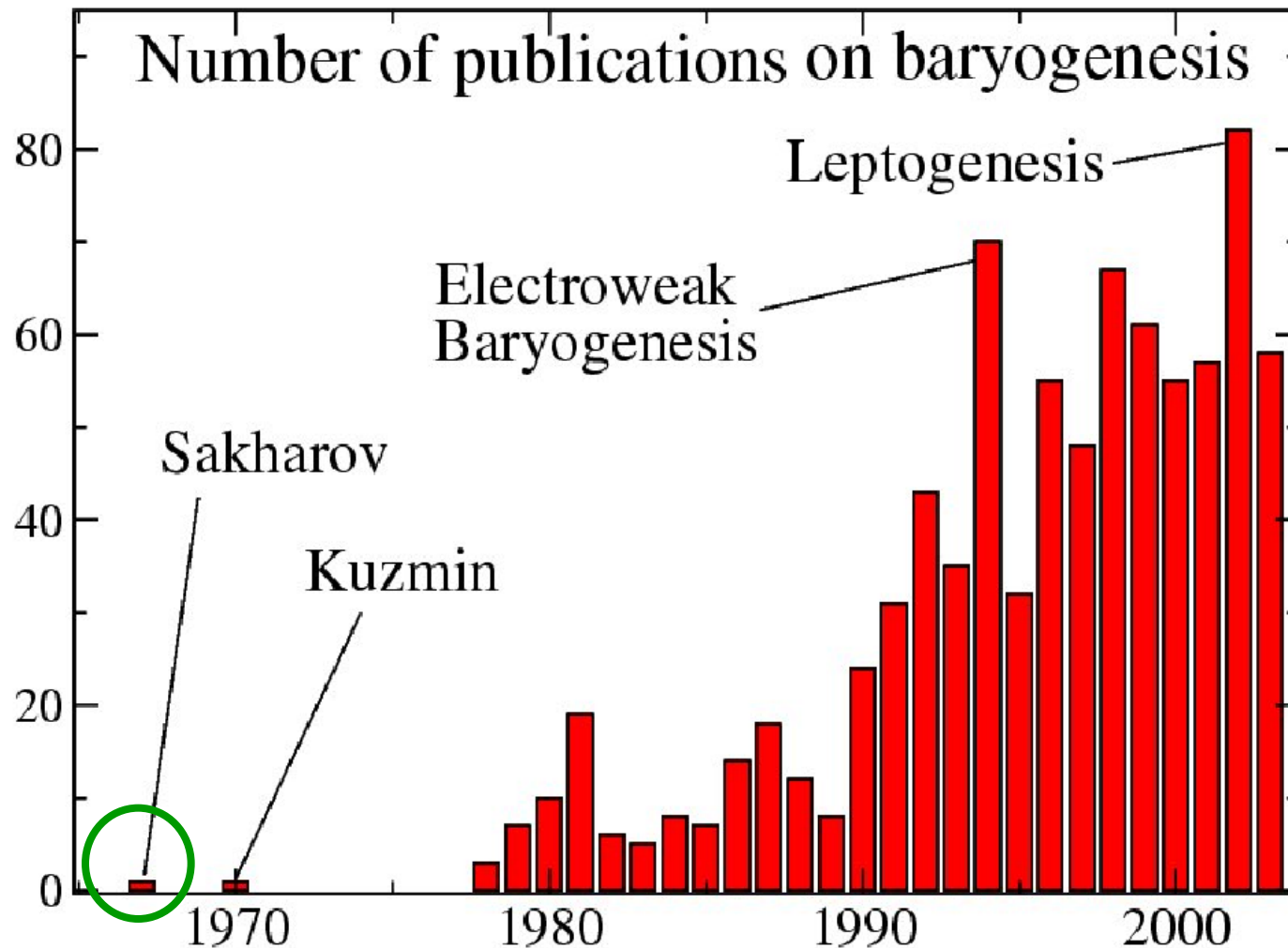
Sakharov's paper:
almost no citation
during 1967-1979

Now >1300 times

Neutrino
Physics

From Cold to Hot

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Lesson: if you publish a paper that nobody cares today, **don't worry**, as it might actually be a seminal work and become popular tomorrow.

Remarks on CP Violation

50

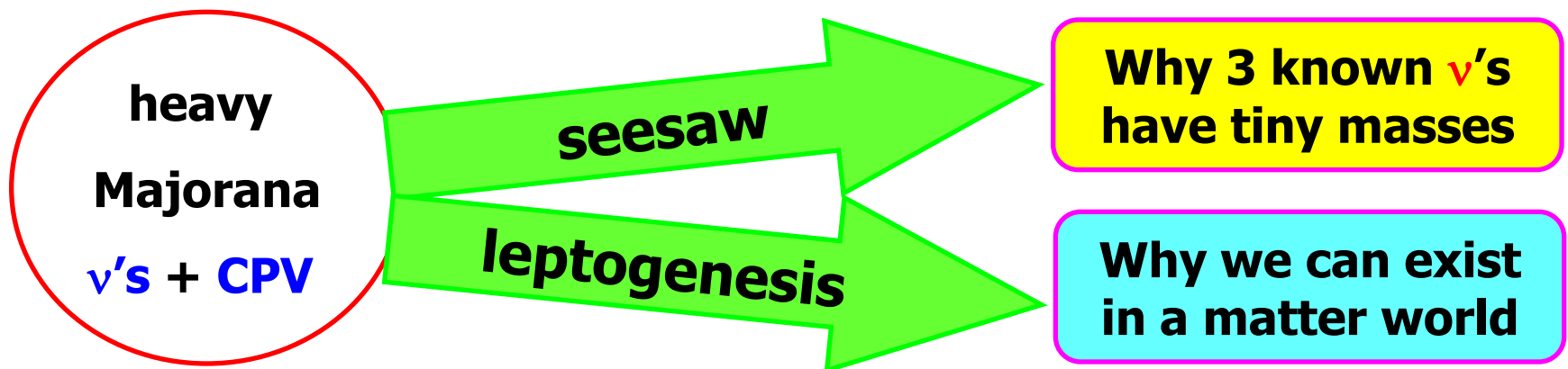
CP violation from the **CKM** quark mixing matrix is not the whole story to explain the **matter-antimatter asymmetry** of the visible Universe.



Two reasons for this in the **SM**:

- **CP** violation from the **SM**'s quark sector is highly suppressed;
- The electroweak phase transition is not strongly first order.

New sources of CP violation are necessarily required.



Thermal Leptogenesis (1) 51

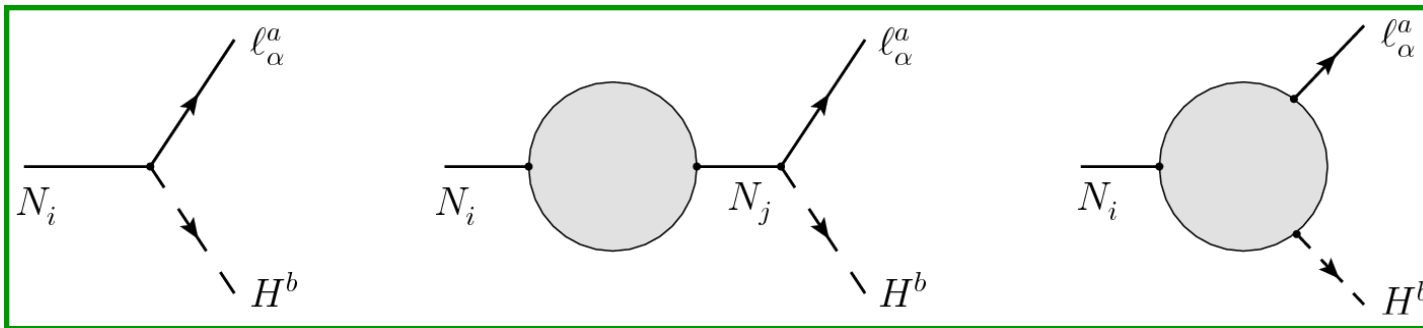
◆ add 3 **heavy right-handed Majorana neutrinos** into SM & keep its $SU(2) \times U(1)$ gauge symmetry:

$$-\mathcal{L}_{\text{lepton}} = \bar{\ell}_L Y_l H E_R + \bar{\ell}_L Y_\nu \tilde{H} N_R + \frac{1}{2} \bar{N}_R^c M_R N_R + \text{h.c.}$$



Fukugita, Yanagida 86

◆ **lepton-number-violating & CP-violating** decays of heavy neutrinos:



$$\begin{aligned} \varepsilon_i &\equiv \frac{\sum_{\alpha} \left[\Gamma(N_i \rightarrow \ell_{\alpha} + H) - \Gamma(N_i \rightarrow \bar{\ell}_{\alpha} + \bar{H}) \right]}{\sum_{\alpha} \left[\Gamma(N_i \rightarrow \ell_{\alpha} + H) + \Gamma(N_i \rightarrow \bar{\ell}_{\alpha} + \bar{H}) \right]} \\ &\approx \frac{1}{8\pi(Y_{\nu}^{\dagger} Y_{\nu})_{ii}} \sum_j \text{Im} \left[(Y_{\nu}^{\dagger} Y_{\nu})_{ij} \right]^2 \left[f_V \left(\frac{M_j^2}{M_i^2} \right) + f_S \left(\frac{M_j^2}{M_i^2} \right) \right] \end{aligned}$$

$$\begin{aligned} f_V(x) &= \begin{cases} \sqrt{x} \left[1 - (1+x) \ln \frac{1+x}{x} \right] & (\text{SM}), \\ -\sqrt{x} \ln \frac{1+x}{x} & (\text{SUSY}); \end{cases} \\ f_S(x) &= \begin{cases} \frac{\sqrt{x}}{1-x} & (\text{SM}), \\ \frac{2\sqrt{x}}{1-x} & (\text{SUSY}). \end{cases} \end{aligned}$$

Thermal Leptogenesis (2) 52

◆ to prevent **CP** asymmetries from being washed out by the inverse decays and scattering processes, the decays of heavy neutrinos must be **out of thermal equilibrium** (their decay rates must be smaller than the expansion rate of the Universe.

$$\Gamma(N_i \rightarrow \ell_\alpha + H) < H(T = M_i)$$

The **net** lepton number asymmetry:

$$Y_L \equiv \frac{n_L - n_{\bar{L}}}{s} = \frac{1}{g_*} \sum_i \kappa_i \varepsilon_i$$

κ_i : efficiency factors

g_* : number of relativistic d.o.f

s : entropy density

(Boltzmann equations for time evolution of particle number densities)

◆ non-perturbative but (**B-L**)-**conserving** weak **sphaleron** reactions convert a lepton number asymmetry to a baryon number asymmetry.

$$\partial_\mu J_B^\mu = \partial_\mu J_L^\mu = \frac{N_f}{32\pi^2} \left(-g^2 W_{\mu\nu}^i \tilde{W}^{i\mu\nu} + g'^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \right)$$

at the quantum level
via triangle anomaly.

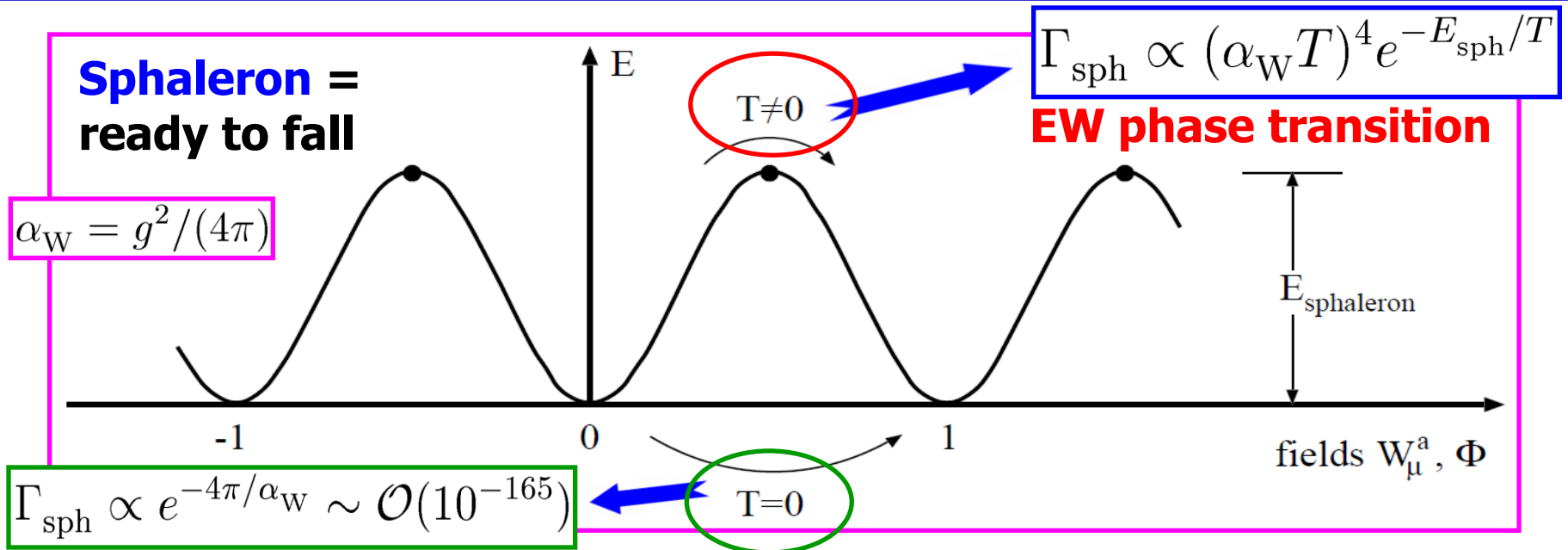
$$B - L = \int d^3x (J_B^0 - J_L^0) = 0$$

(**B-L**) is conserved in the SM ('t Hooft, 76)

Chern-Simons (CS) numbers = $\pm 1, \pm 2, \dots$

$$\Delta B = \Delta L = N_f \Delta N_{\text{CS}}$$

Thermal Leptogenesis (3) 53



Sphaleron-induced ($B+L$)-violating process is in thermal equilibrium when the temperature:

$$10^2 \text{ GeV} < T < 10^{12} \text{ GeV}$$

Baryogenesis via leptogenesis is realized:

$$Y_B \equiv \frac{n_B - n_{\bar{B}}}{s} = -CY_L$$

$$\left. \frac{n_B}{s} \right|_{\text{equilibrium}} = C \left. \frac{n_B - n_L}{s} \right|_{\text{equilibrium}} = -C \left. \frac{n_L}{s} \right|_{\text{initial}}$$

$$\left. \frac{n_{\bar{B}}}{s} \right|_{\text{equilibrium}} = C \left. \frac{n_{\bar{B}} - n_{\bar{L}}}{s} \right|_{\text{equilibrium}} = -C \left. \frac{n_{\bar{L}}}{s} \right|_{\text{initial}}$$

$$C = \frac{8N_f + 4N_\Phi}{22N_f + 13N_\Phi}$$

$$= \begin{cases} 28/79 & (\text{SM}) \\ 8/23 & (\text{MSSM}) \end{cases}$$

History of the Universe

something occurred
over there
13.7 billion years ago

**BIG
BANG**

Inflation

t	10^{-44}	10^{-37} s
T	10^{32}	10^{28}
E	10^{19}	10^{15}

L
↓
B

possible dark matter relics

cosmic microwave radiation visible

Key:		W, Z bosons	photon
q quark	meson	star	
g gluon	baryon	galaxy	
e electron	ion	black hole	
m muon	tau		
n neutrino	atom		

Particle Data Group, LBNL, © 2000. Supported by DOE and NSF

so

we

are

here

today

1 Stone Kills 2 Birds

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(A) It is not difficult to build a canonical “**seesaw** + **leptogenesis**” model which simultaneously account for current data on neutrino oscillations and baryon number asymmetry.

(B) It is also possible to realize **baryogenesis** via **leptogenesis** in other seesaw mechanisms at a super-high energy scale.

(C) Lower-scale **leptogenesis** is not impossible, but suffers from fine-tuning (**resonant leptogenesis**) and very difficult to produce observable signatures at the **LHC**.

(D) How to test **baryogenesis** via **leptogenesis** remains an open question: indirect test? (Majorana ν 's, leptonic CP violation,).

Developments and variations (Davidson, Nardi, Nir, Phys. Rept. **08**):

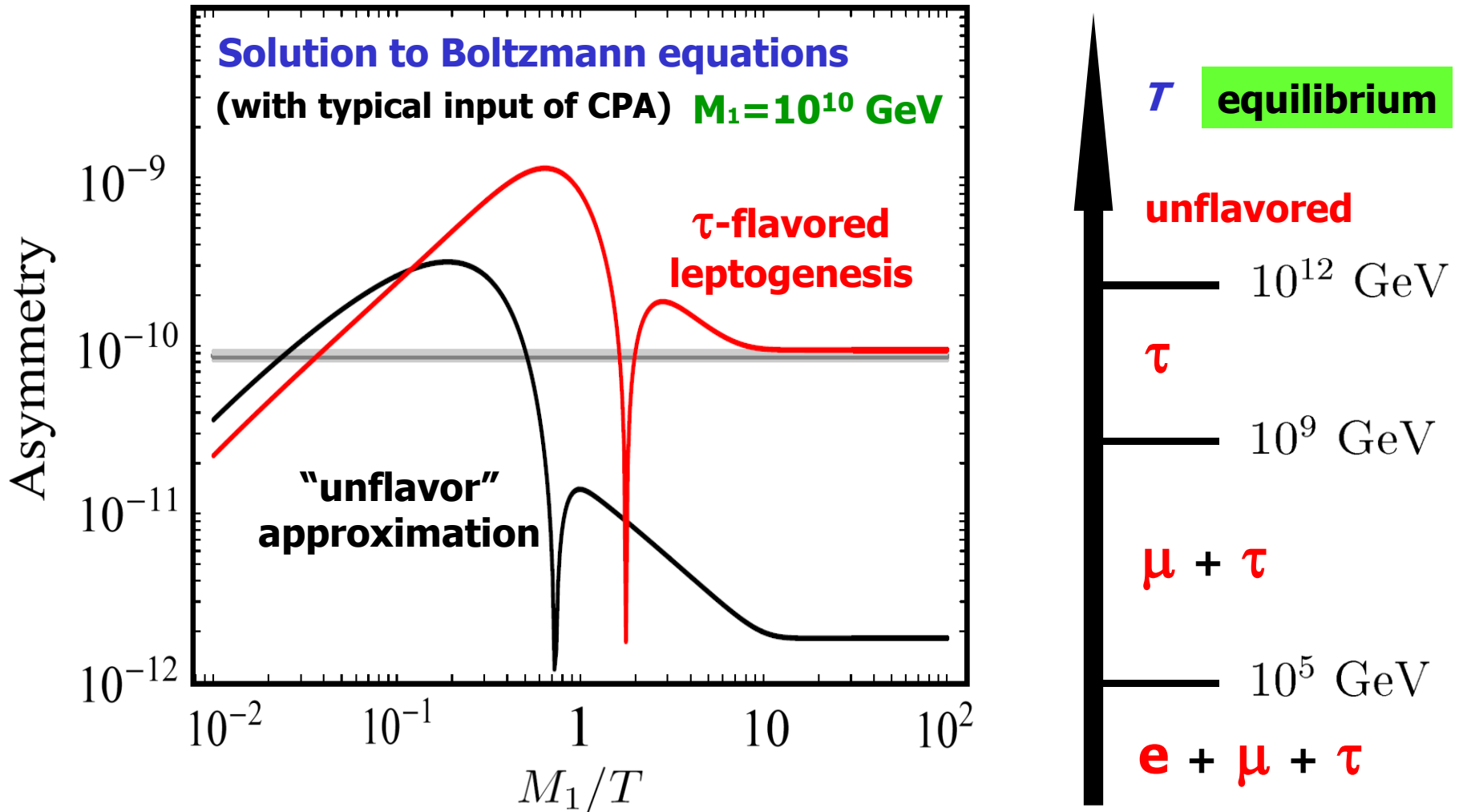
- **Recent developments:** spectator processes; finite temperature effects; flavor effects; $N=2$ leptogenesis; resonant (TeV) leptogenesis;

- **Some variations:** soft (SUSY) leptogenesis; type-II leptogenesis; Dirac leptogenesis; type-III leptogenesis; electromagnetic leptogenesis;

Flavored Leptogenesis

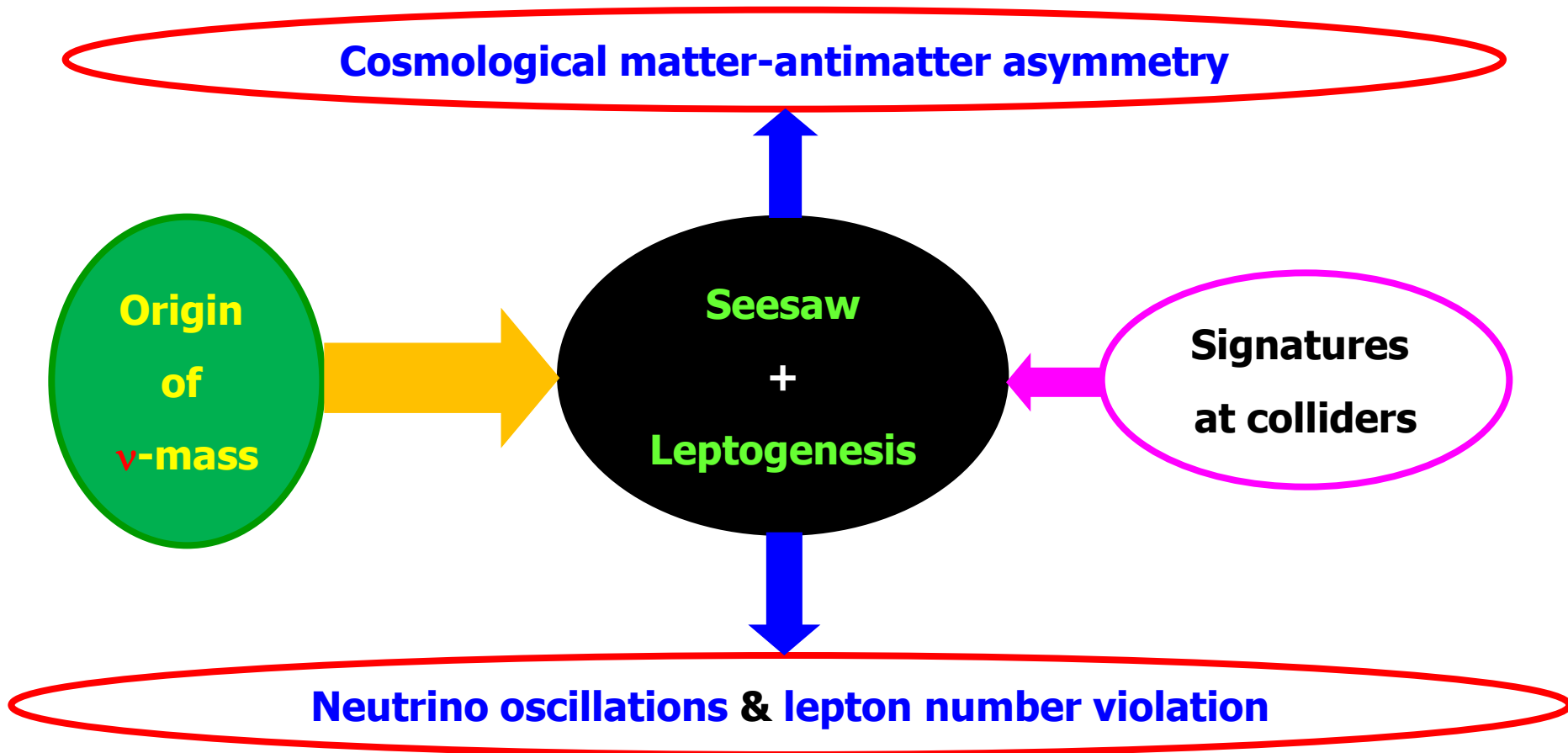
56

Flavor effect: Barbieri et al **00**; Endoh et al **04**; Pilaftsis **05**; Abada et al **06**; Nardi et al **06**; ... (Review: Davidson, Nardi, Nir, Phys. Rept. **08**).



A Grand Picture?

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Cosmic messenger: neutrino astronomy and neutrino cosmology.
Surprise maker: history of neutrino physics was full of surprises.

Cosmic Flavor Physics

C ν B

Hot DM

keV ν 's
Warm DM

Baryogenesis
Leptogenesis

Energetic ν 's
from cold DM

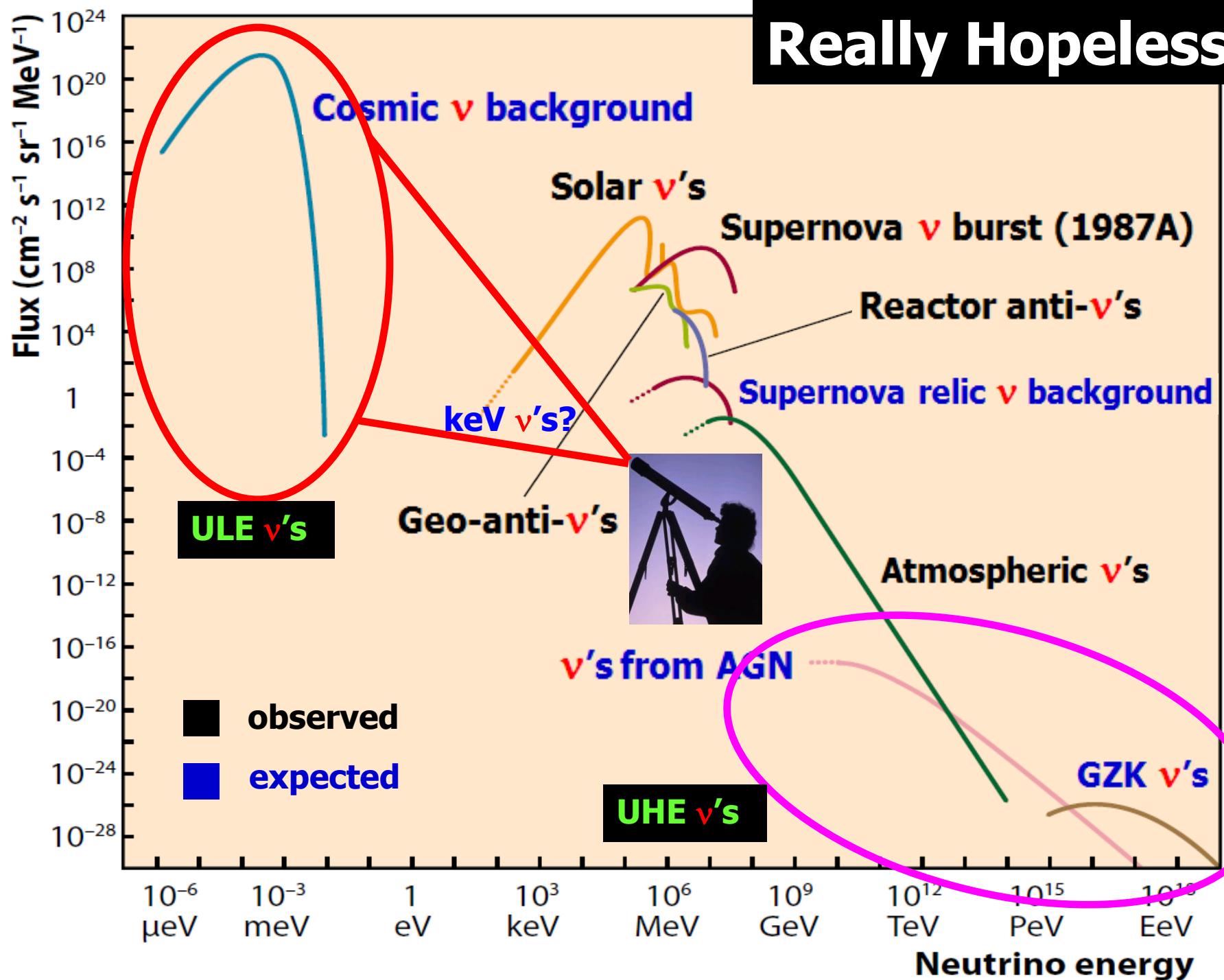
UHE
Cosmic ν 's

Supernova ν 's
(relic background)

.....

A New Road Ahead?

Really Hopeless?





L. Pauling



good
idea?

Thank you for your attention!